## Access Point Selection for Multi-Rate IEEE 802.11 Wireless LANs



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# Access Point Selection for Multi-Rate IEEE 802.11 Wireless LANs 

by Shicong Yang<br>A thesis submitted in partial satisfaction of the requirements for the degree of<br>Master of Science<br>in<br>Engineering - Electrical Engineering and Computer Sciences<br>in the<br>Graduate Division<br>of the<br>University of California, Berkeley<br>Committee in charge:<br>Professor Avideh Zakhor, Chair<br>Professor Jean Walrand<br>Professor Sylvia Ratnasamy

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Access Point Selection for Multi-Rate IEEE 802.11 Wireless LANs

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Abstract<br>Access Point Selection for Multi-Rate IEEE 802.11 Wireless LANs<br>by<br>Shicong Yang<br>Master of Science in Engineering - Electrical Engineering and Computer Sciences<br>University of California, Berkeley<br>Professor Avideh Zakhor, Chair

Access Point (AP) selection is an important problem in WLANs as it affects the throughput of the joining station (STA). Existing approaches to AP selection predominantly use received signal power and as such, do not take into account interference and collisions at each STA, and transmit opportunities (TXOPs) at APs. In this paper, we propose a class of AP selection algorithms based on the joining STA's expected throughput by taking into account the above factors. Specifically, we collect a binary-valued local channel occupancy signal, called busy-idle (BI) signal, at each node and require the APs to periodically broadcast their BI signal together with a quantity that represents TXOPs at the APs. This enables the joining STA to estimate expected throughput for each candidate AP before it selects one. To capture TXOPs at each AP, we propose a few different quantities, including the number of associated STAs, sum of inverse of MAC rates, and the average waiting and idle times. We use NS-2 simulations to demonstrate the effectiveness of our algorithms. For a random topology consisting of 24 APs and 60 STAs, our algorithms can increase average throughput of the joining STA by as much as $52 \%$ as compared to the traditional signal power based AP selection approach (rxpwr). In this case, the achieved average throughput is $97 \%$ of that obtained via the optimal selection. We also show that, in contrast to rxpwr, the throughput of our proposed algorithms remain close to optimal with the increase in AP density or STA density.

To Yu Shi and my family

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## Chapter 1

## Introduction

Wireless local area networks (WLANs) have gained increasing popularity due to their convenience, flexibility, and mobility as compared to traditional wireline infrastructure. As a result, WLANs are becoming the preferred technology of highspeed broadband access in homes, offices, and other hotspots such as coffee shops, shopping malls, and airports. Each WLAN access point (AP) forms a Basic Service Set (BSS), and multiple BSSs can overlap to form an Extended Service Set (ESS) to provide seamless handoff for stations (STAs). Due to the dense deployment of WLANs and the use of ESS to provide roaming services, it is common for STAs to have multiple available APs to choose from. In addition, nearby BSSs often experience inter-BSS co-channel interference due to the limited number of orthogonal channels. The MAC rate and throughput for different APs can vary significantly depending on the physical channel conditions and the interference level. An inappropriate AP selection typically leads to compromised service, thus it is imperative for an STA to identify and select the AP that provides the highest data rate to improve user experience.

AP selection policy is not specified in IEEE 802.11 standards. Currently the most widely used scheme is to select the AP with the strongest received power. Stronger received signal implies that the wireless channel is in better condition and can potentially support higher MAC rates, resulting in higher throughput for STAs. While this strategy is straightforward and easy to implement with no modifications and overhead to existing standards, it is ineffective especially in hyper dense deployment scenarios where adjacent APs could use the same channel. For example, as shown in Figure 1.1, consider two nearby co-channel APs who cannot sense each other, and an "joining" STA within range of both APs. Assume without loss of generality, the joining STA is closer to AP 2 and hence experiences a higher received signal power from it as compared to AP 1. The traditional received signal power based method would result in selecting AP 2, even though it could experience more interference and a lower throughput. Furthermore, the strongest received signal power based algorithm cannot take into account the difference between the potential transmit opportunities (TXOPs) from the two APs, which is another important factor in determining


Figure 1.1. APs with Overlapping BSSs.
throughput. It is clear from this example that choosing an AP with the strongest received power is sub-optimal for hyper dense deployment of WLANs, and that interference, collisions and TXOPs should also be taken into account when selecting an AP among multiple available APs.

