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AN MOS-LSI AUTOCORRELATION
LINEAR PREDICTION SYSTEM
by
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# AN MOS-LSI AUTOCORRELATION LINEAR PREDICTION SYSTEM 

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# An MOS-LSI Autocorrelation Linear Prediction System 

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## ABSTRACT

Integration of an autocorrelation linear prediction system for speech analysis will be described. The system is composed of both analog. switchedcapacitor and digital circuitry. A switched-capacitor autocorrelator is the key component of the system. Accuracy requirements both in the analog and digital processing domains are carefully considered for the speech application. Practical aspects of speech processing are discussed.

The autocorrelator was fabricated on an analog/digital compatible CMOS process. The design, layout, and fabrication of the integrated circuit are described. Experimental results are presented for the autocorrelator integrated circuit as well as the complete linear prediction system.

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## CHAPTER 1

## INTRODUCTION

Recently, synthetic speech has appeared in many consumer products such as automobiles, educational games for children, chess games, microwave ovens, and alarm clocks. The successful integration of speech synthesis algorithms in silicon technology has provided manufacturers with low cost speech synthesis systems. But the inverse process, speech analysis, has remained a task handled by large computer systems or expensive general purpose signal processing integrated circuits, often not operating in real time. Vocoders, store-and-forward message systems, and speech recognition systems will remain prohibitively expensive unless low cost analysis systems are made available.

A real-time linear predictive speech analysis system is described in this thesis. The analysis system employs a mix of switched-capacitor analog circuitry and MOS digital circuitry. The heart of the system is a switchedcapacitor autocorrelation integrated circuit (IC). An automatic gain control circuit which reduces the dynamic range of the incoming speech precedes the autocorrelator. A small microprocessor system converts the autocorrelator's output into linear prediction model coefficients.

The autocorrelator itself was integrated as the final stage of this research. The chapters follow the design of the system from start to finish, roughly in chronological order. Chapter 2 covers the speech analysis theory which forms the basis of the IC. Chapter 3 presents circuits which are used to implement the system. The operation of the circuits is explained. In chapter

4, the circuits chosen in chapter 3 are discussed in detail. Non-idealities due to integration of the circuits in MOS technology are considered. Various system-level design decisions are made. The design, layout, and processing of the autocorrelator IC are discussed. Chapter 5 presents the results obtained from the breadboarded system and from the autocorrelator IC. Conclusions and suggestions are made in chapter 6.

## CHAPTER 2

## LPC THEORY AND APPLICATIONS

Speech is a verbal form of communication. The rate at which information is transmitted during a conversation is approximately 100 bits per second [1]. Hence, speech could theoretically be encoded in such a way as to convey all the information while transmitting only 100 bits per second. One simple digital transmission scheme used today, 8 bit quantization of speech sampled at 8 kHz , requires 64k bits per second. This is 640 times larger than the information rate, the discrepancy reflects how inefficient direct transmission of the speech time waveform is.

The speech waveform is a sequence of sounds. In the case of vowels, each sound is a periodic repetition of a distinct waveform. Speech analysis attempts to eliminate the transmission of the redundant information in the time waveform Many different techniques have been applied to speech analysis, some meeting with more success than others. Mathematical tractability and automatic implementation of analysis algorithms are very desirable properties. One analysis method, linear predictive coding (LPC), has these properties and has been widely applied to the speech analysis problem. Autocorrelation LPC will be described in detail in the following sections.

### 2.1. A YODELL FOR SPEFPCH

To understand speech analysis, we must flrst understand how we produce speech sounds. A sound is produced as follows (see figure 2.1):

Air is forced out of the lungs by muscle contraction. As the air passes through the vocal cords, it is either allowed to flow through unrestricted (unvoiced sounds), or it is transformed into short bursts of air by the periodic opening and closing of the vocal cords (voiced sounds). The air then passes through the vocal tract. The shape of the vocal tract and position of the lips and tongue determine the resonant frequencies (formants) of the sound. The vocal tract acts as an acoustic filter, spectrally shaping the air pressure wave as it passes from the vocal cords to the lips.

A simple model for the speech production process described is shown in figure 2.1. The unrestricted flow of air at the vocal cords is modeled as white noise. The periodic bursts of air at the vocal cords are modeled as periodic


Figure 2.1. Cross-section of the vocal tract (left) and a simple model for the speech production process (right)
impulses. The period of the impulses is called the pitch period. The vocal tract is modeled as a time-varying filter.

Most speech synthesizers are realizations of this simple model. The excitation waveform and filter parameters are changed at a rate of 20 Hz to 100 Hz . Each segment of synthetic speech produced by a given set of parameters is called a frame of speech. The update rate or frame rate corresponds to the rate at which different sounds occur in conversational speech.

In speech analysis, the inverse process is performed. The continuously changing speech waveform is broken into pitch and vocal tract information each frame. There are many different approaches to speech analysis [1]; one particular method will be described in detail.

### 2.2. LPC THEORY

With LPC, the present speech sample is modeled as a linear combination of the past $p$ speech samples plus an unknown input

$$
s(n)=\sum_{i=1}^{n} a_{i} s(n-i)+b u(n) ;
$$

$s(n)$ is the sample of the speech waveform $s(t)$ at time $t=\pi T_{s}$ ( $T_{s}$ is the sampling period), $u(n)$ is the input (glottal excitation), and $a_{i}$ is the $i^{\text {th }}$ LPC coefficient. In the frequency domain, this prediction equation gives an allpole transfer function

$$
\begin{equation*}
G(z)=\frac{S(z)}{U(z)}=\frac{b}{1-\sum_{i=1}^{D} a_{i} z^{-i}} \tag{2.1}
\end{equation*}
$$

$S(z)$ and $U(z)$ are the $z$-transforms of $s(n)$ and $u(n)$, respectively. For a given sound, LPC finds an all-pole filter $G(z)$ which models the vocal tract transfer function. The LPC model can be viewed physically as a cascade of $p$ acoustic tubes of constant length and differing cross-sectional area [2]. The
cross-sectional areas are related to the LPC coefficients (see section 2.4). An LPC transfer function is plotted in flgure 2.2, superimposed on the FFT of the same sound. The LPC all-pole filter attempts to model the resonances of the vocal tract (see section 2.5). Each resonance modeled requires a complex conjugate pair of poles. Typically, vocal tract resonances are spaced 1 kHz apart. So if the speech waveform is sampled at a frequency $f_{s}=\frac{1}{T_{s}}$ - so that we are modeling the vocal tract from OHz to $\frac{f_{3}}{2}$-we need a minimum of $\boldsymbol{p}=\frac{\boldsymbol{f}_{\mathbf{2}}}{1 k H z}$ poles to model the vocal tract resonances. One or two more poles are often included to model the non-flat spectrum of the glottal waveform.

In LPC speech analysis, we are given the speech waveform $s(n)$ and want to determine the LPC coefficients, $a_{i,} 1 \leq i \leq p$. Since we have no prior information about the excitation $u(n)$, we predict the present sample $s(n)$ from the


Figure 2.2 LPC fit (solid line) to a speech spectrum (broken line)
past $p$ samples

$$
s(n)=\sum_{i=1}^{R} \alpha_{i} s(n-i)
$$

The error between the actual speech sample $s(n)$ and the predicted value $\bar{s}(n)$ is the prediction error $e(n)$

$$
\begin{equation*}
e(n)=s(n)-\bar{s}(n) \tag{2.2}
\end{equation*}
$$

There are various error minimization criterion which might be used to find the LPC coefficients. One is to minimize the total squared error $E_{p}$

$$
\begin{equation*}
E_{p}=\sum_{n=-\infty}^{\infty} s^{2}(n)=\sum_{n=-\infty}^{\infty}[s(n)-\bar{s}(n)]^{2} \tag{2.3}
\end{equation*}
$$

To minimize $E_{p}$, we differentiate $E_{p}$ with respect to $a_{k}$ and set $\frac{\partial E_{p}}{\partial a_{t}}=0$ for each $k, 1 \leq k \leq p$. This yields $p$ linear equations

$$
\sum_{i=1}^{\infty} a_{i} \sum_{n=-\infty}^{\infty} s(n-i) s(n-k)=\sum_{n=-\infty}^{\infty} s(n) s(n-k) \text { for } 1 \leq k \leq p
$$

which can be rewritten

$$
\begin{equation*}
\sum_{i=1}^{p} a_{i} R(k-i)=R(k) \quad 1 \leq k \leq p \tag{2.4}
\end{equation*}
$$

where

$$
\begin{equation*}
R(k)=\sum_{n=-\infty}^{\infty} s(n) s(n-k) \tag{2.5}
\end{equation*}
$$

is the autocorrelation function of the speech signal $s(n)$. The solution of (2.4) for the LPC coefficients requires solution of $p$ linear equations in $p$ unknowns. This will be discussed in section 2.4.

### 2.3. TINDOITNG

Note that equation (2.3) minimizes the error over all time. If $s(n)$ is a constant sound, $R(k)$ will be that sound's autocorrelation function and solving equation (2.4) will give LPC coefficients for that sound. But for conversational speech, $s(n)$ is a continuously varying sequence of sounds. Therefore, we
would like to compute $R(k)$ separately for each frame (which should correspond to only one sound if the frame size is chosen properly). Then we can find the LPC coefficients for that particular frame. To achieve this, we window the speech waveform. That is, we multiply the speech waveform by a window function $w(n)$ which weights the present frame more heavily than other frames. This windowing gives a new time waveform $s_{w}(n, j)$

$$
s_{w}(n, j)=s(n) w(n-j)
$$

where $j$ accounts for the positioning of the window. Then this windowed speech $s_{w}(n, j)$ is used in the autocorrelation computation, equation (2.5), to give

$$
\begin{equation*}
R(k, j)=\sum_{n=-\infty}^{\infty} s_{w}(n, j) s_{w}(n-k, j)=\sum_{n=-\infty}^{\infty} s(n) w(n-j) s(n-k) w(n-k-j) \tag{2.6}
\end{equation*}
$$

Since the application of a window results in an autocorrelation function based on short segments of the speech signal, (2.6) is often referred to as the short-time autocorrelation function. Since equation (2.6) is the only autocorrelation function which will be discussed from here on, it will be simply referred to as the autocorrelation function.

The time window $w(n)$ can be of finite duration (FIR) or infinite duration (IIR) (figure 2.3). In either case, the window should have no discontinuities, going smoothly to zero at the window's endpoints. This minimizes the spectral smearing of the formants due to the window [ 1 ]. If an FIR window is chosen, equation (2.6) may be implemented by first computing the sequence $s_{w}(n, j)=s(n) w(n-j)$, then using the windowed speech in equation (2.6). This approach is straightforward; requiring permanent storage (ROM) for the sequence $w(n)$, temporary memory (RAM) for storing the windowed sequence $s_{w}(n, j)$, a multiplier, and a summer [ 3 ].



Figure 2.3. top: FIR time window (e.g. a Hamming window) bottom: IIR time window suggested by Barnwell

The windowing and summation in equation (2.6) can be implemented as a filter following a multiplier for both the FIR and IIR windows. This can be seen by defining a time-reversed version of the window

$$
h(n)=w(-n) .
$$

Then (2.6) becomes

$$
\begin{equation*}
R(k, j)=\sum_{n=-\infty}^{\infty} s(n) h(j-n) s(n-k) h(j-n+k) . \tag{2.7}
\end{equation*}
$$

If we define

$$
\begin{aligned}
& s_{k}^{\prime}(n)=s(n) s(n-k) \\
& h_{k}^{\prime}(n)=h(n) h(n+k)
\end{aligned}
$$

and substitute these into (2.7), we have

$$
R(k, j)=\sum_{n=-\infty}^{\infty} s_{k}^{\prime}(n) h_{k}^{\prime}(j-n) .
$$

We can see that $R(k, j)$ is the convolution of $s_{k}^{\prime}(n)$ with $h_{k}(\boldsymbol{n})$. So if we can produce the time sequence $s_{k}^{\prime}(n)$ and pass it through the linear, time invariant filter with impulse response $h_{k}^{\prime}(n)$, the output of the filter at time $j$ will be the autocorrelation function for lag $k, R(k, j)$.

Producing the sequence $s_{k}^{\prime}(n)$ requires only multiplication and delay. To find the $z$-domain transfer function for the filter with impulse response

$$
h_{k}^{\prime}(n)=h(n) h(n+k)
$$

we recall that multiplication in the time domain corresponds to convolution in the frequency domain. So if we denote the $z$-transforms of the sequences

$$
h(n) \rightarrow H(z)
$$

and

$$
h_{k}^{\prime}(n) \rightarrow H_{k}^{\prime}(z)
$$

then the shifted sequence $h(\pi+k)$ has the transform

$$
h(n+k) \rightarrow z^{k} H(z) .
$$

Now $H_{k}^{\prime}(z)$ can be found [4]

$$
\begin{equation*}
H_{k}^{\prime}(z)=H(z) * z^{k} H(z)=\frac{1}{2 \pi j} \int H(v) H\left(\frac{z}{v}\right) v^{k-1} d v . \tag{2.8}
\end{equation*}
$$

So once a window $w(n)=h(-n)$ has been chosen, $H(z)$ is determined and $H_{k}(z)$ can be found by integration in the complex plane (see appendix A).

For example, let us take

$$
w(n)= \begin{cases}(1-n) \alpha^{-n} & n \leq 0  \tag{2.9}\\ 0 & n>0\end{cases}
$$

where $0<\alpha<1$. The corresponding $h(n)$ is

$$
h(n)= \begin{cases}(1+n) \alpha^{n} & n \geq 0 \\ 0 & n<0\end{cases}
$$

with z-transform

$$
\begin{equation*}
H(z)=\sum_{n=0}^{\infty} h(n) z^{-n}=\frac{1}{\left(1-\alpha z^{-1}\right)^{2}} \tag{2.10}
\end{equation*}
$$

$H(z)$ is a low pass filter with two coincident real poles. Substituting this $H(z)$ into (2.8) and evaluating the integral gives

$$
\begin{equation*}
H_{k}^{\prime}(z)=\frac{(k+1) \alpha^{k}+(1-k) \alpha^{k+2} z^{-1}}{\left(1-\alpha^{2} z^{-1}\right)^{3}} \tag{2.11}
\end{equation*}
$$

(see appendix A). Note that each value of $k$ corresponds to a different filter.

| Filter Specifications |  |  |  |
| :---: | :---: | :---: | :---: |
| lag | poles | zero | $\frac{H_{k}^{\prime}(1)}{H_{0}^{\prime}(1)}$ |
|  |  |  |  |
| $\mathbf{k}=0$ | 0.9604 | -0.9604 | 1.000000 |
| $\mathrm{k}=1$ | 0.9604 | 0.0000 | 0.999796 |
| $\mathrm{k}=2$ | 0.904 | 0.3201 | 0.999184 |
| $\mathrm{k}=3$ | 0.9604 | 0.4802 | 0.998215 |
| $\mathrm{k}=4$ | 0.9604 | 0.5762 | 0.996888 |
| $\mathrm{k}=5$ | 0.9604 | 0.6403 | 0.995205 |
| $\mathrm{k}=6$ | 0.9604 | 0.6860 | 0.993216 |
| $\mathrm{k}=7$ | 0.904 | 0.7203 | 0.990869 |
| $\mathbf{k}=8$ | 0.9604 | 0.7470 | 0.988268 |
| $\mathrm{k}=9$ | 0.9604 | 0.7883 | 0.985309 |

Table 2.1. Filter specifications for $H_{k}{ }_{k}(z)$

All the filters have three poles at $z=\alpha^{2}$ and one real zero. Barnwell has found that for an 8 kHz sampling rate, $\alpha=0.98$ is the best choice [ 5 ]. This window gave spectral errors comparable to a 240-point FIR Hamming window. For the case $\alpha=0.98$, the pole and zero locations and the relative DC gains $\frac{H_{k}^{\prime}(1)}{H_{0}^{\prime}(1)}$ are tabulated in table 2.1. The magnitude response of the filters is shown in figure 2.4. Note the effect of the zero. For all the filters, the -3 dB frequency is 25 Hz .

A block diagram of an autocorrelator employing the IIR window of equation (2.9) is shown in figure 2.5. The autocorrelator requires a $p$ stage delay line, multipliers, and filters. Note that the temporary memory storage (RAM) required is only $4(p+1)+p$. The multiplier in the IIR autocorrelator must be approximately twice as fast as the FIR autocorrelator's multiplier. The IIR autocorrelator outputs values for $R(k)$ every sample, this is useful in some applications (see section 2.7).

The delay line, multipliers, and filters of figure 2.5 can all be implemented as analog or digital circuits. A mix of analog and digital circuits will be used in the autocorrelator described in later chapters.

### 2.4. LPC COEFFICIBNT COKPUTATION - DURBIN'S RECURSION

Once the autocorrelation values for a particular frame have been computed, the set of linear equations (2.4) must be solved to determine the LPC coefficients. The equations can be compactly written in matrix form


Figure 2.4 top: Magnitude response of filter $H_{0}(z)$
bottom: Magnitude response of filters $H_{0}^{\prime}(z), H_{1}^{\prime}(z)$, and $H_{0}{ }_{0}(z)$

$$
\left[\begin{array}{ccccc}
R(0) & R(1) & R(2) & \cdots & R(p-1)  \tag{2.12}\\
R(1) & R(0) & R(1) & \cdot & \cdot \\
R(2) & R(1) & R(0) & \cdot & \cdot \\
\cdot & \cdot & \cdot & \cdot & \cdot \\
\cdot & \cdot & \cdot & \cdot & \cdot \\
R(p-1) & R(p-2) & \cdot & \cdot & R(0)
\end{array}\right]\left[\begin{array}{c}
a_{1} \\
\alpha_{2} \\
\alpha_{3} \\
\cdot \\
\cdot \\
a_{p}
\end{array}\right]=\left[\begin{array}{c}
R(1) \\
R(2) \\
R(3) \\
\cdot \\
R(p)
\end{array}\right]
$$

or

$$
R \cdot \mathbf{a}=\mathbf{r}
$$

where $R$ is the $p \times p$ autocorrelation matrix, $a$ is the $p \times 1$ vector of LPC coefficients, and $\mathbf{r}$ is the $p \times 1$ vector of autocorrelation values. In equation (2.12), the relation $R(k)=R(-k)$ has been used, and the time dependence of $R(k)$ has been dropped for simplicity. The $a_{i}$ 's could be found by inverting the $\mathbf{R}$ matrix and multiplying both sides by $R^{-1}$. This would require $\frac{p^{9}}{3}+O\left(p^{2}\right)$ operations (multiplications or divisions) and $p^{2}$ storage locations. Fortunately, the autocorrelation matrix is symmetric, and the elements along any diagonal are identical. Such a matrix is Toeplitz, and Levinson and Durbin derived efficient recursion relations for solving such linear equations [ 6 ], [7]. The Durbin algorithm is the faster algorithm, requiring $p^{2}+O(p)$ operations and $2 p$ storage locations.

Durbin's recursive solution to (2.12) is

$$
\begin{array}{ll}
\text { start: } & E_{0}=R(0) \\
& m=0 \\
\text { loop: } & m=m+1
\end{array}
$$

$$
\begin{aligned}
& k_{m}=\frac{R(m)+\sum_{i=1}^{m-1} a m^{m-1} R(m-i)}{E_{m-1}} \\
& a_{m}^{m}=k_{m} \\
& a_{l}^{m}=a_{i}^{m-1}-k_{m} a_{m-i}^{m-1} \quad 1 \leq i \leq m-1
\end{aligned}
$$



Figure 2.5. Block diagram of autocorrelator employing the $\Pi$ IR window of equation (2.9)

$$
\begin{equation*}
E_{m}=\left(1-k_{m}^{z}\right) E_{m-1} \tag{2.13}
\end{equation*}
$$

if $(m<p)$ go to loop;
else stop;
$a_{i}^{m}$ is the $i^{\text {th }}$ LPC coefficient for an m-pole model. The loop evaluates the LPC coefficients for all models of order less than or equal to $\boldsymbol{p}$. The algorithm terminates when the model of order $p$ has been found. $E_{p}$, the total squared error (equation (2.3)), is computed in the Durbin algorithm (equation (2.13)). The algorithm computes the LPC coefficients as well as the reflection coefficients (the $k_{i}$ 's). The reflection coefficients have a physical interpretation. As was mentioned in section 2.2, the LPC model of the vocal tract can be viewed as a cascade of $p$ acoustic tubes of equal length and differing crosssectional area. If the $i^{\text {th }}$ acoustic tube of has area $A_{i}$, then

$$
k_{i}=\frac{A_{i-1}-A_{i}}{A_{i-1}+A_{i}}
$$

In low-bit rate transmission of speech, the reflection coefficients are quantized and transmitted because the LPC model is less sensitive to quantization of the reflection coefficients than to quantization of either the autocorrelation values or the LPC coefficients.

The LPC analysis fails to give a stable all-pole filter when $\left|k_{i}\right|>1$ for any $i$ [2]. If $\left|k_{i}\right|>1$, then $E_{i}<0$ which contradicts the definition of $E_{i}$ as the total squared error which must always be non-negative (see equation (2.13)). In terms of acoustic tubes, $\left|k_{i}\right|>1$ corresponds to either $A_{i}<0$ or $A_{i-1}<0$; neither makes sense physically. It has been shown that the autocorrelation method always produces a stable filter if all computations are performed with infinite precision [ 8 ]. In practice, the use of fnite precision arithmetic can result in an unstable filter.

At this point, it is worth noting that the solution of (2.12) for the LPC coefficients is not affected if all the autocorrelation values $\dot{R}(k)$ are scaled by a non-zero constant. For example, if we replace each $R(k)$ in (2.12) with $c R(k)$, then the $c$ factors out to give $c \operatorname{Ra}=c r$ which reduces to $R a=r$. This observation is of interest in later chapters.

The gain in the LPC model ( 6 in equation (2.1)) has not been determined because it is associated with the input $u(n)$ which is unknown. But we may assume the input $u(n)$ is either an impulse $\delta(n)$ (for voiced speech) or samples of a white noise process (for unvoiced speech) with the property that the energy in $u(n)$ is unity. With that constraint, and the reasonable requirement that the energy in the LPC model equal the energy in the speech, it can be shown [8] that

$$
b^{2}=E_{p}=R(0)+\sum_{k=1}^{R} a_{k} R(k) .
$$

### 2.5. FPEEQUENCY DOMADN INTERRPRETATION OF IPC

The popularity and success of LPC is due to LPC's accurate modeling of the resonances of the vocal tract. Early experiments determined that the spectral peaks were perceptually far more important than spectral valleys [9]. The LPC error criterion will now be considered in the frequency domain where the reason for the accurate resonance modeling can be seen.

Recall the definition of the prediction error in equation (2.2)

$$
g(n)=s(n)-s(n)=s(n)-\sum_{i=1}^{n} a_{i} s(n-i)
$$

which transforms to

$$
E(z)=\left[1-\sum_{i=1}^{n} a_{i} z^{-i}\right] S(z)=A(z) S(z)
$$

where $A(z)$ is the denominator of the vocal tract model (equation (2.1))

$$
G(z)=\frac{b}{A(z)}=\frac{b}{1-\sum_{i=1}^{n} a_{i} z^{-i}}
$$

Now the total squared error of (2.3) can be evaluated in the frequency domain by invoking Parseval's Theorem

$$
E_{p}=\sum_{n=-0}^{\infty} e^{2}(n)=\frac{1}{2 \pi} \int_{-\pi}^{\pi}\left|E\left(e^{j u}\right)\right|^{2} d \omega=\frac{1}{2 \pi} \int_{-\pi}^{\pi}\left|S\left(\varepsilon^{j u}\right)\right|^{2}\left|A\left(e^{j v}\right)\right|^{2} d \omega
$$

which can be rewritten

$$
\begin{equation*}
E_{p}=\frac{b^{2}}{2 \pi} \int_{-\pi}^{\pi} \frac{\left|S\left(e^{j u}\right)\right|^{2}}{\left|G\left(e^{j \omega}\right)\right|^{2}} d \omega . \tag{2.14}
\end{equation*}
$$

From this equation, we can see that $E_{p}$ depends on the integrated ratio of two spectra. Points where $|G|$ is smaller than $|S|$ make a larger contribution to the total error than points where $|G|$ is larger than $|S|$. Therefore, the error minimization (2.14) can be viewed in the frequency domain as one which
weights the modeling of spectral peaks more than valleys. So LPC models the resonances of the vocal tract very well.

### 2.6. PRACTICAL CONSIDERRATIONS IN SPEECH ANALYSSS

### 2.6.1. PRE-EMPHASTS

The speech production process was explained earlier. A long-time spectrum for continuous speech shows a roll-off of approximately $-6 \mathrm{~dB} /$ octave above 500 Hz [ 10 ]. This is typical of voiced sounds. The speech spectrum is the product of the excitation's spectrum, the vocal tract transfer function, and the lip-to-air radiation transfer function. The glottal excitation for voiced sounds has a -12dB/octave slope at high frequencies. The vocal tract has unity transfer gain at each resonance and the lip-to-air radiation has a $+8 \mathrm{~dB} /$ octave characteristic at high frequencies. The net effect is a $-6 \mathrm{~dB} /$ octave roll-off at high frequencies as shown in figure 2.6.

To achieve the most accurate model of the spectral peaks, it is advantageous for all spectral peaks to have the same magnitude. Otherwise, the LPC error criterion will cause the lower amplitude peaks to be modeled much more poorly that the higher amplitude peaks. Therefore, the speech waveform is pre-emphasized before LPC analysis is begun. The pre-emphasis is in the form of a simple, one zero filter (zero at 500 Hz ) which removes the $-6 \mathrm{~dB} /$ octave roll-off present in typical voiced speech spectra. Pre-emphasis reduces the likelihood of instability in the LPC model $G(z)$ [2].

Ideally, pre-emphasis is applied only to voiced speech since unvoiced speech does not have the $-8 \mathrm{~dB} /$ octave roll-off characteristic (because the excitation for unvoiced speech doesn't have the $-12 \mathrm{~dB} /$ octave roll-off). But usually a constant pre-emphasis filter is used for all speech, voiced and


Time Domain


Frequency Domain


Figure 2.6. Construction of the speech waveform in time and frequency domains
unvoiced. The main reason is that unvoiced speech has a very simple spectral shape associated with it, hence modeling is fairly simple and is not hampered by pre-emphasis. Furthermore, the voiced/unvoiced decision is not an easy one; and the modeling error resulting from not pre-emphasizing a voiced segment of speech is much larger than the error resulting from pre-emphasizing an unvoiced segment. Also, adaptive pre-emphasis requires additional analysis of the speech to determine the optimal pre-emphasis filter.

### 2.6.2. DYNAMIC RANGE

Another concern is the dynamic range of the incoming speech. With a particular speaker, the speech has a dynamic range on the order of 30 dB . When different speakers and slight variations in the speaker-to-microphone distance are allowed, the dynamic range increases to 40 dB . If the incoming
speech is quantized by a linear analog-to-digital converter (ADC), 7 bits of resolution would be necessary. More bits would be used in practice to minimize clipping and quantization noise; a 10 or 12 bit $A D C$ is commonly utilized.

To eliminate the need for a 10 or 12 bit $A D C$ at the input, an automatic gain control (AGC) circuit should be used. A properly designed AGC would decrease the dynamic range of the speech considerably without affecting the speech's spectral characteristics and thereby relax the ADC requirements. An 8 bit ADC is sufficient if an AGC is employed (see chapter 4). The AGC would scale all the speech samples in a given frame and hence the frame's autocorrelation values $R(k)$. As was noted in section 2.4, scaling all the autocorrelation values does not change the resulting LPC coefficients.

### 2.6.3. ANTI-ALIAS FILTER

Before sampled-data processing can begin, the speech must be bandlimited to $\frac{f_{s}}{2}$. If the bandlimiting filter causes a large attenuation of the speech spectrum below $\frac{f_{3}}{2}$, some of the LPC parameters will be wasted modeling this attenuation near $\frac{f_{3}}{2}$ This is undesirable. So a high order filter or elliptic filter with a sharp roll-off characteristics and cutoff frequency close to $\frac{f_{s}}{2}$ is preferred. Unfortunately, such a filter introduces significant phase nonlinearity. But as can be seen from equation (2.14), the LPC error criterion depends only on the magnitude of the spectrum of the incoming speech - not on the phase.

### 2.7. OTHER APPLICATIONS OF THE AUTOCORRINATOR

Autocorrelators have many uses in speech processing. In addition to LPC analysis for speech transmission, some speech recognition systems use an autocorrelation-based LPC distance measurement between sounds. The Itakura-Saito measure [ 11 ] requires storage of a reference template for each sound, the template is the sound's LPC coefficient vector arof (see equation (2.12)). When an unknown sound is uttered, its autocorrelation matrix $\mathbf{R}$ is found (see equation (2.12)), and the distance between the unknown sound and each reference template is computed as

$$
\begin{equation*}
d=10 \log \left[\frac{a_{\mathrm{Te}} / \mathrm{Ra} \mathrm{Ra}_{\mathrm{a}} \rho}{a^{T} \mathrm{Ra}}\right] \tag{2.15}
\end{equation*}
$$

$\mathbf{a}^{T}$ is the transpose of a The denominator is the minimum LPC error $E_{p}$ achievable for a p-pole model of the unknown frame (see equation (2.3)) [8]. The numerator represents the total error $E_{p}^{\prime}$ obtained if the unknown frame of speech is modeled by the stored template $a_{\text {ref }}$. Therefore the numerator will always be greater than or equal to the denominator, so the ratio is greater than or equal to one and therefore $d \geq 0$. This distance measure will equal zero only if $a_{r o f}=a$ i.e. when the unknown speech and the reference template have identical LPC spectra.

Pitch detection is an extremely difficult problem, and pitch detection errors are more often responsible for poor quality synthetic speech than are vocal tract modeling errors. The best pitch detectors rely on a variety of pitch detection techniques, one technique is the autocorrelation technique [12]. The autocorrelation function, if computed over a time much larger than the pitch period, will be periodic with period equal to the pitch period. This periodicity is easily measured; a simple peak-to-peak distance measurement on the autocorrelation function reveals the pitch period. The autocorrelation
function should be computed every sample to find the pitch period, and an IIR autocorrelator is an excellent choice for such an application. Accuracy of the autocorrelation values is not crucial, so simpler filters (e.g. one pole filters) for $H^{\prime}{ }_{k}(z)$ could be used.

The voiced/unvoiced/silence decision used in pitch detectors, speech recognition systems, adaptive pre-emphasis subsystems, and telephone multiplexing systems can be made very accurately using the first few autocorrelation values $R(0), R(1), R(2)$ and a zero-crossing detector [13].

## CHAPTER 3

## CIRCUITS FOR THE AUTOCORRELATION LPC SYSTEM

Circuitry for implementing a nine pole autocorrelation LPC analysis system will be described in this chapter. The autocorrelator employs the IIR window discussed in chapter 2. The system is a mix of analog and digital circuitry. A completely digital implementation of the LPC system - excluding the input antialias filter - would be possible, either by designing a custom integrated circuit (IC) or by programming a general purpose digital signal processor. But combining analog MOS switched-capacitor techniques and digital MOS circuitry potentially offers a lower power, smaller area integrated circuit approach.

In this chapter, circuits are presented for each major block of the system, and their operation is described. So as not to cloud the functional descriptions, non-idealities associated with the IC implementation are not considered until next chapter.

### 3.1. SYSTHM OVERVIEW

A block diagram of the complete system is shown in figure 3.1. The speech first passes through a bandlimiting, low pass filter. The filter is a fifth order elliptic which has a -3 dB cutoff frequency of $3.4 \mathrm{kHz}, 1 \mathrm{~dB}$ of passband ripple, and includes a zero at 500 Hz for pre-emphasis. The bandlimited, pre-emphasized speech passes through an automatic gain control circuit (AGC) and then to the autocorrelator where the autocorrelation values for the present frame are computed. The ten autocorrelation values are transformed to LPC coefficients by a small microprocessor system. The


Figure 3.1. LPC system block diagram
speech is sampled at a rate of $f_{\mathrm{z}}=8 \mathrm{kHz}$; the autocorrelation values are sampled at a frame rate of 80 Hz .

### 3.2. THE AUTOCORREHATOR

### 3.2.1. CIRCUIT OPTIONS

An autocorrelator using the IIR window of equation (2.9) requires delay, multiplication, and filtering. An analog delay line of length $p$ can be constructed by cascading $p$ switched-capacitor (SC) sample-and-hold circuits. Such a delay line requires $p$ operational ampliffers ( $O p \mathrm{amps}$ ). Time multiplexing of one op amp and $p$ capacitors to implement a $p$ stage delay is possible [ 14 ]. If the signal to be delayed is available in digital form, a RAM of $p$ words will function as a $p$ stage delay line.

Fast. accurate multiplication of signals is another requirement of the autocorrelator. A digital multiplier provides exact multiplication of two digital numbers. Multiplication speed can be directly traded for IC area - a parallel multiplier is faster and larger than a serial multiplier. A multiplying digital-to-analog converter (MDAC) provides accurate multiplication of a digital signal with an analog signal; the product is in the form of an analog output voltage. The time per multiply for an MDAC is dependent on the speed of the op amp used and the type of MDAC (e.g. serial or parallel). Analog continuous time multipliers which multiply two analog signals and produce an analog product as output are also available. The digital multiplier is compatible with a digital delay line, the MDAC with either a digital or analog delay line, and the analog multiplier with an analog delay line.

The filters required for the autocorrelator are third-order low pass filters with a cutoff frequency of 25 Hz . Digital filtering is required if a digital multiplier is chosen to multiply the speech signals. If either the MDAC or analog multiplier is chosen, the signal to be filtered will be analog. Either continuous time or discrete time analog filters can be used, but a 25 Hz cutoff frequency would require a much larger chip area in a continuous time (resistorcapacitor) implementation. SC filters are discrete time filters and hence are described by $z$-domain transfer functions, so they can accurately realize the transfer functions $H_{k}^{\prime}(z), 0<k<9$, required for this system (see equation (2.11)). With a sampling rate of 8 kHz , the 25 Hz low pass filters can be integrated as SC filters in a reasonable amount of silicon area. (For further discussion of analog circuits for signal processing, see appendix B.)

## s.2.2. THE SHIECTED CIRCUITS

The autocorrelator must provide adequate accuracy for speech analysis. Also, the goal of integrating the autocorrelator onto an IC must be considered. The above discussion breaks down to three basic choices - fully analog, fully digital, or some combination thereof. The fully analog autocorrelator - analog delay line, continuous time analog multiplier, and SC filters could be constructed with only four op amps using multiplexed op amps for the filters and delay line. An ADC would be required to digitize the analog autocorrelation values for the microprocessor which implements the Durbin algorithm. A fully digital approach would require an $A D C$ to digitize the incoming speech for processing. Previous work on autocorrelation LPC with finite word length arithmetic recommends 16 bit by 16 bit multipliers and 32 bit intermediate results to minimize the effects of quantization and truncation [15].[ 16 ]. A fast parallel multiplier could be multiplexed to handle all computations. Such a digital autocorrelator would essentially be a custom designed digital signal processor with a hardware multiplier and very limited instruction set. A hybrid approach - consisting of an MDAC, digital delay line, and SC filters - could be constructed with only three op amps because the MDAC can be incorporated into one of the SC filter sections as a variable input capacitor (see chapter 8 for more on this). Again, an ADC is required to digitize both the incoming speech and the autocorrelation values.

The hybrid approach potentially offers the lowest power, smallest area IC of the three options, as well as high accuracy and simple control logic. This approach was chosen for integration of the autocorrelator. Circuits for the MDAC and filters are considered below. Accuracy and circuit limitations are discussed in the following chapter.

The speech is sampled at an 8 kHz rate, so the time between samples is $125 \mu$ seconds. This is a very long time when compared to typical op amp settling times which are on the order of microseconds. Therefore it is possible and advantageous to employ time multiplexing of the MDAC and filters for the computation of the autocorrelation values. Time multiplexing results in the most efficient use of integrated circuit area.

The autocorrelator block diagram is shown in figure 3.2. The preprocessed speech is sampled at $f_{\mathrm{s}}=8 \mathrm{kHz}$ and held for the analog-to-digital converter (ADC) and multiplying digital-to-analog converter (MDAC). The digitized sample $s_{d}(n)$ (i.e. $s(n)$ digitized) is stored in RAM along with past samples $s_{d}(n-k), 1 \leq k \leq 9$. The $125 \mu$ second sampling period is broken into ten $12.5 \mu$ second time slots. During the $k^{\text {th }}$ time slot, the sample $s_{d}(n-k)$ is read out of RAM and presented as the digital input to the NDAC where it is


Figure 3.2 Autocorrelator block diagram
multiplied by the MDAC's analog input $s(n)$. The analog output of the MDAC, $s(n) s_{d}(n-k)$, is multiplexed to the $k^{\text {th }}$ SC filter (with transfer function $H_{k}^{\prime}(z)$, equation (2.11)) which implements the windowing and summation for the computation of $R(k)$. This procedure is carried out for each of the ten time slots, $0 \leq k \leq 9$; then the process is repeated for the new sample $s(n+1)$.

### 3.2.2.1. MDAC

A four-quadrant SC MDAC for the autocorrelator is shown schematically in figure 3.3. The MDAC is "parallel" rather than "serial" - multiplication occurs in one clock cycle for $B$ bits rather than $B$ cycles for $B$ bits. The ana$\log$ input $V_{i n}$ is connected to the analog sample-and-held voltage $s(n)$. The digital input word $s_{d}(n-k)$ in offset-binary format controls the switches $S_{1}$ through $S_{B}$. The MDAC is controlled by two non-overlapping clocks $\Phi_{1}$ and $\Phi_{2}$


Figure 3.3. Four-quadrant switched-capacitor MDAC
(i.e. $\Phi_{1} \cdot \Phi_{2}=0$, see figure 5.6.) During $\Phi_{1}$, the reset switch is closed and switch $S_{x}$ is connected to ground, so the feedback capacitor $C_{f b}$ and the offset capacitor $C_{x}$ discharge. The digital input word is presented, with switch $S_{j}$ turning on and connecting capacitor $C_{j}$ into the circuit if the $j^{\text {th }}$ bit $B_{j}$ is a logical ' 1 '. The input switch $S_{i n}$ connects $V_{i n}$ to one side of the selected capacitors; the other side of the capacitors is held at zero volts because the op amp inverting input is a virtual ground. So the selected capacitors charge to $V_{i n}$. On $\Phi_{2}$, the reset switch across $C_{f b}$ opens and switch $S_{\text {in }}$ connects the selected capacitors to ground, forcing the stored charge onto $C_{f b}$. Simultaneously, $C_{x}$ is connected to $V_{i n}$, forcing a charge $Q=C_{x} V_{i n}$ onto $C_{f b}$. The output voltage after the op amp settles is

$$
V_{\text {out }}=\frac{\sum_{j=1}^{R} B_{j} C_{j}-C_{x}}{C_{j b}} V_{\text {in }}
$$

which reduces to

$$
V_{\text {out }}=\frac{\sum_{j=1}^{B} B_{j} 2^{j}-2^{B}}{2^{B}} V_{\text {in }}=\left[\sum_{j=1}^{B} B_{j} 2^{j-B}-1\right] V_{\text {in }}
$$

for a binary weighted capacitor array. As can be seen from the above equation, capacitors $C_{1}$ through $C_{B}$ with $C_{f b}$ act as a variable gain amplifier, the gain being controlled by the digital word $s_{\alpha}(n-k)$. Capacitor $C_{x}$ is switched out-of-phase with the other capacitors, thereby providing the half-scale offset required for a four-quadrant MDAC.

### 3.2.2.2. FILTERS

Switched-capacitor filters are analog, sampled-data filters. For the autocorrelator, sampled-data filters are required as discussed in chapter 2. The z-domain transfer function for the filters was given in equation (2.11). Therefore, the filters can be implemented in SC technology once an appropriate
configuration has been found.
The filters required each have three real poles at $z=\alpha^{2}$ and a real zero at $z=\frac{k-1}{k+1} \alpha^{2}, 0 \leq k \leq p$. A SC filter which implements a real pole and real zero is shown in figure 3.4. The circuit is controlled by two non-overlapping clocks $\boldsymbol{\Phi}_{\mathbf{1}}$ and $\Phi_{2}$ (i.e. $\Phi_{1} \cdot \Phi_{2}=0$.) On $\Phi_{1}$, the switches are connected as shown in the figure. On $\Phi_{2}$, the switches are flipped to the other positions. Writing charge transfer equations at two consecutive sample times, $n$ and $n+1$, gives the timedomain relation

$$
\begin{equation*}
V_{\text {out }}(n+1)=\frac{C_{\rho b}}{C_{f b}+C_{r}} V_{\text {out }}(n)+\frac{C_{i}+C_{z}}{C_{\rho b}+C_{r}} V_{\text {in }}(n+1)-\frac{C_{z}}{C_{\rho b}+C_{r}} V_{\text {in }}(n) \tag{3.1}
\end{equation*}
$$

assuming that $V_{\text {out }}$ is sampled on $\Phi_{1}$ and that $V_{\text {in }}$ changes only on the rising edge of $\Phi_{1}$. Transformation of (3.1) into the $z$-domain gives


Fgure 3.4. Switched-capacitor filter, real pole and real zero

$$
\begin{equation*}
\frac{V_{o u t}(z)}{V_{t n}(z)}=-\frac{C_{z}+C_{i}}{C_{f b}+C_{T}} \frac{1-\frac{C_{z}}{C_{z}+C_{i}} z^{-1}}{1-\frac{C_{\rho b}}{C_{f b}+C_{T}} z^{-1}} \tag{3.2}
\end{equation*}
$$

Note that the pole location is $\frac{C_{\rho b}}{C_{f b}+C_{r}}$, the zero location is $\frac{C_{z}}{C_{z}+C_{i}}$, and the DC gain is $\frac{V_{\text {out }}(1)}{V_{\text {in }}(1)}=-\frac{C_{G}}{C_{r}}$. Since passive capacitor values are non-negative, the pole and zero locations for this configuration are in the interval $[0,1]$. Therefore, this filter can realize $H_{k}^{\prime}(z)$ for any $k>0$ (see table 2.1). The case $k=0$ requires a negative real zero which can be achieved by reversing the switch phasing of $C_{i}$. If the phasing of $C_{i}$ is reversed, the sign of the $C_{i}$ term in equation (3.2) is inverted:

$$
V_{\text {out }}(n+1)=\frac{C_{f b}}{C_{f b}+C_{T}} V_{\text {out }}(n)+\frac{-C_{i}+C_{z}}{C_{f b}+C_{T}} V_{i n}(n+1)-\frac{C_{z}}{C_{f b}+C_{T}} V_{i n}(n),
$$

or in the $z$-domain

$$
\begin{equation*}
\frac{V_{\text {out }}(z)}{V_{\text {tn }}(z)}=-\frac{C_{z}-C_{i}}{C_{f b}+C_{T}} \frac{1-\frac{C_{z}}{C_{z}-C_{i}} z^{-1}}{1-\frac{C_{f b}}{C_{f b}+C_{T}} 2^{-1}} \tag{3.3}
\end{equation*}
$$

The pole location is the same as the previous circuit. The difference is the zero location which is now $\frac{C_{z}}{C_{z}-C_{i}}$. The zero can be any real value excluding the interval $[0,1]$. So the two circuits, identical except for the switch phasing of $C_{i}$, offer zero locations over the entire real axis.

A circuit with a transfer function identical to equation (3.2) but with different switch timing than figure 3.4 is shown in figure 3.5. This circuit switches the feedback capacitor $C_{f b}$ out of the feedback loop rather than $C_{r}$. Likewise, $C_{z}$ is switched out of the circuit rather than $C_{i}$. On $\Phi_{1}$, the reset switch resets the op amp, $C_{i}$ is connected to ground, and $C_{f b}$ and $C_{z}$ are floating. $O n \Phi_{2}$, the reset switch is open, $C_{i}$ is connected to the input, and $C_{f b}$ and


Figure 3.5. Switched-capacitor filter, one pole and one zero, different switching scheme
$C_{z}$ are connected into the circuit. Again, notice that by simply inverting the phasing on the input switch for $C_{i}$, the input voltage $V_{\text {in }}(n+1)$ is introduced with a sign inversion. This changes the transfer function of the filter from (3.2) to (3.3).

Time multiplexing of the op amp of figure 3.5 for multiple filters is now possible since $C_{f b}$ and $C_{z}$ hold the state of the filter (figure 3.6). When $C_{f O_{j}}$ and $C_{x_{k}}$ are floating, a different pair of capacitors, $C_{\rho b_{k+1}}$ and $C_{x_{k+1}}$ may be switched into the circuit so that another filtering function can be performed. Each pair of capacitors, $C_{f b_{k}}$ and $C_{x_{k}}$ form one channel of the multiplexed filter section. There are ten channels per op amp to implement the ten filters required for the autocorrelator. Three multiplexed fllter sections must be cascaded to implement the 3 pole, one zero transfer functions required
( $H_{k}(z)$ of equation 2.11).
For the purpose of illustration, let $\Phi_{A}=\Phi_{B}=\Phi_{a}$ and $\operatorname{RESET}=\Phi_{1}$ in figure 3.6. The timing is as follows: during $\Phi_{1}$, the reset switch is closed and discharges $C_{r}$, all $C_{f b}$ and $C_{z}$ capacitors are floating. During $\Phi_{2}$, the reset switch is open, the input switch changes position, and one set of capacitors $C_{f b_{k}}$ and $C_{x_{k}}$ are connected into the circuit. $C_{i}$ and $C_{z}$ transfer charge onto $C_{\rho b}+C_{r}$. The filter transfer function is

$$
\frac{V_{\text {out }}(z)}{V_{\text {in }}(z)}=-\frac{C_{z_{k}}+C_{i}}{C_{f b_{k}}+C_{r}} \frac{1-\frac{C_{z_{k}}}{C_{z_{k}}+G_{k}} z^{-1}}{1-\frac{C_{f b_{k}}}{C_{f b_{k}}+C_{r}} z^{-1}}
$$

This clocking repeats, but on $\Phi_{2}, C_{z_{k+1}}$ and $C_{f b_{k+1}}$ are connected into the circuit. $C_{z_{k}}$ and $C_{f b_{k}}$ are now floating. If ten sets of capacitors are stacked on one


Fgure 3.6. Multiplexed version of figure 3.5

| Capacitor Ratios for SC Filters |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| lag | transfer <br> function | pole | zero | $\frac{C_{f b}}{C_{r}}$ | $\frac{C_{z}}{C_{i}}$ |  |
| $k=0$ | equation (3.3) | 0.9604 | -0.9604 | 24.25 | 0.4899 |  |
| $\mathbf{k}=1$ | equation (3.2) | 0.9604 | 0.0000 | 24.25 | 0.0000 |  |
| $\mathbf{k}=2$ | equation (3.2) | 0.9604 | 0.3201 | 24.25 | 0.4708 |  |
| $\mathbf{k}=3$ | equation (3.2) | 0.9604 | 0.4802 | 24.25 | 0.9238 |  |
| $\mathbf{k}=4$ | equation (3.2) | 0.9604 | 0.5762 | 24.25 | 1.3596 |  |
| $\mathbf{k}=5$ | equation (3.2) | 0.9604 | 0.6403 | 24.25 | 1.7801 |  |
| $\mathbf{k}=6$ | equation (3.2) | 0.9604 | 0.6860 | 24.25 | 2.1847 |  |
| $\mathbf{k}=7$ | equation (3.2) | 0.9604 | 0.7203 | 24.25 | 2.5753 |  |
| $\mathbf{k}=8$ | equation (3.2) | 0.9604 | 0.7470 | 24.25 | 2.9526 |  |
| $\mathbf{k}=9$ | equation (3.2) | 0.9604 | 0.7683 | 24.25 | 3.3159 |  |

Table 3.1. Capacitor ratios for implementing $H_{k}^{\prime}(z)$
op amp, one pole-zero pair for the ten filters $H_{k}{ }_{k}(z), 0 \leq k \leq 9$, have been realized. If the $C_{z}$ capacitors are eliminated, one pole for ten fllters is realized. The filters $H_{k}^{\prime}(z)$ can be efficiently constructed using one multiplexed polezero section followed by two multiplexed pole sections. As noted earlier, changing the switch phasing of $C_{i}$ during the $k=0$ time slot results in a sign reversal of the $C_{i}$ term in the transfer function. This is necessary to implement the negative real zero for filter $H_{0}^{\prime}(z)$.

The capacitor ratios for the filters $H_{k}(z)$ are listed in table 3.1. Since all channels of a multiplexed filter section share the same $C_{r}$ and $C_{i}$, all have the same DC gain which is $\frac{V_{\text {out }}}{V_{\text {in }}}(1)=-\frac{C_{i}}{C_{T}}$. As was noted in chapter 2 , the DC gain for the filters $H_{k}(z)$ is different for each $k$. Rather than have a different $C_{i}$
for each filter, the different DC gains are implemented by scaling in the microprocessor (see section 4.1.7).

### 3.3. DURBIN RECUREION MICROPROCEBSOR

The analog autocorrelation values output by the autocorrelator must be transformed into LPC coefficients or reflection coefficients by the Durbin recursion algorithm (see section 2.4). For a 9 pole LP.C model, the recursion involves 100 operations (multiplications or divisions) each frame. Accuracy considerations necessitate digital processing. Previous investigations have reported a need for 16 bit multiplies and 32 bit intermediate results in the recursion algorithm to minimize error due to finite word arithmetic [ 16 ],[15]. Given this, only 16 bit microprocessors with a multiply instruction were considered, and the Intel 8088 was chosen.

The microprocessor system is shown in figure 3.7. To digitize the analog autocorrelation values, an $A D C$ is included. The memory requirements of the Durbin algorithm are minimal and are easily handled by a 256 by 8 bit RAM. The program size was estimated to be less than $1 k$ bytes, so a $1 k$ byte EPROM was chosen. Speed, word length considerations, and the program will be discussed in the following chapter.

### 3.4. AN AUTOUATIC GAIN CONTROL CIRCUIT

Ideally, the input speech would generate an $R(0)$ (analog voltage) equal to the $A D C$ 's full scale input at every frame; this would minimize the error due to the quantization of the autocorrelation values. The magnitude of $R(0)$ has twice the dynmaic range of the speech because $R(0)$ is the short-time energy of the speech waveform which is proportional to the speech amplitude squared. The dynamic range of the input speech is typically 30 dB , resulting


Fgure 3.7. Block diagram of 8088 system
in a $60 d B$ range for $R(0)$. To minimize the dynamic range of $R(0)$, and thereby reduce errors due to quantization of the autocorrelation values, scaling of the input speech at each frame is necessary.

An automatic gain control circuit (AGC) for this purpose is shown in block diagram form, figure 3.8. The speech passes through two parallel paths. The upper path delays a frame of speech while the lower path computes an estimate of $\sqrt{R(0)}$ for the frame. Then, as the speech passes out of the delay line, it is scaled by $g \propto \frac{1}{\sqrt{R(0)}}$

The lower path estimates $\sqrt{R(0)}$ rather than compute it exactly. An exact computation might seem in order, but the IIR window used in the autocorrelator overlaps multiple frames and therefore exact computation is neither possible nor worthwhile. Furthermore, the square root operation is not easily realized. To simplify matters, $\sqrt{R(O)}$ is estimated using the absolute


Figure 3.8. Block diagram of automatic gain control circuit (AGC)
value function and filtering,

$$
V_{v}=\sum_{n=-\infty}^{\infty}|s(n)| w(n-j)=\sum_{n=-\infty}^{\infty}|s(n)| h(j-n) .
$$

where $w(n)$ is the same two pole window function as is used in the autocorrelation computation, equation (2.6), and $w(-n)=h(n)$ as in chapter 2. The use of the same window function should generate an estimate of $\sqrt{R}(0)$ which is fairly accurate since $R(0)$ and $V_{y}$ are based on the same weighted speech segment.
$V_{y}$ must be scaled to give an estimate of $\sqrt{R(0)}$. To find the scaling factor, we make use of statistical data on the amplitude distribution of speech. Speech has an amplitude distribution which is very closely approximated by the Laplacian distribution [17]

$$
p(s)=\frac{1}{\sqrt{2} \sigma_{s}} \exp \left(-\frac{\sqrt{2}|s|}{\sigma_{s}}\right)
$$

where $\sigma_{s}$ is the root mean square value of speech. If we take the expected value of $V_{v}$

$$
E\left(V_{y}\right)=\sum_{n=-\infty}^{\infty} E(|s(n)|) h(j-n)=E(|s(n)|) \sum_{n=-\infty}^{\infty} h(j-n)=E(|s(n)|) H(1)
$$

because $\sum_{n=-\infty}^{\infty} h(j-n)$ is the DC gain of the filter $H(z), H(1)$ (DC or 0 Hz corresponds to $z=1$ ). $E(|s(n)|)$ is found by integrating

$$
E(|s(n)|)=\int_{-\infty}^{\infty}|s| p(s) d s=\frac{\sigma_{s}}{\sqrt{2}}
$$

If the speech signal is assumed ergodic over a frame ( 12.5 msec ), then $\sqrt{R(0)} \approx_{\sigma_{s}}$, so $E\left(V_{y}\right) \approx \frac{\sqrt{R(0) H(1)}}{\sqrt{2}}$.

Not only should the AGC scale the speech in an attempt to give $R(0)$ equal to the ADC's full scale input, it should set the gain so as to minimize clipping at the ADC. Clipping of the speech generates errors in large amplitude samples which heavily contribute to the autocorrelation values. Under the Laplacian distribution assumption, speech has the property that the amplitude is greater than $4 \sigma_{3}$ only $0.35 \%$ of the time because

$$
\operatorname{Prob}\left[|s(n)|>4 \sigma_{s}\right]=1-\operatorname{Prob}\left[-4 \sigma_{s}<s(n)<4 \sigma_{s}\right]=1-\int_{-4 \sigma_{z}}^{4 \sigma_{s}} p(s) d s=0.0035
$$

So if the gain is set to $\frac{1}{g}=\frac{H(1)}{4 \sqrt{2} V_{y}} \approx \frac{1}{4 \sigma_{3}}$, the speech will be clipped about $0.35 \%$ of the time, so the error due to clipping will be negligible.

If the analyzed speech is to be reconstructed, the AGC gain should be stored and transmitted for use in the synthesizer. For such situations, an ADC is included to quantize the present scale factor $g$. Then, to handle the scaling of the speech, an MDAC is employed in the feedback loop of an op amp to
implement division. Only a small number of bits of resolution is required to give adequate performance in the AGC; five or six bits is sufficient [18]. A companding ADC with logarithmic transfer characteristic is preferred rather than a linear $A D C$. In any case, the AGC gain should be changed at the frame rate of 80 Hz .

A feedback AGC system, without the delay line, was considered for this application. This would greatly simplify the AGC and make an IC realization much easier and smaller in area. A feedback AGC uses the last frame's energy, $R(0)$, to estimate the scaling factor for the present frame. If the signal does not vary rapidly from frame to frame, this would work very well. Unfortunately, speech changes very rapidly from frame to frame. To illustrate this point. let us consider a segment of background noise proceeding the word 'peat'. The background noise fills frame 1 , and the $/ \mathrm{p} /$ sound begins at the start of frame 2 . The energy in the frame of background noise will be very low, so the feedback AGC will set the gain to be very large for frame 2. The result is excessive clipping of the /p/ sound as it is scaled by the AGC. This causes a large error in the computation of the autocorrelation values for frame 2, resulting in an incorrect LPC model or an unstable model. When synthesized, the $/ \mathrm{p} /$ sound cannot be distinguished from a/b/or /ee/, and the word 'peat' can not be distinguished from 'eat' or 'beat'. This is a common occurrence - plosives are transient in nature and are heavily clipped by a feedback AGC. Setting the gain for frame 2 based on the average energy in frame 2 eliminates this problem.

An AGC of the type described would be very useful as a speech preprocessor, whether the subsequent processing is analog or digital. The AGC reduces the bit requirement of the following $A D C$ and minimizes quantization
error at the ADC which might generate unacceptable errors in computation.

## CHAPTER 4

## DESTGN OF THE SYSTEM

In the last chapter, circuits were chosen for implementing the autocorrelator, the AGC, and the Durbin recursion algorithm; but many design details such as the number of bits in the MDAC and the op amp design were not considered. The design details fall into two groups. Decisions such as the number of bits in the MDAC and the quantization of the autocorrelation values are speech related. On the other hand, design of the op amp and the SC circuits is independent of the speech processing application; the SC circuits should be designed to give accurate voltage transfer and filter characteristics. Computer simulation was used extensively during the design phase. The op amp and other analog circuits were simulated on the circuit simulation program SPICE [ 19 ]. Speech related simulations were done by running sentences of digitized speech through specially written programs.

### 4.1. SPEFRCH REIATELD DESTGN

### 4.1.1. STMULATIONS

A high quality microphone (Shure model SM-10) and 12 bit ADC were used to digitize sentences spoken by a variety of speakers. The sentences and speakers are listed in appendix $C$ along with the source code for the speech simulation programs. The main program, Generateauto.c, simulates figure 3.1. This program takes speech as input and generates the autocorrelation values for each frame. It also features optional control of various aspects of the autocorrelator design such as AGC pre-processing, quantization of the

MDAC input, and quantization of the autocorrelation values.
After the speech is analyzed, it can be synthesized and played back by the program Speakpitch.c which is a direct-form LPC synthesizer (all computations in Speakpitch.c use floating-point arithmetic). For synthesis, the pitch periods are estimated by a Gold-Rabiner pitch detector [ 20 ]. Intelligibility is a subjective but important criterion which is applied to the synthesized speech to determine the quality of the analysis. Alternatively, the autocorrelation values can be compared to a reference set of autocorrelation values using the Itakura-Saito spectral distance measure, equation (2.15). The program spec_dev.c computes the spectral distance between two sets of autocorrelation values. This spectral distance measure, or spectral deviation from the reference, is extensively employed below to quantify the effect of quantization and other modifications to the LPC analysis discussed in chapter 2. Spectral deviation and the number of unstable frames are plotted versus design variables. This is an objective method of measuring errors. A spectral deviation of 3 dB is considered to be the acceptable limit. Unfortunately, spectral deviation is not directly related to perceived errors. Large spectral deviations at high frequencies are not as objectionable as the same amount of spectral deviation at lower frequencies (especially near the first resonance). Nonetheless, 3dB of spectral deviation is generally considered tolerable (slight perceptual error): 1 dB of spectral deviation is usually undetectable [21].[ 22 ].