To address these issues, a variety of schemes have been proposed in the literature [1]-[18], many of which try to optimize potential throughput and bandwidth. Nicholson et al. propose that STAs quickly associate with each AP and run a battery of tests to estimate the quality of each AP's connection [1]. Vasudevan et al. propose to use potential bandwidth as a metric to facilitate AP selection [2], where beacon delays are used to estimate potential uplink (UL) and downlink (DL) bandwidth. Sundaresan et al. propose to optimize AP selection based on expected throughput obtained from cross-layer information [3]. Abusubaih et al. consider the effect of newly arrived STA on total network UL and DL throughput [4]. Similarly, Miyata et al. propose an AP selection algorithm to optimize total network throughput as well as preserving newly arrived STAs throughput [5]. Luo et al. consider wireless mesh networks and propose that a STA should make its association based on end-to-end performance [6]. A number of approaches take interference and collision into account for selecting APs. For instance, Fukuda et al. propose to avoid interference when selecting an AP [7]. Du et al. propose a metric to capture the effect of hidden nodes and multiple MAC rates [8]. They use the channel utilization field in the beacon packets and suggest that the difference between the AP's and the STA's respective channel usage captures the hidden node effect. Abusubaih et al. consider interference between BSSs and develop a metric based on collision probability to facilitate AP selection [9]. Jang et al. exploit the retry field in the MAC header to estimate collision probability, and propose to use expected throughput as a metric to choose APs [10]. Some researchers approach AP selection problem from fairness point of view. For example, Bejerano et al. propose to select AP for max-min fair bandwidth allocation [11]. Gong et al. further propose a distributed max-min throughput AP selection [12]. Zhou et al. consider multi-AP wireless hotspots and propose a new fairness notion called Fulfillment-based Fairness to select AP [13]. Judd et al. notice AP load imbalance problem for received signal strength based AP selection algorithm [14]. To alleviate this problem, Chen et al. propose to use probe delay to capture the load and probability of collisions on each AP [15]. They argue that higher load results in higher collision probability and therefore longer backoff time, so the probe frame delay increases when traffic load is
heavy. Moreover, Bahl et al. propose to utilize the well-known cell breathing concept in cellular telephony to balance load in WLANs [16]. Other work try to study the AP selection problem using game theory tools. Musacchio et al. approach wireless AP selection from the economic point of view and model the problem as a dynamic game [17]. Mittal et al. present a game-theoretic analysis of wireless AP selection by selfish STAs [18]. Jiang et al. shows joining the correct AP can be achieved by distributed solution under certain model [19].

In this thesis, we propose a class of AP selection algorithms to maximize a joining STA's DL expected throughput. Our proposed AP selection metrics not only consider TXOPs at APs, but also take into account the inter-BSS interference with a more accurate collision estimation technique. We use the framework in [20], which provides a method to estimate the collision probability for UL traffic at a given STA. The basic idea behind [20] is that all STAs and APs continually measure the spatial channel occupancy around them, with APs periodically broadcasting a compressed binaryvalued busy-idle (BI) signal to indicate their local channel occupancy to all associated STAs. Each STA can then estimate UL collision probability by comparing its local BI signal with that of the AP's. We extend this framework to estimate DL collision probability, and then compute decision metrics at the joining STA to select an AP.

Throughout the thesis, we use STA to refer to a non-AP station, and use node to refer to either an AP or an STA. The remainder of the thesis is organized as follows: Chapter 2 discusses our packet loss model, and the method to estimate each component of packet loss; Chapter 3 describes our proposed algorithms; Chapter 4 presents the performance evaluations, and Chapter 5 concludes the thesis.

## Chapter 2

## Packet Loss Modeling and Estimation

We categorize packet loss in WLANs into two classes: collisions and channel errors. A collision is defined as a packet failure at the intended receiver due to interference from other transmitters which are in close proximity to the receiver. A channel error is defined as an unsuccessful decoding of a packet due to low received SNR, which is caused by large path loss or deep multipath fade, given that the packet does not suffer from collisions. The probability of total packet loss can be expressed as:

$$
\begin{equation*}
P_{L}=1-\left(1-P_{C}\right)\left(1-P_{e}\right) \tag{2.1}
\end{equation*}
$$

where $P_{C}$ is the packet loss probability due to collisions, and $P_{e}$ is the packet loss probability due to channel error given that the packet does not experience collisions. Equivalently, the packet success rate $P_{S}$ is given by:

$$
\begin{equation*}
P_{S}=1-P_{L}=\left(1-P_{C}\right)\left(1-P_{e}\right) \tag{2.2}
\end{equation*}
$$

In this thesis, we assume none of the packets suffering from collisions are captured, and are therefore assumed to be lost.