Occasionally the LPC analysis results in an unstable fiter modeling the vocal tract due to errors in computation (e.g. quantization and truncation). The effect of an unstable frame on the quality of the synthesized speech is not easily determined. If an unstable frame is isolated (i.e. surrounded by long
spans of stable frames), it can be replaced by a stable LPC model either by repeating the last stable frame or by interpolating the reflection coefficients of the neighboring frames. If a string of consecutive unstable frames occurs, it is difficult to find a stable model to replace them, and the result is an audible discontinuity in the synthesized speech.

### 4.1.2. DOWNSAMPLING

Each filter $H_{k}^{\prime}(z)$ (equation (2.11)) is realized by cascading three first order low pass filter sections; each section has a cutoff frequency of 50 Hz . As such, the third low pass filter section is presented with an input signal with very little signal power above 50 Hz . This makes downsampling at the third filter section an attractive possibility. Downsampling reduces the computational workload in a digital approach and reduces capacitor ratios - and hence chip area - in a SC filter approach. This is a modification to the system which seems worthwhile.

A downsampling factor of ten was considered because it is convenient to implement. If the speech signal is spectrally flat. downsampling by a factor of ten would introduce aliases in the filter's passband ( $0 \mathrm{~Hz}-50 \mathrm{~Hz}$ ) that are 47 dB below the baseband signal.

The simultation program includes an option for downsampling in the third filter section. This was used to test the effect of downsampling by a factor of ten. The results are tabulated in table 4.1, row 1. The units of spectral deviation are millibels $(\mathrm{mB}), 1 \mathrm{mB}=0.01 \mathrm{~dB}$. Note that the errors contributed by downsampling are extremely small and are perceptually undetectable.

The downsampling by a factor of ten means the third filter section operates at a sampling rate of 800 Hz . To achieve the desired cutoff frequency of 50 Hz , the capacitor ratio $\frac{C_{f b}}{C_{T}}$ is only 2.04 . This is much smaller than the

| Spectral Deviation Results |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| test condition | mean <br> $(\mathrm{mB})$ | standard <br> deviation <br> $(\mathrm{mB})$ | number <br> of <br> unstable <br> frames | total <br> number <br> of <br> frames |
| downsampling by factor of <br> 10 at third filter section | 0 | 6 | 0 | 4239 |
| AGC pre-processing <br> AGC pre-processing and <br> truncation of R(k) to <br> nearest integer | 6 | 19 | 0 | 4239 |
| Truncation of R(k) to <br> nearest integer without <br> AGC pre-processing | 11 | 32 | 55 | 4239 |

Table 4.1. Spectral deviation results for various test conditions
ratio required for the first two filter sections which operate at an 8 kHz sampling rate - they have $\frac{C_{f b}}{C_{T}}=24.25$.

### 4.1.3. EFFFECT OF AGC ON STABILITY

An AGC is very important in this system - it relaxes the bit requirement of the MDAC and the ADCs. But an AGC can cause instability in the LPC model if the AGC changes its gain too often and/or too much, resulting in a time waveform which is difficult to model. The effect of the AGC was simulated, and the results are presented in table 4.1, row 2. Note that the AGC works very well because the spectral deviations are very small. The scaled speech (output of the AGC) was played back through loudspeakers and found to be extremely intelligible, only lacking the dynamic range of the original speech.

If the autocorrelation values are truncated to the nearest integer prior to the Durbin recursion algorithm, as is the case in this LPC system, the results are not as good (table 4.1, row 3). The larger spectral deviations and
the unstable frames are caused by quantization of the autocorrelation values. Such quantization is unavoidable because the autocorrelation values must be digitized for the microprocessor which handles the Durbin recursion algorithm. Still, the number of unstable frames is fairly small, only amounting to $1.2 \%$ of the frames analyzed. This should be contrasted with the results obtained without the AGC but including the integer truncation (table 4.1, row 4). Without the AGC, the large dynamic range of the speech results in a large dynamic range for $R(0)$. Small values of $R(0)$ result in heavy quantization of all the autocorrelation values and can cause large errors or instability in the LPC model. Figure 4.1 shows the distribution of $R(0)$ with and without AGC pre-processing. A comparison of the graphs clearly demonstrates that the AGC is beneficial.

### 4.1.4. MDAC BITS

The number of bits required in the MDAC should be minimized since for a SC MDAC the area of the capacitor array roughly doubles for each bit required. So, from an area standpoint, a minimum number of bits is desirable. Also, the RAM delay line size increases as the number of bits increases. Furthermore, the $A D C$ is simplified and conversion time is reduced as the number of bits in the MDAC decreases. A good AGC reduces the number of bits required by keeping the signal amplitude large.

The simulation program Generateauto.c provides optional control of the number of bits in the MDAC. Due to quantization of the speech onto the computer, the MDAC is simulated by a 12 bit by $B$ bit multiply where $1 \leq B \leq 12$. This is not the same as the MDAC which multiplies an analog voltage (ideally represented as a floating point quantity) and a finite length word. But quantization of both the multiplier and the multiplicand in the computer simulation



Figure 4.1. top: Distribution of $R(0)$ values with AGC pre-processing bottom: Distribution of $R(0)$ values without AGC pre-processing
does provide an upper limit on the error due to quantization in the MDAC.
Let's consider the problem of quantization in the computation of $R(k)=\sum_{n=-\infty}^{\infty} s(n) s(n-k) w(n) w(n-k)$. Since the delayed speech is quantized prior to multiplication in the MDAC, $s(n-k)$ should be replaced by $s_{d}(n-k)=s(n-k)+q(n-k)$ where $q(n-k)$ is the quantization error due to the $A D C$. For an $A D C$ which rounds the analog input to the nearest quantization level, $q(n)$ has a uniform probability distribution over the interval $-\frac{1}{2^{B}} \leq q \leqslant \frac{1}{2^{B}}$. If this quantized value is used in the autocorrelation computation, we get an approximation to $R(k)$ :

$$
\begin{aligned}
R_{a}(k) & =\sum_{n=-\infty}^{\infty} s(n) s_{d}(n-k) w(n) w(n-k) \\
& =\sum_{n=-\infty}^{\infty} s(n)[s(n-k)+q(n-k)] w(n) w(n-k) \\
& =\sum_{n=-\infty}^{\infty} s(n) s(n-k) w(n) w(n-k)+\sum_{n=-\infty}^{\infty} s(n) q(n-k) w(n) w(n-k) \\
& =R(k)+\sum_{n=-\infty}^{\infty} s(n) q(n-k) w(n) w(n-k)
\end{aligned}
$$

where $R_{a}(k)$ is the approximation to $R(k)$. The quantization error $q$ is a random variable with $E(q)=0$ and $\operatorname{Var}(q)=\frac{2^{-2 B}}{3}$ Furthermore, assuming the speech waveform traverses many quantization levels, $q(n)$ is independent of $q(m)$ for $m \neq n$ and $q$ is uncorrelated with $s$ [4]. If we assume a given speech waveform $\{s(n)\}$, then only $q$ is a random quantity. The random variable $R_{a}(k)$ has expected value

$$
\begin{aligned}
E\left[R_{a}(k)\right] & =E\left[R(k)+\sum_{n=-\infty}^{\infty} s(n) q(n-k) w(n) w(n-k)\right] \\
& =R(k)+E\left[\sum_{n=-\infty}^{\infty} s(n) q(n-k) w(n) w(n-k)\right]
\end{aligned}
$$

$$
\begin{aligned}
& =R(k)+\sum_{n=-\infty}^{\infty} s(n) E[q(n-k)] w(n) w(n-k) \\
& =R(k)
\end{aligned}
$$

so $R_{\mathrm{a}}(k)$ is unbiased, and variance

$$
\begin{aligned}
\operatorname{Var}\left[R_{a}(k)\right] & =\operatorname{Var}\left[R(k)+\sum_{n=-\infty}^{\infty} s(n) q(n-k) w(n) w(n-k)\right] \\
& =\operatorname{Var}\left[\sum_{n=-\infty}^{\infty} s(n) q(n-k) w(n) w(n-k)\right] \\
& =\sum_{n=-\infty}^{\infty} \operatorname{Var}[s(n) q(n-k) w(n) w(n-k)] \\
& =\sum_{n=-\infty}^{\infty} s^{2}(n) \operatorname{Var}[q(n-k)] w^{2}(n) w^{2}(n-k) \\
& =\operatorname{Var}[q(n-k)] \sum_{n=-\infty}^{\infty} s^{2}(n) w^{2}(n) w^{2}(n-k) \propto \operatorname{Var}(q) R(0) .
\end{aligned}
$$

The proportionality stems from the observation that the final summation looks just like the expression for $R(0)$ if $w(n)$ is replaced by $w(n) w(n-k)$ (see equation (2.6)). So the final summation expresses the computation of $R(0)$ when a different window, $w(n) w(n-k)$, is used. The standard deviation of $R_{a}(k)$ is

$$
\sigma_{R_{a}}=\sqrt{\operatorname{Var}\left(R_{a}\right)} \propto \sqrt{\operatorname{Var}(q) R(0)},
$$

and the ratio of the desired output, $R(0)$, to the standard deviation of the actual output., $\sigma_{R_{a}}$, is

$$
\frac{R(0)}{\sigma_{R_{\mathrm{a}}}} \propto \frac{R(0)}{\sqrt{\operatorname{Var}(q) R(0)}}=\frac{\sqrt{R(0)}}{\sqrt{\operatorname{Var}(q) .}}
$$

This ratio, which is similar to a signal-to-noise ratio, increases as $R(0)$ increases, so a large $R(0)$ is desirable. Scaling the input speech by using an AGC is one possible way to acinieve a consistently large $R(0)$. The ratio also increases if $\operatorname{Var}(q)=\frac{2^{-2 B}}{3}$ decreases, this occurs if the number of bits $B$ in the $A D C$ is increased.

| Spectral Deviation Results |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| MDAC bits | mean <br> $(\mathrm{mB})$ | standard <br> deviation <br> (mB) | number <br> of <br> unstable <br> frames | total <br> number <br> of <br> frames |
| 4 | 368 | 338 | 1302 | 4239 |
| 5 | 205 | 251 | 1105 | 4239 |
| 6 | 118 | 173 | 820 | 4239 |
| 7 | 65 | 126 | 383 | 4239 |
| 8 | 34 | 94 | 170 | 4239 |
| 9 | 14 | 59 | 41 | 4239 |
| 10 | 5 | 34 | 5 | 4239 |
| 11 | 2 | 24 | 0 | 4239 |
| 12 | 1 | 17 | 0 | 4239 |

Table 4.2 Spectral deviation results versus MDAC bits

Simulations with the number of MDAC bits as the independent variable were performed on all the sentences in the data base to determine the minimum number of bits acceptable. The results are tabulated in table 4.2 and graphed in figure 4.2. In the upper graph, the mean spectral deviation is plotted versus the number of MDAC bits with a solid black line; the mean plus three times the standard deviation of the spectral deviation data (mean $+3 \sigma$ ) is plotted on the same graph with a dashed line. By Tchebycheves inequality [23] at least $89 \%$ of all the data lies below the dashed line. As can be seen from the graphs of figure 4.2, 8 bits ( 7 bits + sign) is acceptable.

In the autocorrelator, the MDAC is followed by a low pass filter $H_{k}^{\prime}(z)$ with very narrow bandwidth. Therefore, ADC/MDAC non-linearities can be tolerated in moderation because they generate harmonic distortion at higher frequencies which will be attenuated by the flters.


Figure 4.2 top: Spectral deviation versus MDAC bits bottom: Unstable frames versus MDAC bits

| Spectral Deviation Results |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $R(k)$ quantization <br> (bits) | mean <br> $(\mathrm{mB})$ | standard <br> deviation <br> $(\mathrm{mB})$ | number <br> of <br> unstable <br> frames | total <br> number <br> of <br> frames |  |
| 6 | 57 | 95 | 479 | 4239 |  |
| 7 | 35 | 79 | 268 | 4239 |  |
| 8 | 18 | 57 | 147 | 4239 |  |
| 9 | 10 | 38 | 71 | 4239 |  |
| 10 | 5 | 27 | 16 | 4239 |  |
| 11 | 2 | 11 | 9 | 4239 |  |
| 12 | 1 | 6 | 6 | 4239 |  |
| 13 | 0 | 5 | 1 | 4239 |  |
| 14 | 0 | 1 | 0 | 4239 |  |
| 15 | 0 | 0 | 0 | 4239 |  |
| 16 | 0 | 0 | 0 | 4239 |  |

Table 4.3. Spectral deviation results versus $R(k)$ quantization

### 4.1.5. QUANTIZATION OF THE AUTOCORRTH ATION VALUES

Since the analog autocorrelation values must be quantized prior to the Durbin recursion algorithm, the effect of such quantization must be investigated. Quantization can lead to large spectral errors or even instability.

The simulation program Generateauto.c provides optional control of the quantization of the autocorrelation values. At each frame, the autocorrelation values are computed exactly using floating point arithmetic. Then, for quantization to B bits ( $\mathrm{B}-1$ bits $+\operatorname{sign}$ ), all $R(k)$ are scaled by the factor $\frac{2^{B-1}}{R(0)}$ and truncated to the nearest integer. This results in $R(0)=2^{B-1}$. Table 4.3 and figure 4.3 show the results of such quantization. Quantization to the 10 bit level is acceptable, the number of unstable frames rapidly increases below 10



Figure 4.3. top: Spectral deviation versus $R(k)$ quantization bottom: Unstable frames versus $R(k)$ quantization
bits.

### 4.1.6. DC GAIN OF FILTERS

Due to the filtering, the maximum signal amplitude at the output of each filter section is smaller than its maximum input signal amplitude. To maintain maximum output voltage and therefore the maximum $R(0)$ possible, each filter section has a DC gain larger than one. The gain was determined by running speech through the system. The main concern was to avoid clipping.

The filters are a cascade of first order sections. The one pole, one zero filter section was positioned first, followed by a one pole section which is in turn followed by the final one pole section which operates at the lower sampling rate. The selected gain values are $2.5,1.38$, and 1.3 respectively.

### 4.1.7. THE BOB8 MICROPROCESSOR AND DURBIN'S RECURSION

The Durbin recursion algorithm transforms the quantized autocorrelation values into LPC coefficients $a_{i}$ and reflection coefficients $k_{i}$. In a microprocessor implementation, the algorithm must be implemented with fixed point arithmetic. The two goals of the microprocessor system are real time computation while generating negligible modeling errors due to the integer arithmetic. The two requirements are conflicting in nature; increasing computational accuracy requires longer word lengths which means longer multiplication and division times. The design strategy was to first find word lengths at every step in the algorithm which produce negligible errors. Then this program was run on the microprocessor system to see if it was fast enough for real time analysis. Due to the availability of 8 bit and 18 bit manipulations with the 8088 instruction set, word lengths of $8,16,24$, and 32 bits were considered.

The program spec_dev.c was modifled to check the effect of finite length arithmetic in the Durbin algorithm. The flexibility of the $C$ programming language, which allows manipulation of bits by shifting and masking, was very helpful.

Durbin's recursive solution of equation (2.12) is listed below, and the number of bits assigned to each variable is lisied in Table 4.4. The real number 1.0 is scaled to $O N E=\mathbb{R}^{14}$ in the 8088 program. After reading a set of autocorrelation values $R(k), 0 \leq k \leq 9$, each $R(k)$ is shifted left until there is a ' 1 ' in bit 14 of $R(0)$, so that $2^{14} \leq R(0)<2^{15}$. Each $R(k)$ is treated as a 16 bit integer. Since $\left|k_{i}\right|<1$ for a stable model, $\left|k_{i}\right|<0 N E$ in the 8088 program, so $k_{i}$ is stored as a 16 bit number. The $a_{i}$ 's do not have a theoretical bound, as do the $k_{i}$, but they do have a practical bound for speech modeling; a practical bound of $\left|a_{i}\right|<8$ was determined experimentally. In the 8088 program, $\left|a_{i}\right|<8 \cdot O N E$ and therefore the largest $a_{i}$ will require 18 bits; so each $a_{i}$ is stored as a 24 bit word for convenience of manipulation. Also, it was found that the magnitude of the product $a_{i} R(m-i)$ never exceeds $2^{31}$ (32 bits) despite the fact that $a_{i}$ is an 18 bit integer and $R(m-i)$ is a 16 bit integer. Therefore the product can be stored as a 32 bit integer. Likewise, the product $k_{m} a_{m=i}^{m-1}$ never exceeds 32 bits. The 8088 program includes a subroutine for

| Word sizes for the Durbin algorithm |  |
| :--- | :---: |
| variable name | bit length |
|  |  |
| $R(k)$ | 16 |
| $m$ | 8 |
| $k_{m}$ | 18 |
| $a_{m}^{m}$ | 24 |
| $a l^{m-1} R(m-i)$ | 32 |
| $k_{m} a_{m-i}^{m}$ | 32 |
| $E_{m}$ | 16 |

Table 4.4. Word size at different points in the Durbin algorithm.
multiplying an 18 bit word ( $a_{i}$ ) by a 16 bit word. This multiplication time is reduced, on the average, by checking the top two bits of the 18 bit integer because if the top two bits are just a sign extension, a 16 bit by 16 bit multiplication will suffice.

The microprocessor also must modify the output of the SC filters before beginning the Durbin recursion. Each SC filter has an undesirable DC offset voltage which adds to the autocorrelation value. Also, the SC filters all have the same DC gain (see section 3.2.2.2). But the gains should be slightly different as can be seen in table 2.1. The 8088 program goes through an initialization phase during which the autocorrelator's input is zero. This allows the 8088 to sample the DC offisets of the filters and store them. Then the microprocessor begins execution of the main program. Each frame, a new set of autocorrelation values are read. For each autocorrelation value, the corresponding offset voltage is subtracted and the difference is scaled by the relative DC gain of table 2.1. The result is the autocorrelation value which is used in the Durbin recursion algorithm:

$$
\begin{aligned}
& \text { start: } \quad E_{0} \\
& \text { loop: } \quad=R(0) \\
& m=0 \\
& m+1 \\
& k_{m}=\frac{R(m)+\sum_{i=1}^{m-1} a_{i}^{m-1} R(m-i)}{E_{m-1}} \\
& a_{m}^{m}=k_{m} \\
& a_{i}^{m}=a_{l}^{m-1}-k_{m} a_{m-i}^{m-1} \quad 1 \leq i \leq m-1 \\
& E_{m}=\left(1-k_{m}^{2}\right) E_{m-1} \\
&\text { if(m}<p) g o \text { to loop; } \\
& \text { else stop; }
\end{aligned}
$$

| Spectral Deviation Results |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| MDAC bits | mean <br> $(\mathrm{mB})$ | standard <br> deviation <br> $(\mathrm{mB})$ | number <br> of <br> unstable <br> frames | total <br> number <br> of <br> frames |  |
| 4 | 28 | 60 | 246 | 4239 |  |
| 5 | 18 | 48 | 117 | 4239 |  |
| 6 | 15 | 43 | 79 | 4239 |  |
| 7 | 14 | 42 | 49 | 4239 |  |
| 8 | 13 | 41 | 52 | 4239 |  |
| 9 | 12 | 40 | 51 | 4239 |  |
| 10 | 12 | 37 | 62 | 4239 |  |
| 11 | 12 | 37 | 52 | 4239 |  |
| 12 | 13 | 38 | 51 | 4239 |  |

Table 4.5. Spectral deviation results versus MDAC bits with all modifications

The final version of the 8088 program required 120 bytes ( 960 bits) of RAM to store all the variables. A 256 by 8 RAM was chosen; this allows 136 bytes for the program stack which was more than necessary. The stack is only used to save a few registers temporarily during a subroutine call.

### 4.1.8. TOTAL ERRROR FROM ALI, MODIFICATIONS

As might be expected, inclusion of all the modifications discussed in sections 4.1.2 through 4.1.7 results in an error which is larger than the error due to any one modification alone but less than the sum of the individual errors. The results of downsampling, MDAC quantization, $R(k)$ truncation to the nearest integer, and AGC pre-processing all simultaneously in effect are tabulated in table 4.5 and graphed versus MDAC bits in figure 4.4. Using an 8 bit MDAC results in acceptable performance. Auditioning synthesized speech



Figure 4.4. top: Spectral deviation versus MDAC bits, final system bottom: Unstable frames versus MDAC bits, final system
confirmed this decision. If an 8 bit MDAC was used in the analysis, the synthesized speech was easily understood although occasional minor flaws could be detected.

### 4.2. ANALOG IC DESIIGN

To demonstrate the feasibility of the analog/digital hybrid approach, the SC circuits for the autocorrelator were integrated on a single CMOS chip. The digital circuits for the autocorrelator are simple ciruits (i.e. small RAM, control logic) and were not included on the chip. MOS was chosen because it accommodates SC circuitry and is compatible with digital circuitry: CMOS, rather than NMOS or PMOS, was chosen because it offers more flexibility as well as more gain per amplifier stage. The IC design was a two part job, one being MDAC and SC filter design to minimize parasitic related errors, the other the design of the op amp. One parasitic, MOSFET channel charge redistribution during turn-off, is not well understood and hence it is not modeled properly in circuit simulators such as SPICE [ 24 ]. So reliable computer simulation of these charge effects was not possible. Therefore, a breadboard version of the autocorrelator was built for experimentation. Op amp design was done exclusively on SPICE.

### 4.2.1. THE PROCESSS

For integration of the IC, a reliable metal-gate CMOS process was chosen A P-type substrate, 1000 angstrom gate oxide thickness, and 30 V oxide breakdown voltage are characteristics worth noting. The minimum drawn line width is $10 \mu \mathrm{~m}$ which results in $8 \mu \mathrm{~m}$ channel lengths after out-diffusion of the source and drain. The gate-to-drain and gate-to-source overlaps are 1 to 2 microns for the NMOSFET, but only 0.1 to 0.2 microns for the PMOSFET due to a self-
aligning $\mathrm{P}+$ implant. Capacitors are MOS capacitors (metal-oxide-N+). The threshold voltages are typically IV for the NMOSFET and -2V for the PMOSFET. Since the substrate is P-type, the NMOS transistors are used as switches; PMOS transistors must be placed in an N -well so they are inefficient from an area standpoint unless a number of switches can be grouped into one well. A more detailed description of the process can be found in appendix $D$ as well as in [14].

### 4.2.2. A SIMPLE MODEE FOR THE MOSFET

For analog circuit design, simple equations which model the MOSFET are useful. Equations for an N channel MOS transistor are given below, and all parameters are defined. The $P$ channel MOS transistor follows the same equations if the direction of positive drain current is changed. Typical values for the parameters are listed in table 4.6.

If the transistor is in the linear region of operation (i.e. if a continuous channel extends from drain to source), the MOSFET acts as a resistance of value

| Typical Values for MOSFET Model Parameters |  |  |  |
| :--- | :--- | :--- | :--- |
| Parameter | SPICE Symbol | NMOS | PMOS |
| $V_{\text {eh }}$ | VTO | 1.0 V | -2.0 V |
| $\mathbf{k}$ | KP | $24 \frac{\mu A}{\nu^{2}}$ | $7 \frac{\mu A}{V^{R}}$ |
| $\lambda$ | LAMBDA | $0.01 V^{-1}$ | $0.005 \mathrm{~V}^{-1}$ |
| $N_{S J B}$ | NSUB | $1.6 \times 10^{15}$ | $1.0 \times 10^{18}$ |
| $t_{0 x}$ | TOX | $0.1 \mu$ | $0.1 \mu$ |

Table 4.6. Model parameters for SPICE simulations

$$
\begin{equation*}
R_{0 n}=\frac{1}{k \frac{W}{L}\left(V_{g 3}-V_{t h}-\frac{V_{d g}}{2}\right)} \approx \frac{1}{k \frac{W}{L}\left(V_{g 3}-V_{t h}\right)} \tag{4.1}
\end{equation*}
$$

The approximation is valid if $V_{g a}-V_{\text {th }} \gg \frac{V_{\text {da }}}{2}$ The parameters are

$$
\begin{aligned}
k & =\mu C_{o x}^{\prime}, \\
\mu & =\text { the mobility of the channel charge, } \\
C_{o x} & =\text { the gate to channel capacitance per unit area, } \\
W & =\text { the width of the active area. } \\
L & =\text { the length of the active area, } \\
V_{g s} & =\text { the gate to source voltage, } \\
V_{d s} & =\text { the drain to source voltage, } \\
V_{t h} & =\text { the threshold voltage of the transistor. }
\end{aligned}
$$

The transistor is in the linear region if both $V_{g s}>V_{t h}$ and $V_{g d}>V_{t h}$. If $V_{g s}>V_{t h}$ but $V_{g t}<V_{t h}$, then the transistor is in the saturation region (i.e: the channel is pinched off at the drain), and the transistor follows the relation

$$
I_{d s}=\frac{k W}{2 L}\left(V_{g \pi}-V_{t h}\right)^{2}\left(1+\lambda V_{d s}\right)
$$

where
$I_{\text {de }}=$ the drain to source current,
$\lambda^{-1}=$ the Early voltage of the transistor.
The threshold voltage $V_{c h}$ is dependent on the source to substrate voltage

$$
V_{t h}=V_{t h 0}+\gamma\left[\sqrt{\left|V_{b s}\right|+2\left|\varphi_{f}\right|}-\sqrt{2\left|\varphi_{f}\right|}\right]
$$

where

$$
\begin{aligned}
V_{t n 0} & =\text { the threshold voltage measured with } V_{b s}=0 . \\
\gamma & =\text { the body effect parameter }, \\
V_{b z} & =\text { the substrate to source voltage, } \\
\varphi_{f} & =\text { the Fermi level of the substrate. }
\end{aligned}
$$

The capacitances associated with the MOSFET are shown in figure 4.5. The $\mathrm{N}+$ source and drain diffusions in the P substrate form diode junctions which are always reverse-biased and have an associated non-linear junction capacitance. The gate metal overlaps the source and drain diffusions slightly, giving rise to overlap capacitances $C_{o v}$. These overlap capacitances provide an undesirable coupling between the gate and source and between the gate and drain when the transistor is off. The total gate to source, gate to drain, and gate to substrate capacitances are complicated functions of the terminal voltages [ 25 ].

### 4.2.3. OPERATIONAL AMPLIFIER

Since all circuits employing the op amp are SC circuits, the op amp loading is capacitive. A simple transconductance amplifier which uses the capaci-


B
Figure 4.5. Capacitances associated with a MOSFET
tive load for compensation was designed. Important design goals are settling to $0.1 \%$ in $3 \mu$ seconds, open loop gain greater than 1000, large output swing and low noise. Low power dissipation and small area are desirable but not crucial due to the multiplexing of each op amp.

The op amp schematic is shown in figure 4.6. Current source M14 biases the input differential pair M1-M2. Wilson current mirrors M3-M4-M5 and M6-M7-M8 provide current gain as well as high output impedance. The drain current of M4 is mirrored to the output by cascode current mirror M9-M10-M11-M12. The op amp has a differential mode transconductance of $G_{m}$

$$
G_{m}=\frac{1}{2^{2}} g_{m_{4 n}}\left[\frac{\frac{W_{0}}{L_{8}}}{\frac{W_{6}}{L_{6}}}\right]+\frac{1}{2^{2}} g_{m_{m}}\left[\frac{\frac{W_{5}}{L_{5}}}{\frac{W_{3}}{L_{9}}}\right]\left[\frac{\frac{W_{11}}{L_{11}}}{\frac{W_{10}}{L_{10}}}\right] ;
$$

$g_{m_{\text {en }}}=g_{m_{1}}=g_{m_{2}}$ is the transconductance of the input transistors M1 and M2. If the $\frac{W}{L}$ ratios are as shown in figure 4.6, $G_{m}$ reduces to

$$
G_{m}=g_{m_{4 n}}\left[\frac{\frac{W_{\mathrm{g}}}{L_{\mathrm{g}}}}{\frac{W_{8}}{L_{\mathrm{g}}}}\right]=g_{m_{4 n}}\left[\frac{\frac{W_{5}}{L_{5}}}{\frac{W_{\mathrm{s}}}{L_{\mathrm{s}}}}\right]=g_{m_{4 n}} A_{I} \propto \sqrt{I_{\text {bias }}}
$$

$A_{I}$ is the current gain of the Wilson mirrors M3-M4-M5 and M6-M7-M8, $A_{I}=2.5$ in figure 4.8. The differential mode voitage gain is just $A_{\nu}=G_{m} R_{\text {out }}$ where $R_{\text {out }}$ is the output impedance of the Wilson mirror M6-M7-M8 in parallel with the output impedance of the cascode mirror M9-M10-M11-M12.

$$
R_{\text {out }}(\text { Wilson }) \approx r_{07}\left(g_{m \theta} r_{0 \theta}\right)=\frac{\sqrt{16 \mu C_{o z}^{\prime} \frac{W_{0}}{L_{\theta}}}}{\lambda_{7} \lambda_{\theta} A_{f} I_{\text {oicas }}^{\frac{2}{2}}}
$$



Figure 4.6. CMOS op amp schematic ( $\frac{W}{L}$ ratios next to transistors)

$$
R_{\text {out }}(\text { Cascode }) \approx r_{012}\left(g_{m 12} r_{011}\right)=\frac{\sqrt{16 \mu C_{0 x}^{\prime} \frac{W_{12}}{L_{12}}}}{\lambda_{12} \lambda_{11}\left(A_{I} I_{b i a s}\right)^{\frac{3}{2}}}
$$

so

$$
R_{\text {out }}=R_{\text {out }}(\text { Wilson })| | R_{\text {out }}(\text { Cascode }) \times I_{\text {oice }}^{-\frac{9}{2}}
$$

giving

$$
A_{\nu}=G_{m} R_{\text {out }} \propto \sqrt{I_{\text {bias }} I_{\text {bias }}}-\frac{a^{2}}{2}=\frac{1}{I_{\text {otias }}}
$$

So the low frequency voltage gain is inversely proportional to bias current. But reducing the current to achieve higher gain reduces bandwidth and increases the noise [ 26 ].

Since the CMOS process uses a P-type substrate, the PMOS transistors sit in an N -well and therefore have a higher output resistance than the NMOS transistors. So the PMOS transistors were chosen for the simple current source for biasing the input stage. The input transistors M1 and M2 are large area devices to minimize the op amp's noise [26].

The op amp is employed in a shunt-shunt feedback configuration with its non-inverting input grounded. In such a configuration, the common mode input signal is very small so a large common mode rejection ratio is not required. Nonetheless, the symmetry of the op amp should provide a very large common mode rejection.

### 4.2.4. SPEEED AND COMPENSATION

The op amp is basically a one stage design. As such, it should provide a wide bandwidth. All nodes internal to the op amp have an low frequency impedance of $\frac{2}{g_{m}}$ the highest impedance node is the output node. $G_{m}$ has two non-dominant poles due to the total capacitance at the drains of the
input transistors M1-M2 interacting with the equivalent resistance looking into the Wilson mirrors

$$
p_{n d}=-\frac{g_{m}}{2 C_{t}}=-\frac{g_{m}}{2\left(C_{o v}+C_{j}\right)}
$$

( $C_{o v}$ is the gate overlap capacitance, $C_{j}$ is the junction capacitance associated with the source and drain diffusions). The dominant pole is at the output node due to the large output resistance $R_{\text {out }}$ interacting with the feedback and load capacitors.

Compensation is only meaningful in the context of feedback circuits. In the SC autocorrelator, the op amp is subjected to numerous feedback configurations. In all cases, the feedback is shunt-shunt (i.e. voltage output, current input).

Stability and settling time can be determined from the phase margin of the loop gain [27]. The loop gain of the shunt-shunt feedback circuit figure 4.7 is

$$
\begin{equation*}
T(s)=\frac{\left(G_{m}-y_{f}\right) y_{f}}{\left(y_{i}+y_{f}\right)\left(y_{0}+y_{f}\right)} \tag{4.2}
\end{equation*}
$$

where the reverse transmission through the op amp has been neglected - it is assumed to be much smaller than $\left|y_{f}\right|$ at all frequencies of interest (appendix E). All terms of (4.2) are functions of the complex frequency $s$. The loop gain $T(s)$ can be simulated directly on SPICE using the configuration of figure 4.8. The op amp with feedback element $y_{f}$ across it has a voltage gain

$$
\frac{V_{0}}{V_{x}}=-\frac{\left(G_{m}-y_{f}\right)}{\left(y_{0}+y_{f}\right)}
$$

The voltage divider has the transfer function

$$
\frac{V_{T}}{V_{0}}=\frac{y_{f}}{\left(y_{i}+y_{f}\right)}
$$

The cascaded gain is the loop gain


Figure 4.7. Shunt-shunt feedback circuit


Figure 4.6. Circuit for simulating loop gain

$$
T(s)=-\frac{V_{r}}{V_{x}}=\frac{V_{0} V_{r} \quad\left(G_{m}-y_{f}\right) y_{f}}{V_{z} V_{0}\left(y_{i}+y_{f}\right)\left(y_{0}+y_{f}\right)}
$$

This provides a very simple means of simulating the loop gain directly. This is important in circuits which have frequency dependent feedback such as those in the autocorrelator. Exact simulation of loop gain is discussed further in appendix E .

Once an acceptable phase margin was found using figure 4.8, the step response of the feedback circuit was simulated. The worst case for stability occurs in the reset configuration. Settling times for MDAC and multiplexed filters are tabulated in table 4.7. The SPICE model parameters which were used are listed in table 4.6. These are conservative model parameters based on data from previous experiments [ 28 ].

| Settling Time Simulation Results |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Circuit Simulated (figure) | Switch <br> Phasing | $C_{r}$ or $C_{1}$ | Load Capacitance | Settling Time to $0.1 \%$ |
| MDAC <br> (fig 3.3) | reset switch on | $C_{1}=0.1 p F$ | OpF | $2.2 \mu \mathrm{sec}$ |
| MDAC <br> (ig 3.3) | reset switch off | $C_{1}=0.1 p F$ | OpF | $1.3 \mu \mathrm{sec}$ |
| Multiplexed filter (fig 3.6) | reset on | $C_{r}=0.22 p F$ | 10 pF | $1.2 \mu \mathrm{sec}$ |
| Multiplexed filter (fig 3.6) | reset off | $C_{r}=0.22 p F$ | 10pF | $1.9 \mu \mathrm{sec}$ |

Table 4.7. Settling time results from SPICE for different configurations

### 4.2.5. EFFTECT OF PARASTITCS ON MDAC AND SC FILTERS

To implement the SC circuits of chapter 3 , an N channel MOSFET is used wherever a switch is needed. But the MOSFET is not an ideal switch. Aside from finite on-resistance and gate capacitance, the gate overlap capacitance and channel charge introduce error charge in the signal path of the SC circuits. In some conflgurations, this error charge is signal dependent which causes distortion. These non-idealities must be considered and their effects minimized during the design phase.

In SC circuits, the finite on-resistance of the MOSFETs slows the charging of the capacitors. For a capacitance $C$ and MOSFET on-resistance $R_{o n}$, the associated time constant is $\tau=R_{0 n} C$. To charge the capacitance to within $0.1 \%$ of its final value requires seven time constants (7 7 ). Charging time does not present a problem in this system because the largest time constants are a few hundred microseconds, so $7 \tau<1 \mu \mathrm{sec}$ which is much less than the smallest time allowed for charging (which is $4 \mu \mathrm{sec}$ ). If the charging time were a problem, the time constant could be reduced by decreasing $C$ or by decreasing $R_{o n}$. The on-resistance can be decreased by increasing gate drive voltage ( $V_{g=}-V_{l k}$ ) or increasing the transistor's $\frac{W}{L}$ (see equation (4.1)).

For the SC MDAC of figure 4.9, the input switches $S_{1}$ through $S_{B}$ and $S_{\text {in }}$ can be considered to be ideal switches. This can be understood by noting that the MDAC operates by transferring charge from the input capacitor array $C_{1}$ through $C_{B}$ onto $C_{f b}$ on $\Phi_{2}$. The Gaussian surface, shown as the dotted line in Agure 4.9, represents the charge transfer region. As long as the reset switch is open, the charge inside the surface must remain constant. Since the switches $S_{1}$ through $S_{B}$ are outside this surface, they do not contribute to the charge transferred and therefore have no effect on the output voltage. The


Figure 4.9. SC MDAC
only error charge is contributed by the reset switch which provides DC stability and therefore breaks the Gaussian surface. As the reset switch turns off, some fraction of its channel charge will be trapped on the inverting node. Also, the reset clock is coupled to the inverting node through the gate overlap capacitance $C_{o v}$. The output voltage due to these sources can be approximated as

$$
V_{o u t} \propto \frac{C_{o v}}{C_{f b}} \Delta V_{c l}+\frac{r Q_{\text {channal }}}{C_{f b}}
$$

where $\Delta V_{c l}$ is the amplitude swing of the clock signal, $Q_{\text {channel }}=C_{0 z} W L\left(V_{g z}-V_{\text {eh }}\right)$ is the charge accumulated in the channel when the transistor is in the linear region, and $0 \leq r \leq 1$ is the fraction of channel charge dumped onto the inverting node when the transistor turns ofl. Fortunately, prior to each multiplication the MDAC is in the reset mode. So the feedthrough causes a constant DC offset voltage at the MDAC output. The
clocking scheme results in the op amp's offset voltage ( $V_{\text {offast }}$ ) being sampled onto the input capacitor array each reset period. So the op amp's offiset voltage is not multiplied by the variable gain of the MDAC, but it does appear directly at output. The total DC output voltage is

$$
\begin{equation*}
V_{o u f_{d c}} \approx V_{o f f=0 t}+\frac{C_{o v}}{C_{f b}} \Delta V_{c l}+\frac{r Q_{c h a r n o l}}{C_{f b}} . \tag{4.3}
\end{equation*}
$$

This offset passes through the SC filters and is subtracted digitally in the microprocessor as discussed in section 4.1.7.

Finite op amp gain results in a gain error in the MDAC. This gain error occurs for all products and therefore scales all autocorrelation values by the same factor. Since the LPC model is not changed by a uniform scaling of all autocorrelation values (see section 2.4), gain error is of no consequence in this application

The diode junction composed of a capacitor's $\mathrm{N}+$ diffusion and the P - substrate is always reverse biased, so it has an associated non-linear capacitance and reverse-bias leakage current. For the binary capacitor array, the N+ diffusions of the capacitors are connected to the input switches $S_{1}$ through $S_{B}$. This eliminates problems due to the non-linear capacitances because they are driven by the input source. For $C_{f b}$, the diffusion is connected to the output of the op amp. The non-linear junction capacitance associated with Cfo does present a non-linear capacitive load to the op amp which helps to compensate the op amp.

When all the switches $S_{1}$ through $S_{B}$ are on, the leakage currents for the diode junctions of $C_{1}$ through $C_{B}$ are supplied by the source driving $V_{\text {en }}$, and the leakage current for the diode on the output of the op amp comes from the output stage of the op amp; therefore the leakage currents have no effect. (Actually, the leakage current flowing through the MOSFET switch
drops a negligible voltage $I_{\text {loak }} R_{\text {on }}$.) The leakage current associated with a junction does present a source of error if any of the switches $S_{1}$ through $S_{B}$ is open. If input switch $S_{j}$ is open, a leakage current due to $C_{j}$ 's backplate diode flows through it and onto $C_{f b}$. This leakage dominates the small leakage current associated with the drain diffusion of the MOSFET switch $S_{j}$. The maximum error due to leakage currents occurs when all switches $S_{1}$ through $S_{B}$ are off (i.e. all bits in the digital word are ' 0 '). Then the error is roughly

$$
\Delta V_{\text {out }}=\frac{\sum I_{\text {leak }} \Delta t}{C_{f b}} \approx \frac{2 J_{\text {leat }} \Delta t}{C_{\text {ox }}^{\prime}}
$$

which equals $36 \mu$ Volts in the worst-case ( $\Delta t=12.5 \mu$ seconds and $J_{\text {leak }}=100 \frac{n A}{\mathrm{~cm}^{2}}$ ). This error is negligible for an 8 bit MDAC with a 5 Volt full scale output.

As was mentioned above, the op amp's offset voltage is sampled on the input capacitors during the reset phase and therefore the offset voltage is not multiplied by the MDAC gain. Since the $\frac{1}{f}$ noise of the op amp is a low frequency noise which can be viewed as a slowly varying offset voltage, the $\frac{1}{f}$ noise also appears directly at the output of the MDAC and is not multiplied by the MDAC's gain.

### 4.2.6. FILTERS

The filters suffer from many of the same errors as the MDAC. Unique to the SC filters are the multiplexed capacitors $C_{z}$ and $C_{f b}$. To investigate different switching schemes, MOSFETs are included on both sides of each capacitor (see figure 3.6) [ 29 ]. The multiplexing could be accomplished with output side switches only, but this would introduce undesirable signaldependent error as can be seen from the following: Assume only the output
side switches are used (all switches connected to the op amp's inverting input are shorted). The MOSFET output switch turns off when $V_{g R}-V_{t h}=0$. Since $V_{g s}=V_{c l}-V_{o u t}$, the charge transferred onto $C_{f b}$ due to $C_{o v}$ would be $Q=C_{o v}\left(\Delta V_{c l}-V_{o u t}-V_{t h}\right)$ and the charge transferred onto $C_{f b}$ from the channel of the MOSFET switch is

$$
Q=r Q_{\text {channat }}=r C_{o x} W L\left(V_{g s}-V_{t h}\right)=r C_{o x}^{\prime} W L\left(V_{c l_{H J}}-V_{o u t}-V_{t h}\right)
$$

where $0 \leq r \leq 1$ is the fraction of channel charge dumped onto $C_{f b}$ when the transistor turns off. $r$ is a function of clock rise/fall times and loading on the source and drain of the transistor. If the loading at the source and drain is identical, $r \approx \frac{1}{2}$ Note that these charge quantities are dependent on $V_{\text {out }}$, so the errors are signal dependent and cause distortion. To eliminate such signal dependent charge transfers, a MOSFET switch is also included on the input side of each multiplexed capacitor. The input side switch is turned off before the output side switch is turned off. Since the input side switch is connected to the inverting input of the op amp which is a virtual ground, the charge transferred onto $C_{f b}$ when an input side switch turns off is $Q=C_{o v}\left(\Delta V_{c l}-V_{d h}\right)+r Q_{c h a n n e l}$. This error charge is dependent on $V_{o u t}$ only through $r$ since the loading on the output side of the switch is dependent on $V_{\text {out }}$.

Switching only on the input side is not possible due to bootstrapping. To illustrate this problem, let's consider the case of $\pm 7.5 \mathrm{~V}$ clocks and $V_{\text {th }}=1 \mathrm{~V}$. Then, if $C_{f b_{k}}$ is floating and has -5 V stored on it and the output during time slot $k+1$ is -5 V , the input side of $C_{f b_{k}}$ would be at -10 V . If MOSFET $S_{k}$ has its gate at $-7.5 \mathrm{~V}, S_{k}$ will turning on thereby connecting $C_{f b_{k}}$ into the circuit in parallel with $C_{f b_{k+1}}$. This alters the charge on both $C_{f b_{k}}$ and $C_{f b_{k+1}}$ and ruins the multiplexing. This bootstrapping problem could be eliminated by reducing
the output signal swing or by increasing the clock amplitude or by adding the output side switches. Reducing the output swing reduces the dynamic range of the filters. Increasing the clock amplitude increases the amplitude of clock related errors and may not be possible if clocks are generated on chip. So the output switches eliminate bootstrapping problems and also reduce the capacitive loading on the output of the op amp.

To minimize the signal dependent errors, the following switching sequence is recommended for the multiplexed filters: 1) reset switch on, all other switches off, 2) reset off. 3) input side switch for channel $k$ on, all other switches off, 4) output side switch for channel $k$ on, input side switch still on, all others off. 5) input side switch turns off, output side switch still on, all others off, 6) output side switch turns off, all other switches off. Repeat cycle for channel $k+1$.

By discharging $C_{r}$ at the start of each time slot, channel to channel crosstalk through $C_{T}$ is eliminated. By connecting the capacitor's N+ diffusion on the output side of the op amp. problems due to non-linear junction capacitance and junction leakage current are avoided. The non-linear capacitance is driven by the output of the op amp. The junction leakage current flowing when the output side switch is on is supplied by the op amp output stage. When the multiplexed capacitors is out of the circuit, the leakage current will still flow. But it does not effect the filter at all. This can be seen by considering the Gaussian surface of figure 4.10. The analysis is simplified if the switches and op amp are assumed ideal, so we shall do so. We will look at one channel, channel $k$. In figure 4.10, if we start with $V_{t n}=0 \mathrm{~V}$ and $V_{\text {out }}=0 \mathrm{~V}$, the reset switch open, and the other switches on, each of the capacitors in the Gaussian surface have zero charge on them. The total charge


Figure 4.10. One channel of multiplexed filter showing junction leakage current
inside the Gaussian surface must remain constant since there is no current flowing into or out of this node. This total charge $Q_{t}$ is initially zero. Then the switches are turned off. While channel k's switches are open, the other channels are connected into the circuit. When the switches for channel $\mathbf{k}$ are once again turned on, we have $V_{i n}=0$ and the op amp's inverting input is a virtual ground, so the charge on $C_{8}$ is zero and the charge on the op amp's input capacitance is zero. So the charge on $C_{f b}$ and $C_{r},\left(C_{f b}+C_{r}\right) V_{o u f,}$ must equal zero because the total charge $Q_{i}$ must remain constant. Therefore $V_{\text {out }}=0 \mathrm{~V}$ so the leakage current had no effect whatsoever. (The reset switch does break the Gaussian surface and therefore does inject charge into the surface. This causes a DC offset voltage but does not invalidate the above argument.)

During the reset period, the DC offset voltage of the multiplexed filter section is equal to the offset voltage of the op amp. Otherwise, the DC output
voltage depends on the time slot. To find the the DC output voltage, we will consider the op amp and all switches except the reset switch to be ideal. Given this assumption, the DC output voltage can be found by writing charge transfer equations for a given time slot. For time slot $k$ and sample $\pi+1$.

$$
\left(C_{f b_{k}}+C_{r_{k}}\right) V_{\text {out }}(n+1)=C_{f b_{k}} V_{\text {out }}(n)+r Q_{\text {chansel }}+C_{o v} \Delta V_{c l} .
$$

To find the DC output voltage, we take the limit as $n$ goes to infinity. This gives

$$
\left(C_{f b_{k}}+C_{r_{k}}\right) V_{\text {out }}(\infty)=C_{f b_{k}} V_{\text {ous }}(\infty)+r Q_{\text {chanral }}+C_{o v} \Delta V_{c t}
$$

which reduces to

$$
\begin{equation*}
V_{\text {ous } D C}=V_{\text {out }}(\infty)=\frac{C_{\text {ov }}}{C_{r}} \Delta V_{c l}+\frac{r Q_{\text {chennsel }}}{C_{r}} . \tag{4.4}
\end{equation*}
$$

The interesting result is that the DC output voltage depends only on the loss capacitor $C_{r}$ and not on $C_{f o}$. This makes sense because, for a given filter, $C_{f o}$ is always connected into the circuit and acts like an open circuit for DC signals.

The finite gain of the op amp causes a slight reduction of the magnitude of the filter's pole location. If the op amp gain is infinite, the pole is $z=\frac{C_{f b}}{C_{f b}+C_{r}}$. If the op amp has an open loop voltage gain of $a$, the pole moves to

$$
\frac{C_{f b}}{C_{f b}+C_{T}} \frac{1+\frac{1}{a}}{\left.1+\frac{1}{a} \left\lvert\, \frac{C_{Q}}{C_{f b}+C_{T}}\right.\right]}
$$

For $a>1000$, the shift in the pole location is negligible.
The op amp's $\frac{1}{f}$ noise and op amp's oflset voitage are sampled onto $C$ during the reset period. Then, when the reset switch opens, $G$ retains the sampled $\frac{1}{f}$ noise and offiset voltage. Since the $\frac{1}{f}$ noise changes very slowly
and the offset voltage is constant, both are effectively canceled. The autocorrelator's output noise is dominated by the third filter section due to the low sampling rate.

### 4.3. IC IAYOUT

The layout was made as compact as possible while maintaining isolation between analog signal paths and clock signals wherever necessary. The op amp layout is shown in figure 4.11. The input transistors are the large polygons. Ideally, the input transistors would be circular. This assures good matching independent of mask alignment errors in either the X or Y direction. The polygons are an approximation to a circle; we could not make circles with our mask making equipment. The op amp occupies $450 \mathrm{mil}{ }^{2}$ of area.

To minimize the area of the layout, the switches in the SC circuits were realized with NMOS transistors. The layout of an NMOS transistor can be seen in the op amp layout. The gate metal was extended on both sides of the active area to minimize any leakage currents between the source and drain (this is important when the NMOS transistor is used as a switch). To be safe, $\mathrm{P}+$ isolation diffusions are placed between any two $\mathrm{N}+$ diffusions which are not connected. This costs area but was strongly recommended by former users of this CMOS process [ 28 ].

Values for the capacitors on the chip were chosen as small as possible to minimize total chip area. But small capacitors make parasitic charge transfer errors more noticeable (see section 4.2.5). For the MDAC, $C_{1}=0.1 p F$ was chosen. For the multiplexed filters, $C_{r}=0.22 p F$ for section 1 and 2 and $C_{r}=0.66 p F$ for section 3. The third filter section operates at a lower clock rate than the other two sections ( 800 Hz rather than 8 kHz ) and therefore requires smaller capacitor ratios to achieve the desired low frequency cutoff.


Figure 4.11. Op amp layout

To allow for experimentation with different clocking schemes, all the gates of the multiplexed filter switches must be controllable from off chip. This would amount to 80 control lines if all switch gates were brought out separately. By using a multiplexer of PMOS switches, the number of pins is reduced. A plot of the IC layout is shown in figure 4.12. The four opamps can been seen lined up in a column down the center of the chip. The top op amp is for the third multiplexed SC filter section. The capacitors for the third filter section are in the upper right. The second op amp is for the MDAC; its binary capacitor array is in the upper left. The third op amp is for the first SC filter section - the section which implements a pole and a zero for each channel. The feedback and zero capacitors for section one can be seen to the right of the third op amp. The bottom op amp is for the second SC filter section Its capacitors are in the lower left. Note the difference in size between the feedback capacitors of sections three and two. The difference is due to the lower sampling rate used in the third filter section. The chip dimensions are 148 mil by 133 mil , the area is $19,700 \mathrm{mil}^{2}$.

### 4.4. THE AUTOMATIC GAIN CONTROL

The AGC is a crucial element of this system. The AGC used was a breadboard circuit consisting of commercially available parts. The breadboard will be described and circuits for an IC implementation are given.

### 4.4.1. AGC BREADBOARD

For the breadboard, a Reticon SAD512 256 stage bucket-brigade device (BBD) delay line was used. The delay line should hold one frame of speech which is 100 samples for this system. By operating the BBD at a 16 kHz sampling rate, the number of samples held is 128 which is as close to the desired


Figure 4.12 Layout of the autocorrelator IC
value as is practically possible with the available BBDs. Since the speech was bandlimited to 4 kHz prior to the AGC, the signal out of the BBD has no significant signal in the 4 kHz to 8 kHz region and therefore the output of the BBD can be sampled at 8 kHz without filtering. A one pole low pass RC filter (cutoff frequency $=4 \mathrm{kHz}$ ) with gain was placed after the BBD to filter noise output of the BBD and to boost signal amplitude to 5 V peak.

The absolute value function is performed by two op amps and two diodes, the output of which is fed to a cascade of two simple SC one pole filters which implement $H(z)$ of equation (2.10). The output of the second filters is scaled by $\frac{4 \sqrt{2}}{H(1)}$ and then digitized by an 8 bit MDAC. The digital value is used to control a divider circuit (MDAC in an op amp's feedback path [ 30 ]) which sets the gain of the upper path. The delayed speech is scaled by this divider circuit, and the gain is changed each frame.

## 4.4:2. An MOS AGC

The ADC, MDAC, BBD delay line, and filters can all be integrated easily on an MOS IC. Simulations on the number of bits necessary for the AGC's MDAC were performed [ 18 ], and 5 bits of linear coding was found to be sufficient. So a 3 or 4 bit logarithmic ADC would serve adequately. These low speed, low resolution ADCs are easily implemented in a small silicon area [ 31 ]. The scaling of the filter output by $\frac{4 \sqrt{12}}{H(1)}$ can be accomplished simply by scaling down the ADC's voltage reference. Simple SC filters can be used to approximate $H(z)$.

The absolute value function is the only element of the AGC that can not be directly copied from the breadboard onto an IC because floating diodes are not available in a standard CMOS process. Therefore, diode-connected
enhancement-mode NMOS transistors are used instead. A full wave rectifier circuit (absolute value circuit) is shown in figure 4.13. It requires matched resistors and an op amp with low offset voltage, but the requirements are not strict since the AGC scaling need not be exact. Resistor matching of a few percent and 50 mV of ofiset are adequate.


Figure 4.13. MOS absolute value circuit

## CHAPTER 5

## EXPERIMENTAL RPSULTS

To test the system prior to integrating the autocorrelator, a breadboard was built. The breadboard was used extensively, both to test the SC multiplexed filters and to test the system's ability to function as an LPC speech analyzer. Then the SC autocorrelator IC was fabricated with a metal gate CMOS process and tested. For comparison, two sets of multiplexed filters were integrated on a polysilicon gate CMOS process. Results are given for the breadboard system, the IC autocorrelator, and the poly gate multiplexed filters.

### 5.1. THE BRREADBOARD SYSTEM

### 5.1.1. AUIOCORREATOR

An autocorrelator was constructed of commercially available parts to test various aspects of the design prior to integration of the autocorrelator. This was a necessary phase of the design since SPICE does not accurately model the MOSFET channel charge redistribution during turn off (see section 4.2.5). For the breadboard, capacitors were hand measured to assure better than $1 \%$ ratio accuracy. For all filters, switches were included only on the output side of the multiplexed capacitors (flgure 3.6).

Fllectrical data taken from the breadboard is tabulated in table 5.1. The autocorrelator did provide adequate accuracy for speech analysis despite the large amount of adjacent channel crosstalk in the multiplexed filters. The crosstalk is due to stray wiring capacitance on the breadboard which couples

| Autocorrelator Breadboard Data |  |
| :--- | :--- |
| parameter | measured value |
| Total system S/N ratio |  |
| (ADC. MDAC, and flters) | 64 dB |
| MDAC bits | 12 |
| Cutoff frequency of each filter section | 50 Hz |
| Cutoff frequency of fliter sections cascaded | 25 Hz |
| Adjacent channel crosstalk of multiplexed flters | -36 dB |
| (1V peaik sine wave at 10Hz) |  |
| Output swing for $\mathrm{HD} \mathrm{D}_{2}=1 \%$ | $\pm 5 \mathrm{~V}$ |
| (10Hz sine wave input) | 5 V |
| Full scale value of $\mathrm{R}(0)$ | 80 kHz |
| Clock frequency (10 channels) | $\pm 8 \mathrm{~V} . \pm 15 \mathrm{~V}$ |
| Power supply |  |

Table 5.1. Data from autocorrelator breadboard
the adjacent signal paths. The dynamic range of 64 dB was sufficient for speech analysis; the noise was due to analog noise sources and digital noise coupling into the analog signal lines on the breadboard. To test the breadboard with speech input, the breadboard was fed constant vowel sounds and the analog autocorrelation values output by the breadboard were digitized by a 12 bit ADC and stored on a mini-computer. The LPC spectrum for the autocorrelation values was plotted against the fit of the vowel sound to check for errors. As long as $R(0)$ was large enough so that quantization errors due to digitization of the autocorrelation values were negligible (i.e. $R(0)$ greater than 0.4 V ), the results were very good as can be seen in figures 5.1 through 5.4. In each figure, the upper plot is the LPC spectrum generated from data taken from the breadboard, and the lower plot is the LPC spectrum generated by computer simulation of the autocorrelation LPC algorithm. The LPC spectrum is plotted with the solid line, the fil of the sound with a broken line.




Fgure 5.1. top: LPC nt to /ee/sound, from breadboard data bottom: LPC fit to /ee/sound, computer simulation



Munitude las



Figure 5.4. top: LPC fit to /ah/sound, from breadboard data bottom: LPC At to /ah/sound, computer simulation

As a further check of the breadboard analyzer, the autocorrelation values were used to synthesize speech. First, vowel sounds were analyzed, synthesized, and then played back. The synthesis was compared to the original and found to be indistinguishable. Then, sentences were fed through the analyzer and then synthesized. Due to occassional unstable frames (caused by excessive quantization of the autocorrelation values) and a poor pitch tracker, the synthetic speech sounded much worse than the original. Nonetheless, all synthetic speech was understandable and considered acceptable by the listeners. A better pitch tracker would have greatly improved the quality of the synthetic speech.

### 5.1.2. THE DURBIN RRECURSION MCROPROCESSOR

The only question remaining in the microprocessor design was the speed of execution of the Durbin algorithm. The system frame rate is 80 Hz which allows 12.5 msec for execution of the algorithm. The execution time was found to be in the range of 10 msec to 11 msec when the 8088 clock frequency was 5 MHz . The execution time varies from frame to frame depending upon the number of calls of the 24 bit by 18 bit multiplication routine, which is dependent on the data and the number of $a_{4}$ which exceed 16 bits. Since 8088s which operate with an 8 MHz clock are now available, the execution time could be cut to less than 7 msec without changing the system at all. Frame periods are typically $10-50 \mathrm{msec}$ so the simple 8088 system (or equivalent) is adequate for all applications.

## 5.1.s. THE ACC

The AGC was constructed as discussed in chapter 4 - bucket-brigade delay line, full-wave rectifler, SC filter, ADC, MDAC. The AGC was found to work
very well, giving a constant autocorrelator output over an input range of 32 dB . The dynamic range of the AGC was limited by the BBD delay line noise. The BBD delay line had a dynamic range of only 34 dB ( 16 kHz sampling rate). If the BBD noise had not been a factor, the autocorrelator with the AGC would have had a useful input range of roughly 60 dB (32dB from the AGC plus 31dB from the autocorrelator). Without the AGC, the autocorrelator's input range was limited by the autocorrelator's dynamic range to 31 dB . But the value of $R(0)$ varies 62 dB as the input varies 31dB due to the squaring of the input signal. Therefore small input signals result in very small $R(0)$ values which are heavily quantized by the following ADC. So the autocorrelator's useful input range for LPC speech analysis without the AGC was actually about 10 dB . So the AGC was a very important addition to the system because it increased the useful input range for speech signals from 10 dB to 32 dB .