Krishnan et al. proposed a framework to estimate UL collision probabilities at STAs, using the local channel occupancy at the STA as well as the periodically broadcasted BI signal associated with the STA's AP, which reflects the AP's local channel occupancy [20]. We now generalize the estimator in [20] to estimate the collision probability on link ( $T x, R x$ ) as follows:

$$
\begin{equation*}
P_{C}(T x, R x)=f\left(B I_{T x}, B I_{R x}\right) \tag{2.3}
\end{equation*}
$$

where $B I_{T x}$ and $B I_{R x}$ are BI signals collected at the transmitter and the receiver, respectively. For DL, suppose AP $i$ is the $T x$ and STA $j$ is the $R x$, hence:

$$
\begin{equation*}
P_{C}(i, j)=f\left(B I_{A P_{i}}, B I_{S T A_{j}}\right) \tag{2.4}
\end{equation*}
$$

We classify collisions into three types: direction collisions (DCs), staggered collisions of type 1 (SC1), and staggered collisions of type 2 (SC2) [20]. A DC for a given node
is a collision in which the node under consideration finishes its backoff period and starts transmitting at the same time as other nodes. An SC1 for a given node is a collision in which the node under consideration transmits first and is then interrupted by a hidden node. An SC2 for a given node is a collision in which the node under consideration interrupts the transmission of a hidden node. Intuitively, for the node under consideration, an SC2 occurs when another node is already transmitting to the intended receiver before the node starts to transmit, a DC occurs when another node starts transmitting at the same time the node starts to transmit, and an SC1 occurs when another node starts transmitting later than, but interrupts, the node's transmission. Based on the above description, $\left(1-P_{C}\right)$ can be expanded into [20]:

$$
\begin{equation*}
\left(1-P_{C}\right)=\left(1-P_{S C 2}\right)\left(1-P_{D C}\right)\left(1-P_{S C 1}\right) \tag{2.5}
\end{equation*}
$$

where $P_{S C 2}$ denotes the probability of $\mathrm{SC} 2, P_{D C}$ denotes the probability of DCs given that it does not experience SC 2 , and $P_{S C 1}$ denotes the probability of SC 1 given that it experiences neither SC2 nor DC [20]. Due to the way collisions are counted, SC2 is the dominant type of collision for high traffic scenarios [20], and can therefore be used to approximate the total DL collision probability in a traffic-saturated WLAN network as:

$$
\begin{equation*}
P_{C}(i, j) \approx P_{S C 2}(i, j)=\frac{\sum_{t} \mathbb{1}\left\{B I_{A P i}(t)=0, B I_{S T A j}(t)=1\right\}}{\sum_{t} \mathbb{1}\left\{B I_{A P i}(t)=0\right\}} \tag{2.6}
\end{equation*}
$$

where $\mathbb{1}\{\cdot\}$ is the indicator function. The intuition is that this is the probability that the channel is busy at the STA given that it is idle at the AP, and hence if at time $t$ a packet was transmitted by the AP when AP senses the channel to be idle, i.e., $B I_{A P i}(t)=0$, it would have experienced collision at the STA with probability $P_{C}(i, j)$.

An 802.11 packet uses PHY modulation rate $R_{\text {PHY }}$ for preamble and PLCP header, and potentially higher modulation rates $R_{\text {MAC }}$ for MAC frame. The probability of channel error for packets from AP $i$ to STA $j$ can be expressed as [21]

$$
\begin{align*}
& P_{e}(i, j)=1-\left(1-B E R_{R_{\mathrm{PHY}}}\left(S N R_{i j}\right)\right)^{L_{\mathrm{PHY}}}  \tag{2.7}\\
&\left(1-B E R_{R_{\mathrm{MAC}}}\left(S N R_{i j}\right)\right)^{L_{\mathrm{MAC}}}
\end{align*}
$$

where $L_{\mathrm{PHY}}$ and $L_{\mathrm{MAC}}$ are the lengths of the preamble and PLCP header, and MAC frame, respectively. $B E R_{R}(S N R)$ denotes the bit error rate which is assumed to be a known function of modulation rate $R$ and $S N R$. $S N R_{i j}$ can be estimated as:

$$
\begin{equation*}
S N R_{i j}=\frac{P r_{i j}}{N o i s e} \tag{2.8}
\end{equation*}
$$

where $\operatorname{Pr}_{i j}$ is the received power of beacon packets from AP $i$ to STA $j$, and Noise is the thermal noise that can be estimated from:

$$
\begin{equation*}
\text { Noise }(\mathrm{dBm})=-174+10 \log _{10}(W)+N_{f} \tag{2.9}
\end{equation*}
$$

where $W$ is the bandwidth of wireless transmission, and $N_{f}$ is the noise figure of the wireless system, which is a property of hardware. Substituting Equation (2.9) into Equation (2.8), $S N R_{i j}$ can be estimated and consequently the channel error probability $P_{e}(i, j)$ can be computed as Equation (2.7).

With the estimates of collision probability $P_{C}(i, j)$ and channel error probability $P_{e}(i, j)$, the total loss probability $P_{L}(i, j)$ can be computed as Equation (2.1). We use $P_{L}(i, j)$ to estimate average backoff time if STA $j$ associates with AP $i$, and to compute our proposed decision metric in Chapter 3.

## Chapter 3

## Proposed AP Selection Algorithm

In this chapter we describe a class of AP selection algorithms which take into account the TXOPs, MAC rates, interference and collisions at the STA. We begin by describing our system model. We assume WLAN operates in infrastructure mode with DCF, and hence no RTS/CTS is used. All traffic flows have the same priority, and packets have Poisson arrival whose rate depends on the application layer data rate. When serving MAC Service Data Units (MSDUs), an AP does not switch to a new MSDU until the previous MSDU is successful or dropped due to its retransmission limit being exceeded. The network is assumed to be saturated, i.e., the application layers always have backlogs in their queues. The MAC rate is determined by the path loss from an STA to its serving AP, and no rate adaptation is assumed to be used. In this analysis we assume APs to be on the same channel, and focus on one STA $j$ joining the network while all other STAs are already associated to and exchanging traffic with their desired APs. For ease of notation, we use $P_{C}(i), P_{e}(i)$ and $P_{S}(i)$ in place of $P_{C}(i, j), P_{e}(i, j)$ and $P_{S}(i, j)$, respectively, since only one joining STA $j$ is considered.

In our proposed algorithm, both APs and the joining STA record their BI signals at a resolution of $10 \mu s e c$ as suggested in [20]; this sampling period provides a good balance between estimation error and transmission overhead. APs broadcast the BI signals every $3 s e c$ with the overhead to send BI signal being about $3 \%$ in the 802.11 b network [20]. Before associating to any AP, the joining STA stays idle and records its local BI signal for the first 3 sec .

Our approach to AP selection is to maximize DL expected throughput (eTP):

$$
\begin{equation*}
A P_{\text {sel }}=\arg \max _{i \in \mathcal{A}}(e T P(i)) \tag{3.1}
\end{equation*}
$$

where $\mathcal{A}$ is the set of candidate APs that the joining STA can choose from. We define $e T P(i)$ as:

$$
\begin{aligned}
e T P(i): & =\frac{\text { total successful MSDU in bits from AP } i \text { to joining STA }}{\text { total time }} \\
& =\frac{\text { total time to send MSDU by AP } i \text { to joining STA }}{\text { total time }}
\end{aligned}
$$

$$
\begin{align*}
& \times \frac{\text { total successful MSDU in bits from AP } i \text { to joining STA }}{\text { total time to send MSDU by AP } i \text { to joining STA }}  \tag{3.2}\\
& =t_{\text {alloc }}(i) \times e T M R(i) \tag{3.3}
\end{align*}
$$

where we denote the first term in Equation (3.2) as $t_{\text {alloc }}(i)$, representing the percentage of channel time that AP $i$ can allocate to the joining STA, and define the second term as $(e T M R(i))$, representing the expected true MAC rate from AP $i$ to the joining STA. Note the MSDU in Equation (3.2) is also known as MAC payload, and we will use them interchangeably in this thesis. We refer the second term as "true" MAC rate because it measures the real MAC layer data rate that the STA experiences by counting only the successfully delivered MAC payloads. In contrast, the nominal MAC rate is the MAC layer data rate that is used by an AP to modulate packets to an STA, which does not take packet loss and overhead into account. The potential TXOP from AP $i$ is captured in $t_{\text {alloc }}(i)$ term, while the effect of MAC rate, interference and collisions is taken into account in both $t_{\text {alloc }}(i)$ and $e T M R(i)$. We elaborate on how to estimate these two terms in the following sections.