As was mentioned in the previous chapter, the BBD delay line held 128 samples which is 28 more than one frame. This is unfortunate but acceptable. A 100 stage BBD could be integrated or the frame length could be changed to 128 samples (frame rate= 82.5 Hz ). This was not done because the AGC was added to the system after the autocorrelator and microprocessor systems had been built, so the frame length was already set at 100 samples.

### 5.2. AUTOCORFKHATOR IC FESULIS

The MDAC and multiplexed SC fllters for the autocorrelator were integrated on a metal gate CMOS:IC. To allow flexibility in testing, all outputs and inputs were brought out to pins on the IC package so that the MDAC and each fllter section could be tested individually. The IC was fabricated in the integrated circuit laboratory at U.C.!Berkeley (see appendix D for process schedule). The yield was very poor, only $h$ few working chips were available
for testing after numerous runs in the fabrication lab.

### 5.2.1. IDAC

The IDAC was tested, and the data is presented in table 5.2. The integral non-linearity was larger than expected. This can be attributed to oxide gradients (the layout does not employ concentric placement of the capacitor array). parasitic capacitances, and rough metal edges (metal defined the capacitors in the MDAC). This non-linearity could be eliminated by more careful layout [ 32 ].

The reset feedthrough. which contributes to the DC output ollset voltage of the MDAC, was also larger than expected. When the reset switch turns ofl (see figure 3.3), its channel charge must go somewhere. The charge can flow to the op amp output node, to the op amp inverting input node, or to the substrate. It was expected that most of the charge would go to the op amp output node, but this was not the case. In fact, most of the channel charge llowed onto the inverting node, as can be seen'from the following calculations: The DC output voltage due to channel charge is (from equation 4.3)

| MDAC Data |  |
| :--- | :--- |
| parameter | measured value |
|  | 2 LSB |
| Integral non-linearity | 0.9 LSB |
| Diferential non-linearity | $2 \mu \mathrm{sec}$ |
| Settling time $(0.1 \%)$ | 30 mV |
| Reset fedthrough at output | $+3 \mathrm{~V},-5 \mathrm{~V}$ |
| Output swing | 66 dB |
| S/Nratio | $\approx 5 \mathrm{pF}$ |
| load capacitance | 60 kHz |
| Clock frequency | $\pm 7.5 \mathrm{~V}$ |
| Power supply | 15 mW |
| Power dissipation |  |

Table 5.2 Data for the 8 bit SC MDAC

$$
V_{\text {out } c c}=r \frac{Q_{c h a n n a l}}{C_{f b}}=\frac{r C_{o x}^{\prime} W L\left(V_{g s}-V_{t h}\right)}{C_{f b}} \approx r 37 m V
$$

for the MDAC with NMOS reset switch. The contribution to the DC output voltage due to the overlap capacitance is (also from equation 4.3)

$$
V_{o u t} \text { ov }=\frac{C_{o x}^{\prime} W L_{D} \Delta V_{c l}}{C_{f b}} \approx 2.3 \mathrm{mV} .
$$

(the gate overlap was estimated to be $L_{D}=1 \mu \mathrm{~m}$ under the microscope). Comparing these results, we see that the observed feedthrough at the output ( 30 mV ) is mainly due to channel charge from the reset switch being trapped onto the op amp's inverting node. From the experimental data, we can estimate $r \approx 0.75$. The value of $r$ is dependent on the impedance at the output of the op amp as well as the clock fall time (the reset clock line was driven by a 74 COB CMOS AND gate). A value of $r$ near zero would be desirable, but any value of $r$ is acceptable since the feedthrough is the same every cycle and therefore only contributes to the DC output voltage.

Figure 5.5 shows oscilloscope photos of the MDAC output. The top photo shows the MDAC squaring a triangle wave (upper trace), thereby producing a parabola wave output (lower trace). The lower photo shows the MDAC output (lower trace) settling to its final value during clock phase $\Phi_{2}$ (upper trace).

### 5.2.2. MOLTIPIEXED SC FILTERS

The fllters were tested individually. All three filter sections are different section one implements ten poles and ten zeros, section two implements ten poles, section three also implements ten poles but with different capacitor ratios due to downsampling.

The clocks which were used for testing the filters are shown in figure 5.6. In figure 3.6, the switch phasing is shown as $\Phi_{A}$ and $\Phi_{B}$. This labeling is used rather than $\Phi_{1}$ or $\Phi_{2}$ or $\Phi_{\mathbf{3}}$ because the best switch phasing was not known


Fgure 5.5. top: MDAC squaring a triangle wave bottom: MDAC output settling
before the circuit was fabricated although the phasing $\Phi_{A}=\Phi_{3}$ and $\Phi_{B}=\Phi_{2}$ was suggested in chapter 4. Note that $\Phi_{1}$ (reset) and $\Phi_{2}$ are non-overlapping clocks, and $\Phi_{3}$ goes low before $\Phi_{2}$ goes low. The clock amplitudes are $\pm 7.5 \mathrm{~V}$ ( +7.5 V is a logic HI level and turns on an NMOS switch).

To find the best clocking scheme, the fllters were tested with the following clocking schemes: 1) $\Phi_{A}=\Phi_{S}$ and $\Phi_{B}=\Phi_{2}, 2$ ) $\Phi_{A}=H I$ and $\Phi_{B}=\Phi_{2}$, and 3) $\Phi_{A}=\Phi_{2}$ and $\Phi_{B}=H I$. The results using clocking schemes (1), (2), and (3) were practically identical except for the DC output voltages. Also, with clocking scheme (3) the first two fllter sections did not work properly, probably due to the excessive capacitive loading on the op amp output from all ten feedback capacitors' backplate diodes. But section three did work with clocking scheme (3). The measured data is listed in table 5.3. Distortion and crosstalk figures were measured with a 10 Hz sine wave input signal. For the crosstalk


Pigure 5.6. Clocks for testing the multiplexed filters
measurement, the channel being tested had its input grounded and all other channels were fed a IV peak sine wave.

For all cases (except switching scheme (3) for fllter sections 1 and 2), the filter characteristics were very accurate, see figure 5.7. The frequency response of the different channels matched well (better than 0.2 dB ) due to the use of repeated unit capacitors in the layout.

For a given clocking scheme, the DC output voltage for fliter section 3 is smaller than for sections 1 and 2 because $C_{r}=0.22 p F$ in sections 1 and 2 and $C_{r}=0.60 \mathrm{p} F$ for section 3 (equation 4.4). As with the MDAC, the DC offset voltage of the filters was mainly due to the transistor's channel charge. For all filter sections, the DC offset voltage for clocking scheme (3) is smaller than that of scheme (1) or (2). With schemes (1) and (2), the channel charge for the input side switches is provided by the output of the op amp. The charge flows through the reset switch during the reset period. Then, when reset goes

| Measured Filter Characteristics (metal gate process) |  |  |
| :---: | :---: | :---: |
| parameter | filter se (z | filter section 3 |
| -3dB frequency | 50 Hz | 50 Hz |
| Output swing for $H D_{2}=1 \%$ | $\pm 1 \mathrm{~V}$ | $\pm 4 \mathrm{~V}$ |
| S/N ratio | 68dB | 70dB |
| Adjacent channel crosstalk | -44dB | -48d8 |
| Clock frequency (10 channels) | 80 kHz | 8 kHz |
| Sampling rate for each channel | 8 kHz | 800 Hz |
| Average DC output voltage of all channels (input grounded) |  |  |
| $\Phi_{A}=\Phi_{5} \Phi_{B}=\Phi_{g}$ | 2.8 V | 0.7 V |
| $\Phi_{A}=H H^{\prime}, \Phi_{B}=\Phi_{z}$ | 2.3 V | 0.4 V |
| $\Phi_{A}=\Phi_{g}, \Phi_{B}=H I$ | 0.4V | -0.18V |
| Range of DC output oflset voltages, all channels |  |  |
| $\Phi_{A}=\Phi_{5}, \Phi_{B}=\Phi_{2}$ | 440 mV | 40 mV |
| $\Phi_{A}=H{ }^{\prime}{ }^{\prime}{ }^{\prime} \Phi_{B}=\Phi_{2}$ | 200 mV | 18 mV |
| $\Phi_{A}=\Phi_{2,} \Phi_{B}=H I$ | 50 mV | 20 mV |

Table 5.3. Multiplexed Filter Characteristics, Metal Gate Process



Figure 5.7. top: Frequency response of multiplexed filter section 1 , channel 0 bottor: Computer simulation of the above filter
low, the reset switch's channel charge is trapped on the op amp input node and contributes to the DC output voltage. With scheme (3), the reset switch's channel charge which is trapped on the op amp inverting node when reset goes low is used to form the channel for the input side switch when it turns on, thereby giving a flrst order cancellation of the channel charge and a lower DC output voltage.

The harmonic distortion is a function of the output signal level and DC output voltage of the filter. The harmonic distortion is caused by channel charge redistribution which is signal dependent.

An unexpectedily large adjacent channel crosstalk was measured. Crosstalk should be negligibly small because the reset period between channels eliminates the main crosstalk path which is through $\boldsymbol{C}_{r}$. The crosstalk is either due to poor isolation between nearby $\mathrm{N}+$ diffusions, charge pumping through the substrate to the nearby switch transistors, dielectric absorption in $C_{\text {r }}$, or signal coupling onto $C_{f b}$ through the overlap capacitances of the off switches.

### 6.2.3. OPERATIONAL AMPLIFIER

The op amp was tested alone to compare its performance with the design goals. It met or exceeded all requirements of the system. Data for the metal gate op amp is given in the second column of table 5.4.

### 5.2.4. THE IC AS AN AUTOCORRREATOR

Figure 5.8 shows the IC operating as an autocorrelator. The upper trace is the output of the MDAC. The ten products can be clearly seen. The lower trace is the output of the filters. The output is a constant autocorrelation waveform. $R(0)$ is at the left, $R(9)$ is at the right. In both traces, the reset

| Measured Op Amp Characteristics |  |  |
| :--- | :--- | :--- |
| parameter | Metal Gate | Poly Gate |
| Gain | $8,000 \mathrm{~V} / \mathrm{V}$ | $1,000 \mathrm{~V} / \mathrm{V}$ |
| Maximurn output swing | $\pm 5.5 \mathrm{~V}$ | $+1 \mathrm{~V} .-3 \mathrm{~V}$ |
| Noise | $100 \mathrm{nV} / \sqrt{\mathrm{Fz}}$ | $580 \mathrm{nV} / \sqrt{\mathrm{Hz}}$ |
| Noise $1 /$ f corner frequency | 700 Hz | 1 kHz |
| Power Supply | $\pm 7.5 \mathrm{~V}$ | $\pm 6 \mathrm{~V}$ |
| $I_{\text {BIAS }}$ | $150 \mu \mathrm{~A}$ | $300 \mu \mathrm{~A}$ |
| Power Dissipation | 10 mW | 18 mW |
| Number of transistors | 14 | 14 |
| Size | $450 \mathrm{mil}^{2}$ | $460 \mathrm{mil}^{2}$ |

Table 5.4. Op Amp Data, Metal Gate and Poly Gate Processes


## TIME (I2.5uS/DIV)

Pigure 5.8. SC autocorrelator output with sine wave input
period can be seen between channels. The input signal is a 1 kHz sine wave, so the output autocorrelation function is samples of a sine wave.

Unfortunately, the IC autocorrelator did not provide enough accuracy for analyzing speech due to the excessive crosstalk in the filters and the MDAC non-linearity. Also, due to low yield, no chip was found which had a fiter sec-
tion 1 with all 10 zeros functioning. Speech was passed through the IC autocorrelator, but the autocorrelation values usually yielded an unstable LPC model. Nonetheless, the autocorrelation function was fairly accurate, and the IC could have been used for voiced/unvoiced decision making or other low accuracy applications.

### 5.3. A SECOND TEST CHIP

Since excessive crosstalk and offset voltages were measured and since the zeros were not all functional, a second IC consisting of two multiplexed filter sections was constructed. (The two multiplexed flter sections will be refered to as $A$ and $B$ to avoid confusing them with filter sections 1,2 , and 3 of the autocorrelator IC.) Each section has four multiplexed feedback capacitors and zero capacitors. Section A's capacitor ratios were chosen to give a $\mathbf{5 0 H z}$ cutofif frequency at an 8 kHjz sampling rate (similar to the first and second filter sections of the autocorrelator 1C). Section B's capacitor ratios were chosen to give the 50 HZ cutofl at an 800 Hz sampling rate (similar to the third fllter section of the autocorrelator). As in the autocorrelator, section A uses a minimurn unit capacitor for $C_{r}$, section $B$ uses 3 unit capacitors for $C_{r}$. In this IC, all switch gates are brought out to pins to allow maximum flexibility during testing.

The layout of the second IC is shown in figure 5.9. The chip was fabricated on a digital CMOS process with $N$ type substrate, polysilicon gate, with poly:poly capacitors. The op amp is practically identical to the op anp described in chapter 4 with all devices replaced by their complement. This was done to assure that current sources were implemented by NMOSFETs because they are in a well and have a higher output impedance than the PMOSFETs. For the fllters, PMOSFETs were used as switches since they do not


Figure 5.9. Layout of the poly gate multiplexed flters
require a well.

### 5.3.1. RESULITS

The poly gate ICs were extensively tested. The yield was excellent for these chips ( 9 out of 10 worked). This reflects the clean, reliable processing done in industry. Again, to check the effects of various switching schemes. the multiplexed filters were tested with all possible clocking schemes. The clocks used are an inverted version of those shown in figure 5.6 because the switches are PMOS. (A logic HI level is taken to be the voltage required to turn on a switch, so HI is -6 V for this IC.) The measured data for the poly gate filters is tabulated in table 5.5. The most striking differences between the poly gate filters and the metal gate filters are the lower output offiset voltages and lower crosstalk measured for the poly gate filters. The lower offsets are a

| Measured Filter Characteristics (poly gate process) |  |  |
| :---: | :---: | :---: |
| parameter | fllter sec (zeros | filter section B |
| -3dB frequency | 50 Hz | 50 Hz |
| Output swing for $H D_{2}=1 \%$ | 0.7 V | 1V |
| Dynamic range | 62dB | 68 dB |
| Adjacent channel crosstalk | -78dB | -80dB |
| Clock frequency (4 channels) | 32 kHz | 3.2 kHz |
| Sampling rate for each channel | $8 \mathrm{k} H z$ | 800 Hz |
| Average DC output voltage of all channeis (input grounded) |  |  |
| $\Phi_{A}=\Phi_{S_{1}} \Phi_{B}=\Phi_{2}$ | -750mV | -130mV |
| $\Phi_{A}=H I, \Phi_{B}=\Phi_{2}$ | -50mV | -45mV |
| $\Phi_{A}=\Phi_{2}, \Phi_{B}=H I$ | 180 mV | 40 mV |
| $\Phi_{A}=\Phi_{2} \Phi^{\prime} \Phi_{B}=\Phi_{2}$ | 200 mV | 55 mV |
| Range of DC output offset voltages, all channels |  |  |
| $\Phi_{A}=\Phi_{\text {S }} \Phi_{B}=\Phi_{2}$ | 500 mV | 50 mV |
| $\Phi_{A}=H I, \Phi_{B}=\Phi_{2}$ | 60 mV | 20 mV |
| $\Phi_{A}=\Phi_{2}, \Phi_{B}=H I$ | 340 mV | 120 mV |
| $\Phi_{A}=\Phi_{2} \Phi_{B}=\Phi_{2}$ | 400 mV | 110 mV |

Table 5.5. Data for the multiplexed filters, poly gate process
direct consequence of the smaller gate area and overlap capacitances of the self-aligned poly gate transistor. The lower adjacent channel crosstalk is as expected, and the cause of the crosstalk in the metal gate filters is not clear. Possibly the crosstalk comes from coupling onto $C_{f b}$ through the off transistors' overlap capacitances which is much larger in a metal gate process.

The harmonic distortion rapidly decreases as the output swing decreses. Typically, $H D_{2}=1 \%$ for an output swing of $1 V, H D_{2}=0.1 \%$ for an output swing of 0.25 V , and $H D_{2}$ is buried in the noise for any output swing less than 0.1 V . The harmonic distortion only varied a few dB as the different clocking schemes were tried. There was a larger variation in distortion from one chip to another for a given clocking scheme than there was for different clocking schernes on a given chip.

The frequency response for filter section $A$ without the zeros is shown in flgure 5.10. In figure 5.11, the frequency response of section $A$ with a zero is shown. Note the difference in the frequency response when the switch phasing for $G$ is reversed. These responses agree with the transfer functions derived in chapter 3 (equations 3.2 and 3.3).

### 5.3.2. OP AIP

The op amp characteristics were measured and are included in the last column of table 5.4. The output swing of the op amp was limited to +1.25 V . -3 V due to the large body effect of the process.


## FREQUENCY(500Hz/DIV)



Figure 5.10. top: Frequency response of section A, channel 0 bottom: Frequency response of passband of section $A$, channel 0

##  <br> FREQUENCY(500Hz/DIV)



## FREQUENCY ( 500 Hz IDIV)

FIgure 5.11. top: Frequency response of section $A$ with zero, noninverting phasing of $C_{8}$ (equation (3.2) , $C_{s}=C_{\gamma}$ )
bottom: Frequency response of section A with zero, inverting phasing of $C_{5}$ (equation (3.3), $C_{2}=C_{4}$ )

## CHAPTER 6

## SUMMARY AND CONCLUSIONS

An autocorrelation LPC analysis system was built with commercially available parts. The system consisted of an anti-alias/pre-emphasis filter, automatic gain control, SC autocorrelator, and microprocessor. The system did analyze speech in real time with sufficient accuracy to generate useful LPC model parameters.

The switched-capacitor components of the autocorrelator (i.e. MDAC and multiplexed filters) were integrated on a metal gate CMOS IC. While the MDAC and filters were fully functional, problems such as MDAC non-linearity and crosstalk in the filters limited the accuracy of the autocorrelator to less than required for LPC analysis. The MDAC non-linearity can easily be reduced by a more careful layout of the capacitor array. The crosstalk in the metal gate filters is believed to have been caused either by the large overlap capacitances of the metal gate transistors coupling signal onto the feedback capacitors or by signal retained on capacitor $C_{r}$ after the reset period (dielectric absorption). A second IC consisting of two multiplexed flter sections was fabricated on a polysilicon gate CMOS process. Both the crosstalk and DC output offset voltage of the multiplexed filters were greatly reduced on this poly gate IC.

The results gathered from the fabricated ICs verify that multiplezed SC filters can be integrated with performance which matches or exceeds that of the breadboarded filters. By combining these fllters with an accurate 8 bit SC MDAC, an autocorrelator with sufficient accuracy for speech analysis can be
integrated. (SC MDACs of 10 bit accuracy have been successfully integrated [32], so an 8 bit SC MDAC can be integrated.)

The complete autocorrelator in integrated form would include an 8 bit ADC, 8 bit MDAC, digital delay line (RAN), SC multiplexed fllters, and control logic. With a modern polysilicon gate CNOS process with $3 \mu \mathrm{~m}$ line widths, it is estimated that the entire autocorrelator would fit on a $10,000 \mathrm{mil}^{2}$ chip.

### 6.1.1. IMPROVEIENTS AND MODIFICATIONS

The system could be modified to give improved performance. The occassional unstable frames which are caused by course quantization of the autocorrelation values could be eliminated if the ADC which quantizes the autocorrelation values has an adjustable reference voltage which is set to $R(0)$ or a voltage slighty greater than $R(0)$ each frame. (This is possible because $|R(k)| \leq R(0)$ for all $k$.) This would make more effective use of the ADC's bits. But the DC offsets of the filters would have to be canceled prior to the $A D C$ or the microprocessor would have to know the reference voltage each frame so it could properly subtract the offset voltages.

The op amp associated with the MDAC could be completely eliminated by making $C$ of filter section 2 or 3 a binary weighted capacitor array and using the digital word $s(\pi-k)$ to select the capacitors and to determine the switch phasing.

If an LPC model with more poles is desired, the system is easily expanded to produce more autocorrelation values. The number of autocorrelation values which could be generated by the NDAC and multiplezed alters is limited by the settling time of the op amp.

The major drawback of the system is the need for multiple ADCs - one in the AGC, one to digitize the speech in the autocorrelator, and one to digitize the autocorrelation values for the microprocessor. Time sharing of these $A D C s$ is possible since the autocorrelation values and AGC gain value are sampled at the frame rate which is much less than the sampling rate.

The AGC was very effective and could be more so if a quieter analog delay line were available. Other modifications to the AGC were considered and analyzed in [ 18 ].

It is possible that a simpler window could be used in the LPC autocorrelator. This would reduce the area required for the multiplexed filters. For instance, the zeros in the transfer functions have little effect and possibly could be elininated altogether. This is worth investigating.

### 6.1.2. IC LAYOUT AND MODULAR DESGGN

The layout of the metal gate IC was a long, slow process. From start to finish, the layout took about six months. Learning how to use the layout program, poor graphics (a small black and white screen), and painful ploting (two tape transfers between three computers) contributed to the slow layout. Also, a great deal of time was spent experimenting with the layout to achieve the minimum total area. And, as problems came to light, circuit simulations were performed.

In contrast. the time required to lay out the poly gate IC was only three days! The layout was greatly simplifled because building blocks (op amp, switches, and capacitors) had already been layed out by other students and were available. A new layout program with color graphics had been developed [ 33 ], and a plotter was available on the computer which was being used for layout. The total area of the chip was determined by the need for 40 bonding
pads, so there was no reason to worry about saving area during layout. The great reduction in layout time reflects an improvement in layout tools and the usefulness of pre-designed circuit building blocks.

### 6.1.3. ANALOG VS. DIGITAL PROCESSING

In most applications, the words "signal processing" are proceeded by the word "digital". Analog signal processing is dominant in high frequency applications where digital circuits are not fast enough to perform the required computations. But with switched-capacitor technology, all the basic building blocks necessary for analog signal processing are available (appendix B).

Digital processing has an advantage in that layout is not as critical for digital ICs as it is for analog ICs where parasitics must be taken into consideration. Many digital building blocks (or cells) have been developed, and they make for a quick and easy IC layout. But in digital processing, quantization, area, and power dissipation can be a problem.

Analog signal processing should be considered whenever signal processing tasks are to be performed. There are times when analog signal processing will result in a smaller, lower power integrated circuit and is worth the time and effort to design.

## APPENDIX A

## FINDING THE FILTER TRANSFER FUNCTION

A derivation of the filter transfer functions $H^{\prime}{ }_{k}(z)$ (equation 2.11) is included here for completeness. We begin by recalling the time window suggested by Barnwell [5]

$$
w(n)=(1-n) \alpha^{-n} \quad n \leq 0.0<\alpha<1
$$

and

$$
h(n)=w(-n)=(n+1) \alpha^{n} \quad n \geq 0, \quad 0<\alpha<1
$$

which has the $z$-transform

$$
\begin{equation*}
H(z)=\frac{1}{\left(1-\alpha z^{-1}\right)^{2}}, \quad|z|>\alpha . \tag{A.1}
\end{equation*}
$$

The $z$-transform of the sequence $h_{k}^{\prime}(n)=h(n) h(n+k)$ is desired. The $z$ transform of $h(n+k)$ is

$$
h(n+k) \rightarrow z^{k} H(z)=\frac{z^{k}}{\left(1-\alpha z^{-1}\right)^{2}} \quad|z|>\alpha .
$$

$H_{k}(z)$ is found by integrating, equation (2.8),
$H_{k}{ }_{k}(z)=H_{k}(z)^{*} z^{k} H_{k}(z)=\frac{1}{2 \pi j} \int v^{k} H(v) H\left(\frac{z}{v}\right) v^{-1} d v=\frac{1}{2 \pi j} \int H(v) H\left(\frac{z}{v}\right) v^{k-1} d v$ where the integration is along any closed path in the region of convergence of both $H(v)$ and $H\left(\frac{\boldsymbol{z}}{v}\right)$.

Substitution of (A.1) into (2.8) gives

$$
H_{k}^{\prime}(z)=\frac{1}{2 \pi j} \int \frac{1}{\left(1-\alpha v^{-1}\right)^{2}} \frac{1}{\left(1-\alpha \frac{v}{z}\right)^{2}} v^{k-1} d v=\frac{1}{2 \pi j} \int \frac{1}{(v-\alpha)^{2}\left(1-\alpha \frac{v}{z}\right)^{2}} v^{k+1} d v .
$$

We already know that $H(v)$ converges for all $|v|>\alpha$. So $H\left(\frac{z}{v}\right)$ will converge if $\left|\frac{z}{v}\right|>\alpha$, or equivalently, $|v|<\frac{|z|}{\alpha}$. The common region of convergence is
$\alpha<|v|<\frac{|z|}{\alpha}$ Any closed path in the common region will encircle the pole of order two at $v=\alpha$; the poles at $v=\frac{z}{\alpha}$ are outside any such path. Note that since we are interested in values of $k \geq 0, v^{k+1}$ is analytic everywhere and does not contribute a pole. The integral can therefore be evaluated using the residue theorem which states that an integral around a closed contour equals $2 \pi j$ times the sum of the residues of the integrand evaluated at all poles encircled by the path of integration [ 34 ].

Since $H(v)$ has a pole of order two at $v=\alpha$, evaluation of the residue of the integrand is found by differentiating

$$
\text { residue }=\left.\frac{\partial\left[(v-\alpha)^{2} H(v) H\left(\frac{z}{v}\right) v^{k+1}\right]}{\partial v}\right|_{v=a}=\frac{(k+1) \alpha^{k}+(1-k) \alpha^{k+2} z^{-1}}{\left(1-\alpha^{2} z^{-1}\right)^{3}}
$$

This residue equals $H_{k}{ }_{k}(z)$ since the $2 \pi j$ which multiplies the integral in (2.8) cancels the $2 \pi j$ of the residue theorem.

It is worth noting that if $h(n)=w(-\pi)$ is chosen to be the impulse response of a one pole filter, the resulting output filters $H_{k}{ }_{k}(z)$ are also one pole filters. That is, if $h(n)=w(-n)=\alpha^{n}$ for $n \geq 0$ so that

$$
H(z)=\frac{1}{1-\alpha z^{-10}}
$$

then

$$
H_{k}^{\prime}(z)=\frac{\alpha^{k}}{1-\alpha z^{-1}}
$$

The question might arise, "If a one pole window corresponds to a one pole output filter, and if a two pole window corresponds to a three pole output filter, then what type of window corresponds to a two pole output filter?" If we take for $H_{0}^{\prime}(z)$ the two pole filter

$$
H_{0}^{\prime}(z)=\frac{1}{\left(1-\alpha z^{-1}\right)^{2}}
$$

which has the corresponding impulse response

$$
h_{0}^{\prime}(n)=(n+1) \alpha^{n} .
$$

and recall that the output filter for $k=0$ has impulse response $h_{0}^{\prime}(n)=h^{2}(n)=w^{2}(-n)$, then the window can be found from

$$
h(n)=\sqrt{h_{0}^{\prime}(n)}=\sqrt{n+1} \alpha^{\frac{n}{2}}
$$

Such a window has no discontinuities and more heavily weights the present frame than the past frames as desired, but computation of $H_{k}^{\prime}(z)$ for $k \neq 0$ is impossible because $h(n)$ is irrational in $n$ and therefore does not have a closed form $H(z)$ representation to use in equation (2.8). $H_{k}^{\prime}(z)$ is the $z$ transform of $h_{k}^{\prime}(n)=h(n) h(n+k)$ which can be written

$$
h_{k}^{\prime}(n)=h(n) h(n+k)=\sqrt{(n+1)(n+k+1)} a^{\left(n+\frac{k}{2}\right)} .
$$

The inability to find $H_{k}^{\prime}(z)$ as a rational polynomial which can be realized as a recursive sampled-data fllter eliminates this window from consideration.

## APPENDIX B

## CATALOG OF ANALOG COMPUTATIONAL CIRCUITS

The autocorrelator employs the basic computational building blocks for signal processing - delay, multiplication, and filtering. There are many ways to implement each of these blocks, and some alternatives are mentioned briefly below. For a more detailed discussion of each circuit, please see the references cited.

### 1.1.1. DEAAY LINES

Digital delay lines are basically RAM and all are functionally the same. A number of different RAM cells are available for constructing a digital delay line [ 35 ]. Analog delay lines are of two types - cascaded sample-and-hold circuits or multiplexed sample-and-hold circuits.

The simplest MOS sample-and-hold circuits suffer from offset and signal dependent errors (i.e. distortion) due to overlap capacitance and channel charge redistribution. An interesting, feedback-corrected sample-and-hold was presented recently [ 36 ]. Dynamic range of 80 dB was reported for this sample-and-hold which was constructed with a polysilicon gate process.

A multiplexing sample-and-hold ( $\mathrm{S} / \mathrm{H}$ ) scheme, employing one op amp and $p$ capacitors, was used in an LPC lattice analyzer [ 14 ]. The delayed signals are stored on different capacitors, and when a particular delayed signal is desired, the corresponding capacitor is connected into the circuit. The accuracy of this multiplexed $\mathrm{S} / \mathrm{H}$ was limited by the fixed-pattern noise associated with the switching. A dynamic range of only 45 dB was reported, but the
circuit was constructed with a metal gate process; so direct comparison with the 80 dB figure above is not possible.