### 3.1 Estimating $e T M R(i)$

The $e T M R(i)$ from AP $i$ to the joining STA is defined as successful number of MAC payload bits transmitted over the time that AP $i$ spent for delivering those data, including packet transmission time and all associated overhead time. eTMR(i) can be expressed as:

$$
\begin{align*}
e T M R(i): & =\frac{\text { total successful MSDU in bits from AP } i \text { to joining STA }}{\text { total time to send MSDU by AP } i \text { to joining STA }} \\
& =\frac{\sum_{m} L_{i}(m) \times \mathbb{1}\left\{A_{i}(m)\right\}}{\sum_{m} t_{i}(m)} \tag{3.4}
\end{align*}
$$

where $L_{i}(m)$ is the MSDU size in bits from AP $i$ on the $m$ th Physical layer Protocol Data Unit (PPDU) transmission, $t_{i}(m)$ is the time that AP $i$ spent on the $m$ th PPDU transmission, backoff and protocol overhead, $A_{i}(m)$ is the event that the $m$ th PPDU sent by AP $i$ to the joining STA is successful, and $\mathbb{1}\{\cdot\}$ is the indicator function defined by:

$$
\mathbb{1}\left\{A_{i}(m)\right\}= \begin{cases}1 & \text { if } m \text { th PPDU sent by AP } i \text { succeeds }  \tag{3.5}\\ 0 & \text { if } m \text { th PPDU sent by AP } i \text { fails }\end{cases}
$$

If we assume the maximum MAC payload size $L$ is used for each packet, Equation (3.4) can be rewritten as:

$$
\begin{align*}
\operatorname{eTMR}(i) & =\frac{L \times \sum_{m} \mathbb{1}\left\{A_{i}(m)\right\}}{\sum_{m} t_{i}(m)} \\
& =\frac{L \times P_{S}(i)}{t(i)} \tag{3.6}
\end{align*}
$$

where $P_{S}(i)$ is the packet success probability from AP $i$ to the joining STA given by Equation (2.2), $t(i)$ is the average time that AP $i$ allocates to the joining STA for one packet transmission including backoff time, PPDU transmission time and protocol overhead, given by:

$$
\begin{equation*}
t(i)=t_{p}(i)+t_{\mathrm{OH}}(i) \tag{3.7}
\end{equation*}
$$

where $t_{p}(i)$ is the time for AP $i$ to transmit MAC payload to the joining STA, and $t_{O H}(i)$ is the average overhead of one MSDU transmission from AP $i$. Substituting Equation (3.7) into (3.6) and rearranging the terms, we obtain:

$$
\begin{align*}
e T M R(i) & =\frac{L \times P_{S}(i)}{t(i)}=\frac{L \times P_{S}(i)}{t_{p}(i)+t_{O H}(i)} \\
& =\frac{L}{t_{p}(i)} \times P_{S}(i) \times \frac{t_{p}(i)}{t_{p}(i)+t_{O H}(i)}  \tag{3.8}\\
& =R_{\mathrm{MAC}}(i) \times P_{S}(i) \times \frac{t_{p}(i)}{t_{p}(i)+t_{O H}(i)}
\end{align*}
$$

where $R_{\text {MAC }}(i)=L / t_{p}(i)$ is the MAC rate used by AP $i$ for the joining STA to modulate MAC payload. Substituting Equation (2.2) into (3.8), we obtain the following expression for $e T M R(i)$ at AP $i$ :

$$
\begin{equation*}
e T M R(i)=R(i) \times\left(1-P_{C}(i)\right) \times\left(1-P_{e}(i)\right) \times \frac{t_{p}(i)}{t_{p}(i)+t_{O H}(i)} \tag{3.9}
\end{equation*}
$$

where $P_{C}(i)$ is the DL collision probability given by Equation (2.6), and $P_{e}(i)$ is the DL channel error probability given by Equation (2.7). Next we explain how to estimate each component in Equation (3.9) in order for the joining STA to optimally select the AP.
$R(i)$ depends on $S N R_{i}$ from AP $i$ to the joining STA. Assuming the function to map $S N R$ to MAC rate is known, the MAC rate $R(i)$ used by AP $i$ can be predicted as long as $S N R$ is estimated as in Equation (2.8).
$t_{p}(i)$ is the time to transmit MAC payload, i.e., MSDU. It depends on the payload size $L$ in bits and MAC rate $R_{\mathrm{MAC}}(i)$ :

$$
\begin{equation*}
t_{p}(i)=\frac{L}{R_{\mathrm{MAC}}(i)} \tag{3.10}
\end{equation*}
$$