### 1.1.2. ANALOG MULTIPLER

A four-quadrant analog MOS multiplier has been fabricated by Soo [ 37 ]. This multiplier provided 77 dB of signal-to-noise ratio, 1.5 MHz bandwidth, and $0.3 \%$ non-linearity while occupying $450 \mathrm{mil}^{2}$ of chip area. Such a circuit, if combined with a high quality analog SC delay line, would work very well in an autocorrelator.

A four-quadrant analog multiplier/divider in bipolar technology was reported by Gilbert [ 38 ]. The non-linearity was an excellent $0.01 \%$ with a $\pm 10$ volt input signal swing. This circuit might be used with SC delay line and filters in a bipolar compatible CMOS process. The delay lines (cascaded S/H circuits) and filters for the autooorrelator in a purely bipolar technology would be prohibitively large.

### 1.1.3. MDACs

An MDAC is just a DAC with its analog reference input connected to an analog voltage equal to the multiplicand. No attempt will be made to discuss all the possible resistive DACs, capacitive DACs, and combinations thereof which might function as an MDAC; see references [39] and [30] for such a discussion. The MDAC chosen for the autocorrelator is a capacitive DAC compatible with a standard CMOS process.

### 1.1.4. FILTERSS

Various implementations of a real pole and real zero are available. The low frequency cutoff of 25 Hz eliminates RC filters from considerations due to the large area required. Some clever implementations of continuous time
filters with low cutoff frequencies using FETs have been reported [ 40 ].[ 41 ]. SC filters allow low cutoff frequencies and have become very popular for audio range filtering [ 39 ]. Implementation of a negative real zero (in the $z$ domain, not the s-domain) poses a problem in some SC conflgurations.

### 1.1.5. ABSOLUTE VALUE CIRCUITS

An MOS absolute value circuit can be constructed using a diodeconnected enhancement mode transistor to restrict current flow to one direction only, figure 4.13. Accurately matched resistors are required in such a circuit. Alternatively, a sampled-data SC absolute value circuit can be used to compute the absolute value of the input. This requires a comparator to determine the sign of the present sample and an amplifier with a programmable gain of $\pm 1$. In a SC amplifier, the sign of the gain is easily inverted by changing the switch phasing of the input sampling switch.

### 1.1.6. LONG DELAY LINES

Long delay lines, with lengths on the order of a hundred samples, are not feasibly realized as a cascade of sample-and-hold circuits because the number of op amps becomes large, and the area required for them becomes prohibitive. The multiplexed $\mathrm{S} / \mathrm{H}$ mentioned above might work for large delays. But the natural choice for a long analog delay line is the chargecoupled device or the bucket-brigade device. They are compatible with MOS circuitry. A digital approach would employ a large RAM.

## APPENDIX C

## SPEECH PROGRAMS AND SENTENCES

Computer simulation results presented in chapter 4 were performed by passing digitized speech through custom written programs. The speech was sampled at 8 kHz and digitized by a 12 bit ADC. All programs were written in the $C$ programming language. When required, synthesized speech was played back by a 12 bit DAC operating at an 8 kHz rate. The sentences used for the simulations are listed in table C. 1 , followed by the source code for the programs.

### 2.1. GENERRATEAUTO.C

The program Generateauto.c simulates the autocorrelation system and allows optional inclusion of the various system modifications - downsampling, AGC. multiplier quantization (MDAC), pre-emphasis, and quantization of the autocorrelation values. It takes speech as input and generates the autocorrelation values for each frame. The source for Generateauto.c is listed on the following pages.

| Digitized Speech Used for Simulations |  |  |
| :---: | :---: | :---: |
| File Name | Sentence or Phrase Spoken | Speaker |
| Adam.t | Adam. | George White |
| Baker.t | Baker. | George White |
| Charlie.t | Charlie. | George White |
| David.t | David. | George White |
| Dr.Bob.t | Doctor Bob is on vacation again. | Paul Hurst |
| Hello.t | Hello, how are you? | Paul Hurst |
| Susan.t | Susan kicked the goat on Sunday. | Paul Hurst |
| Suzie.t | Suzie sat on the sandwich. | Paul Hurst |
| Thieves.t | Thieves who rob friends deserve jail. | Peter Chu |
| We.t | We were away a year ago. | Bob Brodersen |
| Why.t | Why do I owe you a letter? | Peter Chu |
| ah.t | /ah/ | synthetic sound |
| ahsh.t | /ah/./sh/ <br> We publish part one of the | synthetic sounds |
| audiocritic.t | transcript of our all day seminar on the state of the art. | Bob Brodersen |
| clock.t | Clock, slope,field. | John Fattaruso (RSB) |
| cursor.t | Move the cursor to the clock slope field. | John Fattaruso |
| demo.t | This is a demonstration of synthetic speech. | Bob Brodersen |
| ee.t | /ee/ | synthetic sound |
| handel.t | Behold, I tell you |  |
|  | a mystery. | John Fattaruso |
| is.t | Is waiting to see you. | Steve Love |
| mike.t | The two powering modules available are fitted with a battery and a balancing transformer. | Steve Love |
| oak.asa.t oak.ellen.t | The oak trees are strong. The oak trees are strong. | Asa Romberger Ellen Szeto |
| poweramp.t | The two most interesting power amplifiers for the audio purist. | Barry Hyman |
| room_noise.t | (background room noise) | small fan running |
| sh.t | /sh/ | synthetic sound |
| shah.t | /sh/./ah/ | synthetic sounds |
| ss.t | /ss/ | synthetic sound |
| trends.t | Trends and perspectives in signal processing. | Steve Love |
| xyz.t | XY Z . | Paul Hurst |

Table C.1. Speech used in the simulations of chapter 4

## GENERRATEAUTO.C

\#define SOURCE "/brodersen/hurst/bin"
\#ifdef M
\#undef SOURCE
\#define SOURCE "/mb/audio/hurst/bin"
\#endif
\#include <stdio.h>
\#include <sys/types.h>
\#include <sys/stat.h>
/* This program generates the first 10 autocorrelation values

* for the input file. The autocorrelation values are stored in
* fles. 'output1.xx' contains the autocorrelatin values determined
* using Barnwell's 10 filters exactly. 'output2.xx' contains the
* autocorrelation values determined using a lower sampling rate
* on the last section of each filter.
* 
* to compile: cc -O Generateauto.c -Im -INS
* 

*This is the VAX version.
*/
\#define AD_BITS $11 / *$ number of bits in A/D converter (excluding sign bit) */
\#define $A D$ full scale 2047
\#define POINTS $400 / *$ sets maximum frame size (in samples) */
\#define ALPHA 0.98
\#define pi 3.1415927
\#define NO AUTOC 10
\#define MAX FRAMES 500 /* limits maximum number of frames to 500 */
\#define $\operatorname{sign}(x)(((x)>=0) ? 1:-1) / *$ nice line of code, huh? */
/* see 'C manual', pg. 47 */
$/ *$ all external variables are initialized to 0 */
int frame_rate $=80$;
int samp_freq $=8000$;
int contsampflag $=0$;
int dwnsampflag $=0$;
int gainflag $=0$;
int preemplag $=1$;
int ageflag $=0$;
int clipflag $=1$;
int quant flag
int q bits $=0 ; / *$ This value is never used. If quant_flag $==1, q$ bits is * read from command line.
*/
int $r$ full scale $=2047$;
int rfs_bits $=11$ :/* rfs_bits is 'r_full_scale_bits'. \# bits which correspond * to r_full_scale.
*/
float R[MAX_FRAMES][NO_AUTOC];
struct stat stbuf;
FILE *fopen().*fp_scaled,*fp_sec 1,*fp_sec2,*fp_sec3,*fp_quant;
main (argc,argv)
int argc;
char *argv[];
\{ int i, 1, rate,row,frames,atoi(),framelength,agc[MAX_FRAMES], power(); long filesize; float $\cos ($ ), pow(),low_pass(), mult();
float max_RO,s[POINTS],prod[POINTS]; char *temp file, *mktemp(); FILE *fopen().*fp_input;
$\max \mathrm{RO}=0.0$;
if (arge ==1) instructions();

$$
\mathrm{i}=2 ;
$$

$$
\text { while }(++i<=\operatorname{argc})
$$

$$
\left\{\quad \text { if }\left(\operatorname{argv}[\mathrm{i}-1][0]!={ }^{\prime} \because^{\prime}\right)\right.
$$

ex ("bad parameter");
else switch(argv[i-1][1])
\{ case ' $c$ ': contsampflag $=1$;
break,
case ' $d$ ': dwnsampflag=1;
rate=atoi $(\operatorname{argv}[i++])$; if(rate $==0$ ) ex("-d ?"); break;
case ' $r$ ': frame_rate=atoi $(\operatorname{argv}[i++])$;
break;
case 'g': gainflag=1;
break;
case 'b': rfs_bits=atoi(argv[i++]);
$r$ full _scale=power(2,rfs_bits) - 1;
gainflag=1;
printf("gainflag is now on (i.e. -g flag assumed) $\ n$ ");
if((rfs_bits > 15) || (rfs_bits < 5 ) )
ex("bad number of bits");
break;
case 'a': agcflag=1;
break;
case ' $k$ ': clipflag $=0$;
break;
case ' $q$ ': quant flag $=1$;
q bits=atoi(argv[i++]);
break;
case ' $p$ ': preempflag=0;
break;
case 's': samp_freq=atoi(argv[i++]);
break;
default: ex("bad parameter");
() ()












:(.u\ әाए 7ndur uado 7.ueo..) xa


:(., uNINdNI DNIZISVHdWE-TY










( $\tau==$ get゙ $\ddagger$ Uenb) $!$







:I = isegduresquos





```
}
/* s[i] will hold the speech samples */
for ( }\textrm{i}=0;\textrm{i}<\mathrm{ POINTS; ; + + )
    s[i] = 0.0;
    for(i=0;i<POINTS;i++)
    prod[i] =0.0;
    for (row=0;row<frames;row++)
    {
        printf("\nframe %4d ",row+1);
        for (i=0;i<NO_AUTOC;i++)
            s[i] = S[i+framelength];
    for (i=NO AUTOC;i<framelength+NO_AUTOC;i++)
            s[i] = getsh(fp_input);
        if (preempflag == 1) preemp(s,framelength);
        if (agcflag==1) do_agc(s, agc,framelength,row);
        for (l=0;1<NO_AUTOC;1++)
        {
            for(i=0;i<framelength+1;i++)
                prod[i]=mult(s[i+NO_AUTOC-1],s[i-1+NO_AUTOC-1],
                q_bits,1)/AD_full_scale;
            if (contsampflag == 1)
                R[row][1]=low_pass(prod,1,1,framelength);
            if (dwnsampflag == = 1)
                R[row][1]=low_pass(prod,l,rate,framelength);
            }
}
for (i=0;i<frames;i++)
    if (R[i][0] > max_RO) max_RO=R[i][0];
if (contsampflag == 1)
    norm_store(max_R0,frames, 1,agc);
if (dwnsampflag == 1)
    norm_store(max_R0,frames,2,agc);
fclose(fp_input);
fclose(fp_sec1);
fclose(fp_sec2);
fclose(fp_sec3);
/* sys_call("/bin/rm %s",temp_fie); */
if(agcflag == 1) fclose(fp_scaled})
if(quant_flag == 1) fclose(fp_quant);
printf("\n");
}
/* low_pass() is the bank of low pass filters required in the autocorrelation
```

[^0]
## */

\#define fc 51.453
\#define p1 0.9604
\#define p2 0.9604
\#define gain1 2.5
\#define gain2 1.38
\#define gain3 1.3
/*51.453 is the -3db point for filter \#3 when fs $=8 \mathrm{kHz*}$ /
/*want filter section 1 to have de gain $=2.5 \quad$ */
/*gain of filter section 1 (due to b0 \& b1) is 1.9804*/
$/ *$ so gain1*1.9604 $=1.27 * 1.9604=2.5$
\#define GAINO 1.9604 /*This is the de gain for filter section 0 for R[0] */
float low_pass(prod, 1, rate,framelength)
int 1,rate, framelength;
float prod[POINTS];
\{ float input2,input3;
float pow(), cos(),sqrt(), x, b0,b1,p3,g1,g2,g3,z1,d0;
int i, section;
/* hopefully, all static variables are initialized to zero (seems to be true) */
static float output1[2][NO_AUTOC], output2[2][NO_AUTOC], output3[2][NO_AUTOC];

```
if (rate == 1) section = 0;
else section = 1;
b0=(l+1)*pow(ALPHA,1+0.0);
b1=(l-1)*pow(ALPHA,l+2.0);
z1=b1/b0;
dO=bO/GAINO; /* what the heck is dO ? */
x=cos(2.0*pi*fc/(8000/rate)); /* compute p3 (it depends on the */
p3=(2-x) - sqrt((2-x)*(2-x)-1); /* down sampling of last section.
                                    * 8000 is sampling rate which is
                                    * assumed in window parameters
                                    */
g1=gain1*(1-p1)/GAINO;
g2=gain2*(1-p2);
g3=gain3*(1-p3);
for(i=1;i<framelength+1;i++)
{ input2=output1[section][1];
    input3=output2[section][1];
    output1[section][1]=p1*output1[section][1]+
    (b0*prod[i]-b1* prod[i-1])*g1;
    if (l==0) putsh((short)output1[section][l],fp_sec1);
    output2[section][[1]=p2*output2[section][1]+input2*g2;
    if (l==0) putsh((short)output2[section][1],fp_sec2);
    if(i==(i/rate)*rate)
        { output3[section][1]=p3*output3[section][1]+input3*g3;
        if (l== 0) putsh\(short)output3[section][1],Pp_sec3);
        }
}
return(output3[section][1]);
```

3
/* norm_store() scales autocorrelation results (if asked) and stores * the results in a file.
*/
norm_store(max, rows,outflag, age)
float max;
int rows, outflag, age[MAX FRAMES];
\{ int $\mathrm{i}, \mathrm{j}$, norm, scale, quantize(),round_off();
float fscale,sqrt();
char *filename;
FILE *fopen(), *fp_output;

```
    if (outflag == 1)
    {
        if (gainflag == 1) filename = "output1.g";
        else if (agcflag == 1) filename = "output1.agc";
            else flename = "output1.ng":
3
    else
    }
        if (gainflag == 1) filename = "output2.g";
        else if (agcflag == 1) flename = "output2.age";
            else flename = "output2.ng";
    }
    if ((fp_output = fopen(filename.'w'")) == NULL)
        ex("can't open output file");
    if (max < 0.01) max = 0.1; /* in case max is zero */
    for (i=0;i<rows;i++)
    { if (gainflag == 1)
        if (R[i][0] < 0.01) fscale = 1;
        else fscale = max / R[i][0];
        for(j=0;j<NO_AUTOC;j++)
        { if (gainflag == 1)
        { norm = (r_full_scale*(R[i][i]/max)*fscale);
        /* assure \overline{R[0] = r_full scale */}
                if(j == 0) putsh(r_full_scale,fp_output);
                        else putsh(norm,fp_output);
            }
        else /*if agcflag or no gain options*/
                        putsh(limit(R[i][j],r_full_scale),fp_output);
        }
        if (gainflag == 1)
        { scale=limit(sqrt((r_full_scale/255.0)*fscale),32767);
        putsh(scale,fp_output);
        }
        else if (agcflag == 1)
```

```
    putsh(agc[i],fp_output);
    else putsh(1,fp_output); /* output a 1 for the gain
                                    * if 'no gain' option
                                    */
}
fclose(fp_output);
return;
}
#define ZERO 0.7
preemp(s,framelength)
float s[]:
int framelength;
{
    int i;
    static int fopenflag = 0;
    static float x0, x1, output;
    static FILE *fp_precheck;
    /*
    if(fopenflag++ == 0)
        if((fp_precheck = fopen("PREcheck","w")) == NULW)
            ex("cannot create PREcheck");
    */
    for(i = NO_AUTOC; i < framelength + NO_AUTOC; i++)
    {
        x0 = s[i];
        s[i] = (x0 - ZERO*x1)/(1. + ZERO); /* DC gain = 1 */
        /* putsh((short)s[i],fp_precheck); */
        x1 = x0;
    }
}
#define ROOT2 1.414
#define A 0.99
do_agc(s,agc,framelength,row)
float s[POINTS];
int agc[MAX FRAMES],framelength,row;
{ int j.limit();
    float flimit(),fabs(),sqrt().sigma;
    static FILE *fp_agcout;
    static float out1,out2; /* out1 and out2 are initialized to 0.0
                        * first time 'do_agc()' is called.
                        */
if (row == 0)
    if ((fp_agcout = fopen("agc.out","w")) == NULL)
                    ex("cannot open 'agc.out' file");
```

```
for(j=NO_AUTOC;j<framelength+NO_AUTOC;j+++)
{ out1 = ALPHA*out1 + (1.0-ALPHA)*fabs(s[j]);
    out2 = ALPHA*out2 + (1.0-ALPHA)*out1;
}
```

/* The output of this $|()$.$| and LPF circuit is an estimate of the rms value$ * of the latest speech frame. (Actually, we must multiply the result by

* ROOT2 to get an estimate of sigma.)
* LPF should have the same impulse response as the window used in * autocorrelaton computation (impulse response of t.f. w/ two equal poles). */

```
sigma = R00T2 * out2;
```

agc[row] $=\operatorname{limit}\left(4^{*}\right.$ sigma, AD full scale);
if (agc[row $==0$ ) agc[row] $=1 ; /$ can't allow 0 as an agc value.
* agc $=0$ screws up synthesizer */
putsh(agc[row],fp_agcout);
printf("age output is \%d",age[row]);
for $(\mathrm{j}=\mathrm{NO}$ AUTOC; $\mathrm{j}<\mathrm{frameleng}$ th + NO_AUTOC $; \mathrm{j}++$ )
\{ $s[\bar{j}]=(\mathrm{s}[\mathrm{j}]$ * $A D$ full scale $) / \mathrm{agc}[\mathrm{row}]$;
if (clipflag $==1$ ) $s[j]=$ flimit( $s[j]$,(float) $A D$ full_scale);
putsh(limit( $\mathrm{s}[\mathrm{j}], A D$ full_scale), fp _scaled);
3
return:
1
instructions()
printf("usage: generateauto file \{-c\} \{-d dwnsamp\} \{-r frame_rate\}
$\{-\mathrm{s}$ samp_rate $\} \backslash n \backslash t \backslash t\{-\mathrm{g}\}\{-\mathrm{a}\}\{-\mathrm{k}\}\left\{(-\mathrm{q} q\right.$ bits $\}\{-\mathrm{p}\}\{-\mathrm{b}$ bits $\left.\} \backslash \mathrm{n} \backslash \mathrm{n}^{\prime \prime}\right) ;$
printf(" $\backslash t$ file must contain at least 500 samples of speech $\backslash n$ ");
printf(" $\backslash t-c:$ requests constant sampling rate to be used $\backslash n \backslash t \backslash t$
(output is in output1) $\mathbf{n n}^{\prime \prime}$ ):
printf(" $\backslash t-\mathrm{d}$ dwnsamp: sets down sampling rate for the last filter
section $\left(n^{\prime \prime}\right)$;
printf(" $\backslash t \backslash t$ (dwnsamp=2 means the sampling rate drops by a factor
of 2) $\mathrm{n}^{\prime \prime}$ );
printf(" $\backslash \mathbf{t} \backslash t$ (output is in output2) $\backslash n^{\prime \prime}$ );
printf(" $\backslash t-r$ frame rate: sets the rate at which the autocorrelation

printf(" $\backslash t$-s samp_rate: sets the sampling rate (Default is 8 k Hz ) $\backslash \mathrm{n}$ ");
printf(" $\backslash t$-g: causes program to output a scale factor after each
set $\backslash n \backslash t \backslash t o f$ autocorrelation values ( $R[0]=$ full scale $) \backslash n^{\prime \prime}$ );
printf(" $\backslash t$-a: causes an age circuit to pre-process the signal $\backslash n \backslash t \backslash t$
Value of gain is output every frame $\left.\backslash \mathbf{n}^{\prime \prime}\right)$ :
printf(" $\backslash t \backslash$ tage scaled time waveform is stored in file 'scaled' $\backslash n$ ");
printf("\t -k: stops clipping from occuring at output of age ckt. $\backslash n$ ");
printf(" $\backslash t-q$ q_bits: causes multiplication to be done with multiplier
\n\t\tquantized to q_bits (see comment below; keep q_bits <= 11) $\backslash n^{\prime \prime}$ );
printf(" $\backslash t-p$ : disables pre-emphasis $\backslash n$ ");
printf(" $\backslash t-b$ bits: sets $R[0]=2^{* *}$ bits when used with $-g$ option $\backslash n \backslash t$
TtProgram accepts $8<=$ bits $<=15$ nntt

```
    \t(default is bits=11 -> full scale=2047)\n");
    printf("\t Comment: 'bits' is the number bits used to store the\n\t
    \t results NOT INCLUDING the sign bit.\n");
    printf("\t Therefore, bits=8 allows numbers to range \n\t
    \tbetween -255 and +255\n");
    exit();
}
/* limit(x,max) takes inputs x (float) and max (int) and returns an integer
    * whose value is between -max and +max inclusive. This is a 'clipper' for x.
    *
limit(x,max_value)
float x;
int max_value;
{ int output;
    float fabs();
    if (fabs(x) > max_value)
    { /"printf("\nlimiting\t");*/
        return(output = sign(x)* max_value);
    }
    else return(output = x);
}
/* flimit(x,max) takes inputs x (float) and max (float) and returns an float
* whose value is between -max and +max inclusive. This is a 'clipper' for x.
*/
float flimit(x,max_value)
float x,max value;
{
    float fabs();
    if (fabs(x)> max value)
    { /*printf("\nlimiting\t");*/
        return(sign(x) * max_value);
    }
    else return(x);
}
/* mult( \(x, y, b i t s)\) does floating point multiplication. If asked, the function
* will quantize \(y\) and return the product.
*/
float mult( \(x, y, b i t s, l)\)
float \(x, y\);
int bits, \({ }^{1}\);
( float pow(),y quantized;
int quantize().power();
```

```
    if(quant_flag == 0) return(x*y);
    else
    { y_quantized = quantize(y,bits);
        **printf("y=%f\ty quantized=%f\n",y,y quantized); */
        if (l == 0) putsh((int)y_quantized,fp_quant);/* output quantized
                        * speech once only*/
        return(x * y_quantized);
}
}
/* quantize(y,b) takes y (float); clips it to AD_full scale; and then
* quantizes its value to b bits (not including sign). Returns an int.
* Quantization simulates an A/D converter (see t.f., pg. 106 of Analog
* Devices 'Analog to Digital Conversion Handbook')
*/
quantize(y,b)
int b;
float y;
{ float y temp,y_norm,flimit();
    int limit();
    y_temp = flimit(y,(float)AD_full scale); /* clip y */
    b=b + 1;
    y_temp = ((((int) (y_temp+(1<<(AD_BITS-b)))) >> ((AD_BITS+1)-b))
    << (AD BITS+1)-b); /* quantize to b bits */
    return(limit(y_temp,AD_full_scale)); /* clip y_temp */
}
/* round_off(x) takes x (float) and returns the integer closest to x
    */
round_off(x)
float x;
{
    return((int) (x+\operatorname{sign}(x)*0.5));
}
Abs(t)
int t;
{
    return(sign(t) * t);
}
/* power(a,b) is an integer version of pow(). Returns a to the b power.
    * a,b, and result are all integers.
    */
power(a,b)
int a,b;
{ int result = 1;
```

```
    while(b > 0)
    { result = a * result;
        b-;
    }
    return(result);
}
/* ex() prints a message, then exits. */
ex(str)
char *str;
{ printf("%s\n",str);
    exit();
}
/* sys_call(string,arg) does the following:
* char command[];
* sprintf(command,string,arg1,arg2,..);
* system(command);
*
* Only %s, %c, %d and %h are allowed in the string. %h is replaced
* with the user's home directory path. (i.e. HOME of 'printenv')
*/
#define MAX LINE 500
#define NULJ_CHAR '\0'
#define BLANK''
#define RETURN '\n'
sys_call(string,arg)
char string[MAX LINE].*arg;
{ char command[MAX_LNNE],*getenv(),**ptr;
        int i = 0;
        ptr = &arg;
        sprintf(command,"%c",BLANK);
        while( string[i] != NULL_CHAR )
            if( string[i] == '%' )
            { switch(string[++i])
            l case 's':
                sprintf(command,"%s%s",command,*(ptr++));
                    break;
                    case 'h':
                            sprintf(command,"%s%s",command,
                            getenv("HOME")):
                            break;
    case '%':
                                    sprintf(command,"%s%c",command,string[i]);
                                    break;
    case 'd':
```

```
                        sprintf(command,"%s%d",command,*(ptr++));
                        break;
                    default:
                                    sprintf(command,"unknown conversion type
                                    '%%%c'",string[i]);
                                    ex(command);
                                    break;
}
i++;
}
    else sprintf(command,"%s%c",command,string[i++]);
    system(command);
    return;
}
```


### 2.2. SPEAKPITCH.C

To synthesize speech which was analyzed by Generateauto.c, a simple direct-form LPC analyzer was written. All computations are floating point.

## SPEAKPITCH.c

\#define SOURCE "/brodersen/hurst/bin"
\#define PITCH_FILE "/brodersen/hurst/source/8msec_pitch"
\#ifdef M
\#undef SOURCE
\#define SOURCE "/mb/audio/hurst/bin"
\#undef PITCH FILE
\#define PITCH_FILE "/mb/audio/hurst/source/8msec_pitch"
\#endif
\#include <stdio.h>
\#include <sys/types.h>
\#include <sys/stat.h>
\#define NO_AUTOC 10
\#define NO POLES 9
\#define LOTS 2000
\#define UV 0 /* indicator variable-UV means unvoiced frame */
\#define V 1 /* indicator variable- V means voiced frame */
\#define MAX_24BITS 8388607 /* max value for a 24 bit integer:(2-23)-1 */
int frame_rate $=80$;
int samp freq $=8000$;
int floatflag $=1$; /* float version of Durbin's Recursion is default */
int pitchflag $=0$;
int gainflag $=0$;

```
int ageflag =0;
int unstableflag=1;
int deempllag =1;
int unstble frames=0;
char *pitch file;
struct stat stbuf;
/* This program is a refinement of Sammy Lum's Speak.c. It runs much faster.
*
* Autocorrelation data and pitch estimates are fed into this program to
* produce synthetic speech. The output speech is stored in a file.
*
* To compile: ce -O Speakpitch.c -lm -INS (VAX program)
*/
main(argc,argv)
int argc;
char **argv;
}
    int i, atoi();
        char *temp_file,*mktemp(),string[200];
    pitch_fle = PITCH_FILE;
if (argc == 1) instructions();
    if ((argv[1][0] == '-')| (argv[2][0] == '-'))
            ex("bad flle name");
    i=3;
    while (++i <= argc)
    { if (argv[i-1][0]!= ' -')
                                    ex("bad parameter");
        else switch(argv[i-1][1])
        { case 'r':frame_rate = atoi(argv[i++]);
                        break;
                        case 'f':floatflag = 1;
                        break;
                        case 'p':pitch_fle = argv[i++];
                        break;
                            case 'g':gainflag = 1;
                        break;
    case 'a':agcflag = 1;
                        break;
                        case 's':samp_freq = atoi(argv[i++]);
                        break;
                            case 'u':unstableflag = 0;
                        break,
                            case 'd':deempflag = 0;
                        break;
                            default: ex("bad parameter\n");
        }
            }
```

```
    if ((gainflag == 1)&&&(agcflag == 1))
            ex("can't use both -g and -a options");
if (filter(argv) < 0) ex(" ");
    if(deempflag == 1)
    {
        printf("DE-EMPHASIZING\n");
        sys_call("%s/deemp %s > %s".SOURCE,argv[2],
        temp_fle=mktemp("Spk_TemPXXXXXX"));
        print\overline{P("SCALNG\n");}
        sys_call("%s/scale %s %s;/bin/rm %s",SOURCE,
        temp_fle,argv[2],temp_fle);
    }
        if(deempflag == 0)
        printf("SCALING\n");
            sys_call("%s/scale %s %s",SOURCE,argv[2],
            temp_fle=mktemp("Spk TemPXXXXXX"));
            sys_call("/bin/mv -f %s %s',temp_file,argv[2]);
        }
```

    3
    instructions()
    \{ printf("usage: speakpitch file1 file2 \{-p file3\} \{-r autorate\}
        \(\{-\mathrm{s}\) samp freq \(\left.\}\{-\mathrm{f}\} \backslash \mathrm{n} \backslash \mathrm{t} \backslash \mathrm{t}\{-\mathrm{g}\}\{-\mathrm{a}\}\{-\mathrm{u}\}\{-\mathrm{d}\} \backslash \mathrm{n} \backslash \mathrm{n}^{\prime \prime}\right)\);
    printf("file1 should contain the autocorrelation values \(\backslash n\) ");
    printf("file2 will contain the output samples\n");
    printf("-p file3 should contain pitch information\n
        \(\backslash\) tdefault is a constant 8 msec pitch period \(\backslash \mathrm{n}^{\prime \prime}\) );
        printf("-r auto_rate is the frequency at which the autocorrelation
        In \tvalues were sampled (in Hz ); default is \(80 \mathrm{~Hz} \backslash \mathrm{n}^{\prime \prime}\) );
        printf("-s samp_freq is the sampling frequency (default is 8 kHz ) \(\backslash \mathrm{n}\) ");
        printf("-f flag causes Durbin's Recursion to be done in floating point \(\backslash n\) ");
        printf("-g causes program to read gain input from autocorrelation file \(\backslash n "\) ")
        printf("-a causes program to read agc gain from autocorrelation file \(\backslash n\) ");
        printf("-u causes program to terminate Durbin's recursion whenever \(\backslash n\)
        \t\ta reflection coeff. exceeds ONE\n");
        printf("-d turns off deemphasis \(\backslash n\) ");
        printf(" results are scaled and ready to output to the D/A converter
        in LSI \(\ n\) ");
        exit();
    3
    filter(argv)
    char *argv[]:
    (
        int fpe()
        int count,samples,framelength,atoi(),last frame;
    int \(\mathrm{i}, \mathrm{j}, \mathrm{k}, \mathrm{l}\), output, rows, poles, scale, scaleflag = 1,agc;
    long flesize, r[NO AUTOC]. overflow_count, pitch_period,r_full scale;
    float y[NO_AUTOC], a[NO_AUTOC], newa[NO_AUTOC], *x,gain, sqrt(), fabs(), magn, out,fscale,fagc;
float noise[LOTS], nat_excit[256], simple_excit[256],Gain,comp_gain();

```
FILE *fopen().*fp_auto,*fp_output,*fp_pitch,*fp_excitation;
    signal(8,&fpe); /* this is a function which allows programmer to jump
                    * to a subroutine when a floating point error occurs
                        */
if ((fp_excitation=fopen("excitation","w")) == NULL)
            ex("cannot create file 'excitation'");
if ((fp_auto=fopen(argv[1],"r")) == NULL)
    ex("cannot open file of autocorrelation data");
if ((fp_output = fopen(argv[2],"w")) == NUL)
    ex("can't create output file"):
    if ((fp_pitch = fopen(pitch_fle."r")) == NULL)
    ex("pitch file cannot be opened");
/* initialization */
    overflow_count = 0;
gain =0.0;
count =-1;
for ( }\textrm{i}=0;\textrm{i}<\mathrm{ NO_AUTOC; i++)
{y[i]=0.0;
    a[i] = 0.0;
    r[i] = 0;
    }
    a[0] = 1.0;
/* compute length of the file containing auto values */
    stat(argv[1],&estbuf);
    filesize = stbuf.st_size;
/* determine number of rows */
    framelength = samp_freq/frame_rate;
    printf("framelength=%d samples \t\tframe_rate=%d Hz\n",
    framelength,frame_rate);
rows = flesize/(2*(NŌ AUTOC + scaleflag));
printf("frames = %d\n",rows);
    /*set up arrays of excitations*/
    set_excit(noise,nat_excit,simple_excit,framelength);
/* BEGIN SYNTHESIS */
for (l=0; l<rows; 1++)
{ printf("frame %4d ",l+1);
```

```
for (i=0;i<NO_AUTOC;i++)
    r[i] = getsh(fp_auto); /* read in autocorrelation values */
if (gainflag == 1)
    ( fscale = getsh(fp_auto);
        if (fscale ==0.0) fscale = 1.0; /* can't have fscale==0 */
        if(l == 0) r_full_scale = r[0];
        fscale = fscale * sqrt(255.0/2047.0);/* scale factor */
        /*
        printf("fscale is %f\t",fscale):
        fscale = fscale * fscale * sqrt(r_full scale / 2047.0);
        printf("fscale is %f\n".fscale);
        */
    }
    else if (agcflag == 1)
                            fagc =0.0001 + (agc = getsh(fp_auto));
        else getsh(fp_auto); /* just skip over the scale factor
                        * (which is 1) if no gain option
```

* get pitch */
pitch_period=getsh(fp_pitch);
if (feof(fp_pitch) $!=0$ ) /*check for EOF in pitch file*/
\{ printf(" $\mathrm{In} \backslash$ npitch file $\%$ s is too small. Need at
least \%d pitch periods\n",pitch_file,rows);
return(-1);
\}
samples=(pitch_period * samp_freq)/10000; /* convert pitch period
* to \# of samples at sampling freq; pitch_period is in units of
* 0.1 msec (assumes pitch period is from Monte's bread-board or
* Herb's span program)
*/
printf("Pitch period is \%4.1fmsec $\backslash n$ ",pitch_period/10.0);
/*set $x$ to point to the start of the desired excitation array*/
if (samples >0)
( $\quad \mathbf{x}=$ nat excit; /* voiced */
if (last frame $==$ UV) count $=-1 ; / *$ reset count on a */
last frame $=\mathrm{V}$; /* uv/v transition */
3
else
( $x=$ noise; /*unvoiced*/
samples $=$ LOTS;
last_frame $=U V$;
\}
/* do durbin's recursion on new data. Use the new values
* obtained from durbin's recursion only if it works (i.e.
* number of poles $=9$ )
*/
if (floatflag $==1$ ) /*use floating point version*/

```
    { if ((poles=durbinf(r,newa,&ggain,0)) == NO_POLES)
                        for (i=0;i<NO_AUTOC;i++)
                a[i] = newa[i];
    3
    else /*use integer version*/
    ( if ((poles=durbin(r,newa,&gain,0,0)) == NO POLES)
        for (i=0;i<NO_AUTOC;i++)
                            a[i] = newa[i];
    }
    printf("gain = %7.3f poles = %d\n",Gain=
    comp_gain(gain,fagc,fscale),poles);
    /* compute flter outputs for a frame. Synthesis filter
        * has the form: y(n)=a[1]*y(n-1)+a[2]*y(n-2)+..+G*x(n).
    * y(n) {present output} is stored in y[0], y(n-1) is
    * in y[1],..etc. }x(n)=x[n]=excitation
    */
for ( k=0; k < framelength; k++)
{ if(count >= samples) count=0;
    else count++;
    for (i=1; i<NO AUTOC; i++)
        y[0] = a[i]*y[i] + y[0]; /*y[0] is the present output*/
    /* TESTING VAX random number generator */
            putsh((short)x[count],fp_excitation);
        y[0] = y[0] + x[count]*Gain/856.0;
        output = (out = y[0]*500.0);
        if((magn=fabs(out)) > 32767.0)
        { output = 32767.0 * out/magn;
            overflow_count++;
            printf("***overflow in computation. y[0]=%\n",out);
            }
        putsh(output,fp_output);
        for (j=0;j<NO POLES;j++) /*shift data*/
            y[NO_POLES-j] = y[NO_POLES-1-j];
        y[0] = 0.0;
3
}
fclose(fp_excitation);
fclose(fp_auto);
fclose(fp_output);
fclose(fp_pitch);
    if (overflow count != OL)
        printf("%ld overflows occured in the synthesis filter\n",
        overflow_count);
```

```
    if (unstble frames !=0)
        printf("%d unstable frames \ n',unstble_frames);
return(0);
}
set_excit(noise,nat excit, simple_excit,framelength)
float noise[LOTS], nat excit[256],simple_excit[256];
int framelength; /* Why is this arguement listed ? */
{ int i,rand(),Rand();
/* expected value of noise squared = 1791393 */
    for(i=0;i<LOTS;i++)
    noise[i] = (Rand(0) - 16383.5) * 0.02002;
/* this input waveform is not used in this version of Speakpitch.c */
/* energy in simple_excit = 1782150 */
        for(i=0;i<256;i++)
            simple excit[i] = 0;
            simple_excit[28] = -545;
            simple_excit[29]= 1090;
            simple_excit[30] = -545;
/* energy in nat excit = 1791393
                                    *
            nat excit[0] = 37;
        nat_excit[1] = 83;
        nat_excit[2]=96;
        nat_excit[3] = 107;
        nat_excit [4] = 76;
        nat_excit[5] = 84;
        nat_excit[6] = 90;
        nat_excit[7] = 77;
        nat_excit[8] = 89;
        nat excit[9] = 63;
        nat excit[10] = 80;
        nat_excit[11] = 62;
        nat_excit[12]= 64;
        nat_excit[13]=49;
        nat_excit[14]=44;
        nat excit[15] = -11;
        nat excit 16} = 9;
        nat_excit[17]=-65;
        nat excit[18] = -63;
        nat_excit 19] = -21;
        nat_excit[20] = -4;
        nat excit[21] = -43;
        nat_excit[22] = -159;
        nat_excit[23] = -239;
        nat excit[24] = -320;
        nat_excit[25] = -276;
        nat_excit[26] = -211;
```

```
        nat_excit[27] = -238;
        nat_excit[28] = 155;
        nat_excit[29] = 856;
        nat_excit[30] = -264;
        nat_excit[31] = -404;
        nat_excit[32] = 233;
        nat_excit[33] = -266;
        nat_excit[34] = 293;
        nat_excit[35] = -189;
        nat_excit[36]=177;
        nat_excit[37] = -131;
        nat_excit[38] = 105;
    nat_excit[39] = -134;
    nat_excit[40] = 109;
    nat excit[41] = -71;
    nat_excit[42] = 44;
for(i = 43;i<<56;i++)
    nat_excit[i] = 0;
return;
/* Rand() bridges the incompatability gap between the 11/40 and VAX. This * function returns a random number between 0 and 32767 on both machines. */
```

\& long roie;

```
#define MASK 0x00007fffL /* masks all but last 15 bits on a long integer */
```

\#define MASK 0x00007fffL /* masks all but last 15 bits on a long integer */
Rand(seed)
Rand(seed)
int seed;
int seed;
{ int rand(),noise; /* want 'noise' to be a positive random
{ int rand(),noise; /* want 'noise' to be a positive random
* number between 0 and 32767
* number between 0 and 32767
*/
*/
noise = (int) ((long)rand(seed) \& MASK);
noise = (int) ((long)rand(seed) \& MASK);
return(noise);
return(noise);
}
}
\#define MAX 32BITS ((1 << 31)-1)
\#define MAX 32BITS ((1 << 31)-1)
/* This function accepts 10 autocorrelation values as input and computes
/* This function accepts 10 autocorrelation values as input and computes
* the filter coefficients (the a(i)'s). */
* the filter coefficients (the a(i)'s). */
/* Blows up on frame 323 of 'gen audiocritic.t -a'
/* Blows up on frame 323 of 'gen audiocritic.t -a'
* Because of this, this function is no longer the default.
* Because of this, this function is no longer the default.
*/
*/
durbin(r,newa,gain,delta, shiftent)
durbin(r,newa,gain,delta, shiftent)
int delta,shiftent;
int delta,shiftent;
long r[NO AUTOC];
long r[NO AUTOC];
float newa[NO_AUTOC],*gain;
float newa[NO_AUTOC],*gain;
long a[NO_AUTOC][NO_AUTOC];

```
    long a[NO_AUTOC][NO_AUTOC];
```

```
        short i,j,k,poles,ONE,shiftflag;
        float g,sqrt(),newk[NO_POLES],pow();
        float tempsum,fabs();
/*printf("integer version of Durbin's Recursion\n");*/
    /* ONE = 16384; this works fine with long integers */
    ONE = 32767;
    shiftflag = 0;
    if(delta == 0) printf("R[0]=%5ld ".r[0]);
    else printf(" ");
    r0 = r[0];
    while(r0< (1<< 14))
    l r0=r0<< 1;
        shiftent++:
        shiftflag = 1;
}
if(shiftflag)
        for(i=0;i<NO_AUTOC;i++) /* minimize roundoff error */
            r[i] = r[i] << shiftent;
for(i=1;i<NO AUTOC;i++)
        newa[i]=0.0;
    newa[0] = 1.000;
    /*this is Durbin's recursion. See J.Makhoul paper. a[j][i]=(a sup j)sub i */
    r[0] = r[0] + delta; /*try to fix ill-conditioned matrix*/
    e=r[0];
    printf("R[0]=%5ld ",r[0]);
    if (e<= OL) i=1;
    else for(i=1;i<NO_AUTOC;i++)
    { tempsum = 0;
    for(j=1;j<=i-1;j++)
    { tempsum = tempsum + (int) (a[i-1][j] * r[i-j]);
    if(fabs(tempsum) > MAX 32BITS)
                                    fprintf(stderr,"TEMPSUM OVERFLOW %f",tempsum);
    }
    a[i][i] = ((r[i]*(long)ONE - tempsumm)/e);
    printf("K[%d]=%ld\t",i,a[i][i]):
    if ((a[i][i] >= ONE)|(a[i][i] <=-1*ONE))
        if (unstableflag ==1)
            { printf("refl. coeft >= ONE !! k[%d] = %7.2^n",
        i,a[i][i]/(float)ONE);
            if(delta == 0) unstble_frames++;
            if ((poles=durbin(r,newa,gain,compute_delta(r[0]),
```

```
            shiftent))==NO_POLES) return(poles);
                /* if ((poles=durbin(r,newa,&gain,compute_delta(r[0])
                shiftent))==NO POLES) return(poles); old line -
                wrong (I think) */
                    /* increment R[0] by .1% and redo durbin if unstable %
                        }
                        else {unstble_frames++; break;}
for(j=1;j<=i-1;j++)
{ a[i][j] =a[i-1][j]-((a[i][i] * a[i-1][i-j])/ONE);
    /*a[i][i] * a[i-1][i-j] overflows on frame 323*/
    printf("a[%d][%d] = %ld ",i,j,a[i][j]);
    if(abs(a[i][j]) > MAX_24BITS)
    { fprintf(stderr,"a[%d][%d] = %ld\n",i,j, a[i][j]);
                                    fprintf(stderr,"~ a[][] exceeds 24 bits!! \n");
    }
3
/*e = ((ONE - ((a[i][i] * a[i][i])/ONE))*e)/ONE; */
/*e=(((ONE *(long)ONE - a[i][i] *a[i][i])/ONE)*e)/ONE; */
e=e-(int) (a[i][i]*a[i][i]/ONE)*e/ONE;/* has the nice
feature that e >= (theoretical value of e) */
if (e== 0) { fprintf(stderr,"e == 0\n");e = 1;}
}
    poles = i-1;
    if (poles < NO_POLES) return(poles); /* don't compute a new gain value wih
                            * bad data--just return and use old data*/
for(j=1;j<=poles;j++)
{
    newa[j] = a[poles][j]/((float)ONE);
    if(delta != 0)
    printf("newa[%d] = %f ",j,newa[j]);
    newk[j-1] = a[j][j]/((float)ONE);
    if(delta!= 0)
        printf("newk[%d] = %f ".j-1,newk[j-1]);
}
/* note that lpc_gain-2 = lpc_error */
/* note: If R[0] has been incremented a number of times, R[0] and
    * therefore e are too large -> gain is too large.
    */
*gain = sqrt((float)e/pow(2.0,(float)shiftent));
/* scale gain to undo '<< shiftent' above */
    return(poles);
}
old_durbin(r,newa,gain,delta)
int delta;
long r[NO_AUTOC];
float newa[NO_AUTOC],*gain;
```

```
\{ long a[NO_AUTOC][NO_AUTOC], e,tempsum;
    int \(\mathrm{i}, \mathrm{j}, \mathrm{k}\), poles, ONE ;
    float g.sqrt();
\(/\) "printf("integer version of Durbin's Recursion \(\backslash n\) ");*/
    \(\mathrm{ONE}=10000 ;\)
    for \((\mathrm{i}=1 ; \mathrm{i}<\mathrm{NO}\) AUTOC \(; \mathrm{i}++\) )
        newa \([i]=0.0\);
    newa[0] = 1.000;
    /*this is Durbin's recursion. See J.Makhoul paper. a[j][i]=(a sup j)sub i */
        \(r[0]=r[0]+\) delta; /*try to fix ill-conditioned matrix*/
    \(\mathrm{e}=\mathrm{r}[0] ;\)
    printf("R[0]=\%5ld ",e);
    if ( \(\mathrm{e}<=0 \mathrm{~L}\) ) \(\mathrm{i}=1\);
    else for ( \(\mathrm{i}=1\); i <NO_AUTOC; \(\mathrm{i}++\) )
    \{ tempsum \(=0\);
    for \((j=1 ; j<=i-1 ; j++)\)
            tempsum \(=\) tempsum \(+(a[i-1][j] * r[i-j])\);
        \(a[i][i]=(r[i] * O N E-\) tempsum \() / e ;\)
        /"printf("k[i]=\%ld t ", a[i][i]):*/
        if ( \((a[i][i]>=0 N E) \|(a[i][i]<=-1 * O N E))\)
        if (unstableflag \(==1\) )
        \{ printf("refl. coeff >= ONE !! k[\%d] = \%ld \(\backslash n ", i, a[i][i]) ;\)
            if(delta \(==0\) ) unstble frames ++ ;
                if ((poles=old durbin(r,newa, \&gain, compute_delta (r[\$]
                    \(==\) NO POLES) return(poles);
                        \(/ *\) increment \(R[0]\) by \(.1 \%\) and redo durbin if unstable \(\neq\)
            3
            else \{unstbleframes++; break; \(\}\)
        for \((\mathrm{j}=1 ; \mathrm{j}<=\mathrm{i}-1 ; \mathrm{j}++\) )
            \(a[i][j]=a[i-1][j]-((a[i][i] * a[i-1][i-j]) / O N E) ;\)
        \(e=((\) ONE \(-((a[i][i] * a[i][i]) / O N E)) * e) / O N E ;\)
        if \((e==0 L) e=1 L ;\)
    3
    poles \(=\mathrm{i}-1\);
    if (poles < NO_POLES) return(poles):/* don't compute a new gain value wib
                            * bad data--just return and use old data*/
    \(\mathrm{g}=0.0 ;\)
    for \((\mathrm{j}=1 ; \mathrm{j}<=\) poles \(; \mathrm{j}++\) )
    \(\}\)
```

```
    newa[j] = a[poles][j]/10000.0;
    g = g-newa[j] * r[j];
}
    g=g+r[0];
    if (g<0.0)g=0.0;
    *gain = sqrt(g);
    return(poles);
}
#define fepsilon 0.00001
durbinf(r,newa,gain,delta)
int delta;
long r[NO_AUTOC];
float newa[NO_AUTOC],*gain;
\{ float a[NO_AUTOC][NO_AUTOC],e,tempsum,ONE; int \(\mathrm{i}, \mathrm{j}, \mathrm{k}\), poles; float g.sqrt();
```


## /*printf("float version of Durbin's Recursion\n");"/

```
\(\mathrm{ONE}=1.0000 ;\)
for \((i=1 ; i<N O\) AUTOC \(; i++\) )
newa[i] \(=0.0\);
newa[0] = 1.000;
/*this is Durbin's recursion. See J.Makhoul paper. a[j][i]=(a sup j)sub \(i\) */ \(r[0]=r[0]+\) delta;
\(\mathrm{e}=\mathrm{r}[0]\);
printf("R \([0]=\% 5.0 f \quad\) ",e);
if \((r[0]<=0 \mathrm{~L}) \mathrm{i}=1\);
else for ( \(\mathrm{i}=1 ; \mathrm{i}<\mathrm{NO}\) AUTOC \(; \mathrm{i}++\) )
( tempsum =0;
for \((j=1 ; j<=i-1 ; j++)\)
tempsum \(=\) tempsum \(+(a[i-1][j] * r[i-j]) ;\)
\(a[i][i]=(r[i] * O N E-\) tempsum \() / e ;\)
if ( \((a[i][i]>=0 N E) \|(a[i][i]<=-1 * O N E))\)
if (unstableflag \(==1\) )
\{ printf("refl. coeff \(>=0 \mathrm{NE}!\mathrm{l} \mathrm{k}[\% \mathrm{~d}]=\% \mathrm{f} \backslash \mathrm{n} ", \mathrm{i}, a[\mathrm{i}][\mathrm{i}])\); if (delta \(==0\) ) unstble frames++; delta = compute_delta(r[0]);
\(/\) *if ((poles=durbinf(r,newa, \&gain, delta)) \(==\) NO_POLES \()\) old line of code - wrong (I think) */ if ((poles=durbinf( \(r\), newa, gain, delta \())==\) NO_POLES \()\)
```

```
            return(poles);
            }
            else {unstble_frames++; break;}
for(j=1;j<=i-1;j++)
            a[i][j] = a[i-1][j]-((a[i][i] *a[i-1][i-j])/ONE);
    e=((ONE - ((a[i][i] *a[i][i])/ONE)) *e)/ONE;
    /* if (e == 0L) e = 1L; */
    }
    poles = i-1;
    if (poles < NO_POLES) return(poles);
    g = 0.0;
    for(j=1;j<=poles;j++)
    {
        newa[j] = a[poles][j]/1.0000;
        g = g-newa[j] * r[j];
    }
    g=g+r[0];
    if (g<0.0)g=0.0;
    *gain = sqrt(g);
    return(poles);
}
compute_delta(RO)
long RO;
{ int delta;
    delta = 0.001*RO;
    if (delta == 0) delta = 1;
    return(delta);
}
ex(str)
char *str;
{ printf("%s \n",str);
    exit();
}
float comp_gain(gain,fagc,fscale)
float gain,fagc,fscale;
{
}
    if (gainflag == 1) return(gain/fscale);
    else if (agcflag == 1) return(gain*fagc/800.0);/*800 is the magic */
        else return(gain); /* number which gives #/
/* floating point error causes a jump to this function */
```

```
fpe()
{ printf("Floating point error\n");
    /*printf("Gain=%^nCount=%d\nOutputn-1=%\nOutputn=%f\n\n",Gain,
    Count,Outputn_1,Outputn);
    printf("Fagc=%f\nFscale=%f\n\n",Fagc,Fscale);
    */
    ex('"');
}
#define MAX LINE 500
#define NULL CHAR' '
#define BLANK',
#define RETURN '\n'
sys_call(string.arg)
char string[MAX LINE],*arg;
{ char command[MAX LLNE],*getenv().**ptr;
    int i;
    ptr = &&arg;
    sprintf(command,"%c",BLANK);
    i=0;
    while( string[i] != NULL_CHAR )
    if( string[i] == '%' )
        { switch(string[++i])
        { case 's':
                                    sprintf(command,"%s%s",command,*(ptr++));
                                    break;
        case 'h':
                            sprintf(command,"%s%s",command,
                        getenv("HOME"));
                            break;
        case '%':
                            sprintf(command,"%s%c",command,string[i]);
                            break;
        case 'd':
                                    sprintf(command,"%s%d",command,*(ptr++));
                                    break;
                                    default:
                                    sprintf(command,"unknown conversion type
                                    '%%%c'",string[i]);
                                    ex(command);
                                    break;
            i++;
            }
            else sprintf(command,"%s%c",command,string[i++]);
    system(command);
    return;
```

Pitch information is required to synthesize speech. To determine the pitch for the synthesized speech, a modifled Gold-Rabiner pitch tracker was used [ 20]. The source code for this program is not included here.

### 2.3. SPEC_DEV.C

To quantify errors due to the various system modifications, an ItakuraSaito spectral distance measure was employed (equation 2.15) . The program spec_dev.c takes two sets of autocorrelation values and computes the spectral distance between them. In the simulations of chapter 4, one set of autocorrelation values was computed with high accuracy (no modifications), and the other set was computed with one or more modifications in effect. The spectral distance measured is referred to as a spectral deviation since it is the distance measured from a very accurate, reference frame.

SPEC_DEV.c:

```
#include <stdio.h>
#ifdef FORTY
#include "/usr/audio/hurst/source/NAX_header
#endif
#define NO POLES 9
#define NO_AUTOC 10
#define OUT SCALE 100
#define MAX SHORT 32767
#define ERROR_FLAG -1000/* number to output in place of rms_error if
                                    * an unstable frame is encountered
                                    */
```

int scaleflag $=1$;
int unstableflag $=0$; / causes durbinx() to terminate on an unstable $k$ \%/ int unstble frames:
int quant type $=0 ; /=0->$ use floating point arithmetic */
$/ * 1->$ use long arithmetic */
/* 2 -> use 16 bit integers wherever possible */

```
main(argc,argv)
int argc;
char **argv;
{
    /* short durbinsh(),durbinl(),durbinf(); */
    int atoi(),i,j, frame=0;
    long r[NO_AUTOC],r_ref[NO_AUTOC];
    float a[NO_AUTOC], a_ref[NO_AUTOC],gain,rms_error,numer,spec_dev;
    float durbinf(), error(), log();
    FILE *fopen()."fp_ref_auto,*fp_other_auto, *fp_error;
    if(arge == 1)
    ex("usage: spec_dev ref other [-fis] \n\t-f is the default");
    i=3;
    while(++i <= argc)
    { if (argv[i-1][0]!= '-')
        ex ("bad parameter");
    else switch(argv[i-1][1])
    { case 'f': quant_type = 0; /* use durbinf() */
                break,
            case 'l': quant_type = 1; /* use durbinl() */
                break,
            case 's': quant_type = 2; /* use durbinsh() */
                break;
            default: ex("bad parameter");
    }
}
if((fp_ref auto=fopen(argv[1],"r")) == NULL)
    ex("input flle does not exist");
if((fp_other_auto=fopen(argv[2],"r")) == NULL)
    ex("input fle does not exist");
if((fp_error=fopen("dev"."w')) == NULL)
    ex("cannot create 'dev' ");
while(1)
{
    for(j=0;j<NO_AUTOC;j++)
    { rref[j] = getsh(fp_ref_auto);
            r[j] = getsh(fp_other_auto):
            if(feof(fpref auto) == 1)
                if(j)!=\overline{0}) ex("bad data count in input fle");
                else exit(0);
            if(feof(fp_other_auto) == 1)
                        ex("bad file size in other");
    }
    if(scaleflag == 1) getsh(fp_ref_auto); /* skip gain value */
    if(scaleflag == 1) getsh(fp_other_auto); /* skip gain value */
    rms_error = durbinf(r_ref,a_ref,&gain,0); /* !! not NORMALIZED !! */
```

```
if(durbinf(r,a,\&gain, 0) < 0) /* durbinf failed */
        numer \(=-10 ; / *\) indicates error */
else numer = error(r_ref,a); /* !! not NORMALIZED !! */
if(rms_error \(<=0\) )
        spec_dev = -(float) (MAX_SHORT / OUT_SCALE);
        * indicates an unstable frame in reference data */
else if(numer \(<=0\) )
            spec_dev \(=\) (float) \((\) MAX SHORT / OUT_SCALE);
            **indicates an unstable frame in other data */
        else spec_dev \(=4.343^{*} \log\) (numer / rms_error);
printf("frame \%3d spec_dev = \%f db\n",++frame,spec_dev);
/* printf("normalized rms error \(=\) \%f for frame \%dVn",
(rms_error * MAX SHORT /r[0]), ++frame);*/
/* output spectral deviation in units of 0.01 db
    */
putsh((short) (spec_dev * OUT_SCALE),fp_error):
/* This function accepts 10 autocorrelation values as input and computes
* the filter coefficients (the a(i)'s). */
```

3
3
short durbinsh(r,newk,gain, delta)

## int delta;

long r[NO AUTOC]: /* ?? could be a short since R[0] <= 2047 */ float newk[NO POLES], *gain;
\{ long a[NO_AUTOC][NO_AUTOC],tempsum; /* e could be a short since * $e<=R[0]$. tempsum must

* be a long. a[][] is up
* in the air. See td results
* for limits on a[][]'s
*/
short i,j,k,e,r_sh[NO_AUTOC],r_scale,poles, ONE:
float g,sqrt(),newa[NO_AUTOC]; /* God forbid we should really need * a float. Better check this out.
*/
/"printf("integer version of Durbin's Recursion $\backslash n "$ ");*/
ONE = 32767; /* Different value for ONE results in different rms_error */
$r$ scale $=$ ONE $/ r[0] ;$
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{NO}$ AUTOC; $\mathrm{i}++$ )
$r_{\text {_sh }}[i]=r[i]$ * r_scale;
$r[0]=r$ sh[0]; /* return r_sh[0] for proper scaling in print in main */

```
for \((i=1 ; i<N O A U T O C ; i++)\)
    newa \([\mathrm{i}]=0.0\);
newa[0] \(=1.000 ;\)
```

/*this is Durbin's recursion. See J.Makhoul paper. a[j][i]=(a sup j)sub i */ $r \_\operatorname{sh}[0]=r \_s h[0]+$ delta; /*try to fix ill-conditioned matrix*/
$e=r \_s h[0] ;$
/* printf("R[0]=\%5d ",e); */
if $(\mathrm{e}<=0 \mathrm{~L}) \mathrm{i}=1$;
else for $(\mathrm{i}=1 ; \mathrm{i}<\mathrm{NO}$ AUTOC $; \mathrm{i}++$ )
\{ tempsum $=0$;
for $(j=1 ; j<=i-1 ; j++$ )
tempsum $=$ tempsum $+(a[i-1][j] * r \operatorname{sh}[i-j])$;
$a[i][i]=(r \operatorname{sh}[i] *($ long $)$ ONE - tempsum $) / e ;$
printf("k[\%d]=\%กt",i,a[i][i]/((foat) ONE));
if ( $\mathrm{a}[\mathrm{i}][\mathrm{i}]>=0 \mathrm{ONE}) \|(\mathrm{a}[\mathrm{i}][\mathrm{i}]<=-1 * \mathrm{ONE})$ )
if (unstableflag $==1$ )
\{ printf("refl. coeff $>=$ ONE !! $\mathrm{k}[\% \mathrm{~d}]=\% 7.2 \wedge \mathrm{n} "$,
i,a[i][i]/(float)ONE);
if (delta $==0$ ) unstble frames++;
if ((poles=durbinsh(r,newk,\&gain,compute_delta(r[0])))
$==$ NO POLES) return((short) e);
$/$ *increment $\mathrm{R}[0]$ by $.1 \%$ and redo durbin if unstable*/
3
else \{ unstble_frames++; break;\}
for $(j=1 ; j<=i-1 ; j++)$
$a[\mathrm{i}][\mathrm{j}]=\mathrm{a}[\mathrm{i}-1][\mathrm{j}]-((\mathrm{a}[\mathrm{i}][\mathrm{i}] * a[\mathrm{i}-1][\mathrm{i}-\mathrm{j}]) / \mathrm{ONE})$;
$/ * e=\left((\mathrm{ONE}-((a[\mathrm{i}][\mathrm{i}] * a[i][\mathrm{i}]) / \mathrm{ONE}))^{*} e\right) / \mathrm{ONE} ; * /$
$e=((($ ONE $*$ (long $) \mathrm{ONE}-\mathrm{a}[\mathrm{i}][\mathrm{i}] * a[\mathrm{i}][\mathrm{i}]) / \mathrm{ONE}) * e) / \mathrm{ONE} ;$
if $(e=0) e=1$;
\}
poles $=\mathrm{i}-1$;
if (poles < NO_POLES) return(ERROR_FLAG);/* don't compute a new gain
* value with bad data-just return and use old data*/
$\mathrm{g}=0.0 ;$
for $(\mathrm{j}=1 ; \mathrm{j}<=$ poles; $\mathrm{j}++$ )
\{
newa[j] = a[poles][j]/((float)ONE);
newk[j-1] =a[j][j]/((foat)ONE);
$\mathrm{g}=\mathrm{g}-\mathrm{newa}[\mathrm{j}] \mathrm{r}_{\mathrm{c}} \mathrm{sh}[\mathrm{j}]$;

```
    g=g+r_sh[0]:
    /* just found out (should have known) that g = e */
    /* printf("g = %\te = %d\t",g,e); */
    if (g<0.0)g=0.0;
    *gain = sqrt(g);
    return((short) e);
}
```

/* This function accepts 10 autocorrelation values as input and computes

* the filter coefficients (the a(i)'s). */
short durbinl(r,newk,gain,delta)
int delta;
long r[NO AUTOC]; /* ?? could be a short since $R[0]<=2047$ */
float newk[NO POLES],*gain;
\{ long a[NO_AUTOC][NO_AUTOC], e,tempsum; /* e could be a short since
*e <= R[0]. tempsum must
* be a long. a[][] is up
* in the air. See td results
* for limits on a[][] 's
*/
int $\mathrm{i}, \mathrm{j}, \mathrm{k}$, poles, $\mathrm{ONE} ; /$ / On the VAX, these are the same as longs.
* Change to shorts wherever possible.
*/
float g.sqrt(),newa[NO_AUTOC]; /* God forbid we should really need * a float. Better check this out. */
/"printf("integer version of Durbin's Recursion\n"):*/
ONE $=10000 ;$
for $(\mathrm{i}=1$; $\mathrm{i}<\mathrm{NO}$ AUTOC $; \mathrm{i}++$ )
newa $[\bar{i}]=0.0$;
newa[0] = 1.000;
/*this is Durbin's recursion. See J.Makhoul paper. a[j][i]=(a sup j)sub i */ $r[0]=r[0]+$ delta; /*try to fix ill-conditioned matrix*/
$\mathrm{e}=\mathrm{r}[0]$;
/* printf("R[0]=\%5ld ".e); */
if $(e<=O L) ~ i=1$;
else for ( $\mathrm{i}=1$; $\mathrm{i}<\mathrm{NO}$ AUTOC $; i++$ )
\{ tempsum $=0$;
for $(j=1 ; j<=i-1 ; j++)$
tempsum $=$ tempsum $+(a[i-1][j] * r[i-j]) ;$

```
    \(\mathrm{a}[\mathrm{i}][\mathrm{i}]=(\mathrm{r}[\mathrm{i}] * \mathrm{ONE}-\) tempsum \() / \mathrm{e}\);
    printf("k[i]=\%^t",a[i][i]/((float) ONE));
    if ((a[i][i] >= ONE) \| (a[i][i] <=-1*ONE))
        if (unstableflag \(==1\) )
        \{ printf("refl coeff >= ONE !! k[\%d] = \%7.2^n",
            i, a[i][i]/(float)ONE):
            if(delta \(==0\) ) unstble_frames++;
            if ((poles=durbinl(r,newk, \&gain, compute_delta(r[0])))
            \(==\) NO POLES \()\) return((short) e); /* increment R[0]
            by \(.1 \%\) and redo durbin if unstable */
    1
        else \{unstble_frames++; break; \}
    for \((\mathrm{j}=1 ; \mathrm{j}<=\mathrm{i}-1 ; \mathrm{j}++\) )
    \(a[i][j]=a[i-1][j]-((a[i][i] * a[i-1][i-j]) / O N E) ;\)
    \(e=((\) ONE \(-((a[i][i] * a[i][i]) / O N E)) * e) / O N E ;\)
    if \((e==0 L) e=1 L ;\)
    3
    poles \(=\mathrm{i}-1\);
    if (poles < NO_POLES) return(ERROR_FLAG);/* don't compute a new gain vt
                * bad data--just return and use old data*/
    \(\mathrm{g}=0.0 ;\)
    for \((\mathrm{j}=1 ; \mathrm{j}<=\) poles \(; \mathrm{j}++\) )
\}
    newa[j] = a[poles][j]/((float)ONE):
    newk \([j-1]=a[j][j] /(\) (foat \() 0 N E)\);
    \(\mathrm{g}=\mathrm{g}-\) newa \([\mathrm{j}] * \mathrm{r}[\mathrm{j}]\);
    3
\(g=g+r[0] ;\)
if \((g<0.0) \mathrm{g}=0.0\);
*gain = sqrt (g):
return((short) e);
3
\#define fepsilon 0.00001
float durbinf(r,newa,gain,delta)
int delta;
long r[NO AUTOC];
float newa[NO AUTOC].*gain;
\{ double a[NO_AUTOC][NO_AUTOC],e,tempsum,ONE;
int \(\mathrm{i}, \mathrm{j}, \mathrm{k}\), poles;
double g,newk[NO POLES];
float sqrt();
```

```
/"printf("float version of Durbin's Recursion\n");"/
\(\mathrm{ONE}=1.0000 ;\)
for \((\mathrm{i}=1 ; \mathrm{i}<\mathrm{NO}\) AUTOC \(; i++\) )
    newa \([\mathrm{i}]=0.0\);
newa[0] \(=1.000 ;\)
/*this is Durbin's recursion. See J. Makhoul paper. a[j][i]=(a sup j)subi*/
\(r[0]=r[0]+\) delta;
\(\mathrm{e}=\mathrm{r}[0]\);
/*printf("R[0]=\%6.0f ".e); */
if ( \(\mathrm{r}[0]<=0 \mathrm{~L}\) ) \(\mathrm{i}=1\);
else for \((\mathrm{i}=1 ; \mathrm{i}<\mathrm{NO}\) AUTOC \(; \mathrm{i}++\) )
\{ tempsum \(=0\);
    \(\operatorname{for}(j=1 ; j<=i-1 ; j++)\)
        tempsum \(=\) tempsum \(+(a[i-1][j] * r[i-j])\);
    \(a[i][i]=(r[i] * 0 N E-\) tempsum \() / e ;\)
    /* printf("k[\%d]=\%へt",i,a[i][i]); */
    if \(((a[i][i]>=0 N E) \|(a[i][i]<=-1 * O N E))\)
        if (unstableflag \(==1\) )
        \{ printf("refl. coeff \(>=0 \mathrm{NE}!!\mathrm{k}[\% \mathrm{~d}]=\% \mathrm{f} \backslash \mathrm{n} ", \mathrm{i}, a[\mathrm{i}][\mathrm{i}])\);
                        if (delta \(==0\) ) unstble frames++;
                delta \(=\) compute_delta(r \([0]\) );
                if \((\) (poles=durbinf( \(r\), newa, \&egain,delta \())==\) NO_POLES \()\)
                        return(e);
        3
        else \{unstble_frames++; break; \}
        for \((\mathrm{j}=1 ; \mathrm{j}<=\mathrm{i}-1 ; \mathrm{j}++\) )
        \(a[i][j]=a[i-1][j]-((a[i][i] * a[i-1][i-j]) / O N E) ;\)
        \(e=((\mathrm{ONE}-((\mathrm{a}[\mathrm{i}][\mathrm{i}] * a[\mathrm{i}][\mathrm{i}]) / \mathrm{ONE})) * e) / \mathrm{ONE} ;\)
        \(/ *\) if \((e==0 L) e=1 L ; *)\)
1
poles \(=\mathrm{i}-1\);
if (poles < NO POLES) return((float)ERROR_FLAG);
\(\mathrm{g}=0.0 ;\)
for \((\mathrm{j}=1 ; \mathrm{j}<=\) poles \(; \mathrm{j}++\) )
\{
        newa[j] = -a[poles][j]/ONE; /* fixing sign for error() */
        newk \([j-1]=a[j][j] / 0 N E ;\)
        \(\mathrm{g}=\mathrm{g}\)-newa[j] *r[j];
```

    g=g+r[0]:
    if (g<0.0) g=0.0;
    *gain = sqrt(g);
    return(e);
    }
compute_delta(RO)
long RO;
{ int delta;
delta = 0.001*RO;
if (delta == 0) delta = 1;
return(delta);
}
float error(r,a)
long r[];
float a[];
{
int j:
float err = 0.0;
float R(),B();
for (j= -NO POLES;j<=NO POLES;j++)
err =err + B(j,a) *R(j,r);
return(err);
}
/* R(j,.) returns autocorrelation value of input. Function is necessary
* because error() uses R(j..) and R(-j..)
*/
float R(j,r)
long r[];
int j;
{
if(j<0) j=-1 * j;
return((float)r[j]);
}
$/^{*} \mathrm{~B}(\mathrm{j}, \mathrm{a})$ computes autocorrelation values for the LPC coeffs. Reference is

* G. White paper (Xerox PARC) 'Automatic Speech Recognition, LPC Residual
    * vs. BP Filtering
* 

float B(j, a)
float a[]:
int $j$;
\{
int $i_{i}$
float $\mathrm{b}=0.0$;

```
```

    if(j<0) j = -1 * j;
    for(i=0;i<=(NO POLESS - j);i++)
        b=b+a[i] *a[i+j];
    return(b);
    }
ex(str)
char *str;
{ fprintf(stderr,"%s \n",str);
exit();
}

```

\section*{APPENDIX D}

\section*{THE CMOS PROCESS SCHEDULE}

The process schedule for the high voltage metal-gate CMOS process which was used to integrate the autocorrelator is presented here. This process is a modified version of the CMOS process used by Black [ 28 ]. More information on the process and layout rules can be found in [ 14 ].

This process uses positive photo-resist throughout. Alignment was done with a projection aligner to \(\sim 1 \mu \mathrm{~m}\) precision. The p-channel devices were self aligned by an implant over the metal. The aluminum gates were used as the mask and the sintering step activated the implant.

\section*{Berkeley Metal Gate CMOS Process}

November 18, 1981 (rev. March 5 1982)
1. Initial wafer cleaning - p-type, 5-7 ohm-cm, <100>
a. TCE clean, \(60^{\circ} \mathrm{C}, 10\) minutes (Degrease) (Watch temperature : Boiling TCE will shatter wafers)
b. Dip in acetone
c. Dip in methyl alcohol
d. Rinse in De-ionized (DI) water
e. Piranha etch \(\left(\mathrm{H}_{2} \mathrm{SO}_{4}: \mathrm{H}_{2} \mathrm{O}_{2}-5: 1\right)\) for 10 min .
f. Rinse thoroughly in running DI water
g. Dip in \(\mathrm{HF}: \mathrm{H}_{2} \mathrm{O}(1: 10)\) for 20 seconds
h. Rinse in DI water
i. Blow dry
j. Inspect under collimated light for dust. (If dust remains, repeat from \(h\).; if that doesn't work, repeat from a.)
2. Initial oxidation - 4000A, Initial Oxide Furnace
a. Wet \(O_{2}, 1100^{\circ} \mathrm{C}, 27 \mathrm{~min}(.4 \mu \mathrm{~m})\) (temperature setting \(=1095^{\circ} \mathrm{C}\) )
b. Dry \(N_{2}\) (anneal), \(900^{\circ} \mathrm{C}, 20 \mathrm{~min}\).
3. Positive Photoresist (PR) Step, Mask \#1 : N- well mask.
a. Prebake, \(85-90^{\circ} \mathrm{C}, 15 \mathrm{~min}\). (if wafer just came from furnace then skip prebake)
b. HMDS treatment
1. \(N_{2}\) purge, 10 min .
2. Load wafers
3. Bubble HMDS, 3 min.
4. \(N_{2}\) purge, 5 min .
c. Spin AZ 1450J, \(6000 \mathrm{rpm}, 30\) seconds. (PR thickness \(=1.4 \mu \mathrm{~m}\) )
d. Softbake, \(85-90^{\circ} \mathrm{C}, 15-20 \mathrm{~min}\).
e. Align and expose (Blow off dust on top and bottom)
f. Develop, AZ 351 developer (DI \(\mathrm{H}_{2} \mathrm{O}\) :Developer - 5:1), 1 min . (or regular AZ developer at 1:1 dilution)
g. Rinse in DI water and blow dry
h. Inspect
i. Hardbake, \(110-120^{\circ} \mathrm{C}, 20 \mathrm{~min}\).
j. Oxide etch, buffered \(H F\left(\mathrm{NH}_{4} \mathrm{~F}: H F-5: 1\right)\) etch rate \(.12 \mu \mathrm{~m} / \mathrm{min}\). ( \(.145 \mu \mathrm{~m} / \mathrm{min}\) if solution is just made) (etch time \(=3.5-4 \mathrm{~min}\). with \(15 \%\) over etch) (prepare at least 4 hours before use)
k. PR strip, acetone, 15 min .
l. Piranha clean, \(\mathrm{H}_{2} \mathrm{SO}_{4}: \mathrm{H}_{2} \mathrm{O}_{2}-5: 1,15 \mathrm{~min}\).
4. Implant step - Initial Oxide Furnace
a. Grow implant oxide - 290A
1. Wet \(\mathrm{O}_{2}, 900^{\circ} \mathrm{C}, 3 \mathrm{~min}\)., flowmeter setting \(=4 \mathrm{~cm}\)
2. Dry \(N_{2}, 900^{\circ} \mathrm{C}, 5 \mathrm{~min}\), flowmeter setting \(=4 \mathrm{~cm}\)
b. Implant Phosphorus ( N -), Dose \(=1 x 10^{19}\). 200 keV ( \(\mathrm{xj}(\) well \()=.462 \mu \mathrm{~m}\), Rsh=1.29kohm/square)
5. Piranha Clean, \(\mathrm{H}_{2} \mathrm{SO}_{4}: \mathrm{H}_{2} \mathrm{O}_{2}-5: 1,5 \mathrm{~min}\).
6. Well oxidation-7229A, Initial Oxide Furnace
a. Wet \(O_{2}, 1150^{\circ} \mathrm{C}, 65 \mathrm{~min},(.76 / .92 \mu \mathrm{~m})\) (setting=1144)
b. Dry \(N_{2}, 900^{\circ} \mathrm{C}, 30 \mathrm{~min}\). \(\mathrm{xj}(\) well \()=1.978 \mu \mathrm{~m}\), Rsh=943 ohms/square)
7. Well drive-in, Arsenic Furnace
a. Dry \(N_{2}, 1200^{\circ} \mathrm{C}, 24\) hours
b. Dry \(N_{z}\) (anneal), \(900{ }^{\circ} \mathrm{C}, 60 \mathrm{~min} . \quad(\mathrm{xj}(\) well \()=9.055 \mu \mathrm{~m}, \quad\) Rsh \(=827\) ohms/square)
8. Pos. PR Step, Mask \#2 : N+ (N channel S/D) mask.
a. Apply photoresist, expose, develop (follow 3.a-i)
b. Oxide etch, buffered \(H F\left(N H_{4} F: H F-5: 1\right)\) etch rate \(.115 \mu \mathrm{~m} / \mathrm{min}\) (etch time \(=7.5 \mathrm{~min}\).)
c. PR strip
d. Piranha clean, 15 min .
9. Implant step - Initial Oxide Furnace
a. Grow implant oxide -290A
1. Wet \(\mathrm{O}_{2}, 900^{\circ} \mathrm{C}, 3 \mathrm{~min}\).
2. Dry \(N_{2}, 900^{\circ} \mathrm{C}, 5 \mathrm{~min}\).
b. Implant Phosphorus ( \(\mathrm{N}+\) ), Dose \(=5.84 \times 10^{15}, 160 \mathrm{keV}\)
10. Piranha Clean, 5 min.
11. Oxide growth over \(\mathrm{N}+-3983 \mathrm{~A}\), \(\mathrm{N}+\) Drive-in Furnace
a. Wet \(O_{2}, 950^{\circ} \mathrm{C}, 60 \mathrm{~min}\).
b. Dry \(N_{2}, 900{ }^{\circ} \mathrm{C}, 30 \mathrm{~min}\). \((\mathrm{xj}(\mathrm{N}\) channel \(\mathrm{S} / \mathrm{D})=0.476 \mu \mathrm{~m}\), Rsh=27.88 ohms/square)
12. Pos. PR Step, Mask \#3: P+ (P channel S/D) mask.
a. Apply photoresist, expose, develop (follow 3.a-i)
b. Oxide etch, buffered \(H F\left(N H_{4} F: H F-5: 1\right)\) etch rate \(.115 \mu \mathrm{~m} / \mathrm{min}\). (etch time \(=7.5 \mathrm{~min}\).)
c. PR strip
d. Piranha clean, 15 min .
13. Implant step - P+ Drive-in Furnace
a. Grow implant oxide-290A
1. Wet \(\mathrm{O}_{2}, 900^{\circ} \mathrm{C}, 3 \mathrm{~min}\). \((.29 / .40 \mu \mathrm{~m})\)
2. Dry \(N_{2}, 900^{\circ} \mathrm{C}, 5 \mathrm{~min}\).
b. Implant Boron ( \(\mathrm{P}+\) ). Dose \(=5.50 x 10^{15}\), 32 keV ( \(\mathrm{xj}(\mathrm{P}\) channel \(\mathrm{S} / \mathrm{D})=.598 \mu \mathrm{~m}\), Rsh=22.28 ohms/square, Rsh(well) \(=958\) ohms/square)
14. Gettering step :

Implant Boron Difluoride into back side of wafer Dose \(=5 x 10^{15}, 200 \mathrm{keV}\)
15. Piranha Clean, 5 min .
16. Oxide growth over \(\mathrm{P}+\) and \(\mathrm{N}+/ \mathrm{P}+\) drive-in \(-3200 \mathrm{~A}, \mathrm{P}+\) drive-in Furnace
a. Wet \(O_{R}, 1100^{\circ} \mathrm{C}, 15 \mathrm{~min}\). (setting=1110) (Calibrate furnace temp. first)
b. Dry \(N_{2}, 1100{ }^{\circ} \mathrm{C}, 28 \mathrm{~min}\). ( 27 min . then 2 min . pulling out) ( \(\mathrm{xj}(\mathrm{N}\) channel \(\mathrm{S} / \mathrm{D})=1.654 \mu \mathrm{~m}, \quad\) Rsh=18.39 ohms/square) (xj( P channel \(\mathrm{S} / \mathrm{D})=1.589 \mu \mathrm{~m}, \mathrm{Rsh}=40.9 \mathrm{ohms} / \mathrm{square}\) )
17. Pos. PR Step, Mask \#4 : Thin Oxide ( \(P\) channel and \(N\) channel Gates) mask.
a. Apply photoresist, expose, develop (follow 3.a-i)
b. Oxide etch, buffered \(H F\left(N H_{4} F: H F-5: 1\right)\) etch rate \(.115 \mu \mathrm{~m} / \mathrm{min}\). (etch through \(\sim 12000 \mathrm{~A}\) oxide) (etch time \(=7.5 \mathrm{~min}\).)
c. PR strip
d. Piranha clean, 15 min .
18. Gate Oxide Growth \(-840 \mathrm{~A} / \mathrm{P}+\) (well), \(824 \mathrm{~A} / \mathrm{P}+\) (substrate), 1822A/ \(\mathrm{N}+\) (or 1100A/gate, \(1200 \mathrm{~A} / \mathrm{N}+\) ) \(\mathrm{P}+\) drive-in furnace
a. TCE clean \(\mathrm{P}+\) drive-in furnace at least 12 hours before use
b. Wet \(\mathrm{O}_{2}, 840^{\circ} \mathrm{C}, 75 \mathrm{~min}\). (Calibrate temp. first, check water after 1.5 hour) (setting \(=840\) ) (or Dry \(\mathrm{O}_{2}, 1000^{\circ} \mathrm{C}, 145 \mathrm{~min} .\), init. ox. furnace)
c. Dry \(N_{2}\) (anneal), \(840^{\circ} \mathrm{C}, 15 \mathrm{~min}\). (or Dry \(N_{2}\) (anneal), \(1000^{\circ} \mathrm{C}, 20 \mathrm{~min}\). for Dry \(O_{2}\) growth)
19. Threshold shift implant - Boron, Dose \(=5 x 10^{11}, 55 \mathrm{keV}\) (75 keV alt.)
20. Piranha clean, 5 min .
21. Threshold shift anneal - P+ drive-in furnace Dry \(N_{\ell}, 1000^{\circ} \mathrm{C}, 15 \mathrm{~min}\). (load and unload wafers in SLOWLY)
22. Pos. PR Step, Mask \#5 : Contact cut mask.
a. Apply photoresist, expose, develop (follow 3.a-i) (spin on at 5000 rpm ) (check very carefully for gaps)
b. Descum - Short plasma etch of resist 1. \(N_{2}, 1\) torr, 60 watts, \(65^{\circ} \mathrm{C}\) 2. \(\mathrm{O}_{2}, .76\) torr, 10 watts, 5 min .
c. Oxide etch, buffered \(\mathrm{HF}\left(\mathrm{NH}_{4} \mathrm{~F}: \mathrm{HF}-5: 1\right)\) etch rate \(.115 \mu \mathrm{~m} / \mathrm{min}\). (etch time \(=1.5 \mathrm{~min}\).) (etch through \(\sim 1700 \mathrm{~A}\) of oxide)
d. PR strip
e. Piranha clean, 15 min .
23. Metal deposition - 8000A Aluminum
a. \(H F \operatorname{dip}\) ( \(H F\) :water \(-1: 20\) ), 10 sec . (just until back of wafer repels water)
b. Bake under IR lamp, 15 min .
c. Use following settings: \(25 \mu \mathrm{~A}, 5.2\) remote, 1 staple, \(\sim 5 x 0^{-6}\) Torr, 80 sec.,25 toward
24. Pos. PR Step, Mask \#6 : Metal mask.

Apply photoresist expose, develop (follow 3.a-i) (spin on at 6200 rpm ) (VERY CRITICAL ALIGNMENT to N+)
25. Metal etch - Al etchant type \(\mathrm{A}, 45-50^{\circ} \mathrm{C}\), (Do not overetch) ( \(\sim 3.5 \mathrm{~min}\) )
26. PR strip, acetone, 10 min .
27. Rinse in DI water
28. Pos. PR Step, Mask \#1 : Self align implant. Apply photoresist, expose, develop (follow 3.a-i) (spin on at 6000 rpm )
29. Implant (self aligned PMOS) Boron, Dose \(=3.81 x 10^{19} .45 \mathrm{keV}\) (dose=40 \(\mu\) coulombs)
30. PR strip
a. Acetone, 30 min . ( 1 min . ultrasonic every 15 min .)
b. DI rinse and blow dry
c. Plasma etch, 150 watts, 1 torr, 5 min . or until done
31. Sinter Aluminum \(-450^{\circ} \mathrm{C}, 15 \mathrm{~min}\). with forming gas, 14 cm .
32. Spin on PR, 15 min. prebake \(\left(100{ }^{\circ} \mathrm{C}\right), 5000 \mathrm{rpm}, 30 \mathrm{sec} ., 20 \mathrm{~min}\) softbake \(\left(90^{\circ} \mathrm{C}\right)\)
33. Dice - dicing saw, speed=2(hi), 4.0 mils not sawed, channel \(1=\) \(4.250,2.500\), channel \(2=4.630,1.750\), distance to edge of chip \(=.250 \mathrm{~mm}\).
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\section*{APPENDIX E}

\section*{EXACT SIMULATION OF LOOP GAIN}

The loop gain of a feedback circuit provides valuable stability and settling time information [ 27]. Often loop gain simulations are based on approximations [ 27 ].[ 42 ]. For example, for the shunt-shunt feedback circuit of figure E. 1 the exact loop gain is given by
\[
T(s)=\frac{\left(G_{m}-y_{f}\right)\left(y_{f}-y_{r}\right)}{\left(y_{f}+y_{0}\right)\left(y_{f}+y_{f}\right)}
\]
(following the terminology in [27], see figure E.1). Output loading and the output admittance of the op amp are included in \(y_{0}\); the source admittance \(y_{z}\) and op amp input admittance are included in \(y_{t}\). Usually, \(y_{r}\), the reverse transmission through the op amp, is much smaller in magnitude than \(y_{f}\) in the frequency range of interest and can safely be neglected. But often \(y_{f}\) is assumed much smaller in magnitude than \(G_{m}\) and the loop gain is approximated as
\[
T(s)=\frac{c_{n} y_{f}}{\left(y_{f}+y_{0}\right)\left(y_{f}+y_{f}\right)}
\]

Neglecting \(y_{f}\) is not always valid. For example, if \(y_{f}=s C_{f o}\), then \(y_{f}\) and \(G_{n}\) may have comparable magnitudes near the frequency where \(|T(s)|=1\). In that case, neglecting \(y_{f}\) would yield an incorrect phase margin and possibly false stability data. Circuit design text books introduce the "break-the-loop" loop gain analysis which has a nice intuitive feel, but relies on the above assumptions as well as the assumption that \(\left|y_{0}\right| \gg\left|\frac{y_{f} y_{i}}{y_{f}+y_{t}}\right|[27][42]\). The "break-the-loop" loop gain is given by the voltage transfer function \(T(s)=-\frac{V_{r}}{V_{s}}\)


Figure R1. top: Shunt-shunt feedback circuit riddle: 0 p amp with feedback element \(y_{f}\) bottom: Same circuit with op amp replaced by its two-port representation
in figure E.2.
These approximations need not be made at all because direct, exact simulation of the loop gain is possible with circuit simulators like SPICE. For example, consider the shunt-shunt feedback circuit of figure E.1. If the input current source is replaced by a voitage source \(V_{z}\) as shown in flgure E.3, the transfer function from \(V_{s}\) to \(V_{0}\) is
\[
\frac{V_{0}}{V_{z}}=-\frac{\left(G_{m}-y_{f}\right)}{\left(y_{f}+y_{0}\right)}
\]

A dependent source, controlled by the output voltage, driving the output of the op amp in the reverse direction gives a voltage transfer relation
\[
\frac{V_{f}}{V_{0}}=\frac{\left(y_{f}-y_{r}\right)}{\left(y_{f}+y_{l}\right)}
\]

And therefore the overall transfer function \(-\frac{V_{F}}{V_{z}}\) is
\[
-\frac{V_{F}}{V_{z}}=\frac{\left(G_{m}-y_{f}\right)\left(y_{f}-y_{r}\right)}{\left(y_{f}+y_{0}\right)\left(y_{f}+y_{i}\right)}
\]
which equals the exact loop gain. No approximations were made.
It is often important, due to non-linear effects, to test the loop gain at different DC output voltages. These can easily be accommodated as is shown in figure E.4. The original circuit (figure E4, top) is used to determine the DC operating points. Then controlled sources are connected as shown in figure E. 4 to assure that all DC node voltages are correct. The loop gain is found by computing the small signal gain, \(T(s)=-\frac{V_{F}}{V_{z}}\).

This exact loop gain analysis can be applied to all four of the feedback conflgurations. Here is the procedure for exact loop gain analysis for an arbitrary feedback configuration:


Figure E2. Break-the-loop circuit for finding \(T(s)\)

Draw the circuit, labeling input and output sources correctly. The input source must be a current source if it is shunt feedback at the input, an input voltage source for series feedback at the input. Use Thevenin or Norton equivalences as required. Replace the input source with its dual ( \(i\) \(\rightarrow v_{1} v \rightarrow i\) ), call the new source \(S_{\mathbf{s}}\). Now make a second copy of the circuit. Drive the output of the second circuit with a controlled source of the same type as the output variable, with value +1 times the output of the first circuit. In this circuit, replace the test source \(S_{z}\) with an infinite impedance mismatch (replace a voltage source with an open circuit. replace a test current source with a short circuit.) Label the location where \(S_{x}\) was as \(S_{r}\) with the same polarity. If \(S_{z}\) was a test voltage, \(S_{r}\) will measure an open-circuit return voltage. If \(S_{z}\) was a test current. \(S_{r}\) will measure a short-circuit return current. Have the circuit simulator calcu-
late the transfer functions \(T(s)=-\frac{S_{r}}{S_{s}}\) which is the exact loop gain. An arbitrary DC input source can be accommodated as discussed above.


Figure E. 3 Circuit for finding \(T(s)\) exactly


Fgure E.4. Circuit for Anding \(T(\mathrm{~s})\) exactly, including DC biasing

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[^0]:    * computation. Each autocorrelation coefficient has a different filter.