Maximum payload is typically used in WLANs to improve transmission efficiency.
$t_{O H}(i)$ is the average overhead time for AP $i$ to deliver one MSDU, which includes preamble, PLCP header, MAC header and CRC, inter-frame spacing time, possible ACK time, and backoff time. In 802.11 each MSDU has a predefined retransmission limit $N$. Let $n \in[0, \cdots, N-1]$ be the retransmission state of an MSDU, $\pi(n)$ be the probability that a node is in retransmission state $n$, and $t_{O H}(i, n)$ be the overhead for a single MSDU transmission on the $n$th retry. Then $t_{O H}(i)$ is given by:

$$
\begin{equation*}
t_{O H}(i)=\sum_{n=0}^{N-1} \pi(n) t_{O H}(i, n) \tag{3.11}
\end{equation*}
$$

and $t_{O H}(i, n)$ is given by:

$$
\begin{equation*}
t_{O H}(i, n)=\bar{t}_{\mathrm{b}}(i, n)+t_{h}(i)+t_{\text {protocol }} \tag{3.12}
\end{equation*}
$$

where $\overline{t_{\mathrm{b}}}(i, n)$ is the average backoff duration on the $n$th MSDU retry when AP $i$ is transmitting to the joining STA, $t_{h}(i)$ is the time to transmit the PHY layer preamble, the PLCP header, the MAC header, and MAC CRC, and $t_{\text {protocol }}$ is the overhead introduced by the 802.11 protocol for a single PPDU transmission, including inter-frame spacing, backoff time, and possible ACK time given by:

$$
t_{\text {protocol }}= \begin{cases}T_{\mathrm{SIFS}}+T_{\mathrm{ACK}}+T_{\mathrm{DIFS}} & \text { if PPDU succeeds }  \tag{3.13}\\ T_{\mathrm{EIFS}} & \text { if PPDU fails }\end{cases}
$$

where $T_{\mathrm{ACK}}$ is the time to transmit an ACK packet if the ACK packet is modulated at lowest rate, $T_{\text {SIFS }}$ is the short inter-frame spacing, $T_{\text {DIFS }}$ is the DCF inter-frame spacing, and $T_{\text {EIFS }}$ is the extended inter-frame spacing defined by the 802.11 standards as:

$$
\begin{equation*}
T_{\mathrm{EIFS}}=T_{\mathrm{SIFS}}+T_{\mathrm{ACK}}+T_{\mathrm{DIFS}} \tag{3.14}
\end{equation*}
$$

This implies that $t_{\text {protocol }}$ in Equation (3.13) is the same regardless of whether or not the packet transmission is successful, if the ACK packet is modulated at lowest rate.
$t_{h}(i)$ in Equation (3.12) does not depend on the retransmission state $n$, and can be calculated as:

$$
\begin{equation*}
t_{h}(i)=\frac{L_{\text {pre }}}{R_{\mathrm{PHY}}}+\frac{L_{\text {plcp }}}{R_{\mathrm{PHY}}}+\frac{L_{m o}}{R_{\mathrm{MAC}}(i)} \tag{3.15}
\end{equation*}
$$

where $L_{\text {pre }}$ is the length of preamble in bits, $L_{p l c p}$ is the length of PLCP header in bits, $L_{m o}$ is the length of MAC header and CRC in bits, $R_{\text {PHY }}$ is the PHY modulation rate defined for a particular 802.11 protocol, and $R_{\mathrm{MAC}}(i)$ is the modulation rate used for MAC frame by AP $i$. Combining Equations (3.11) and (3.12), we obtain:

$$
\begin{align*}
t_{O H}(i) & =\sum_{n=0}^{N-1} \pi(n) t_{O H}(i, n) \\
& =\sum_{n=0}^{N-1} \pi(n) \times\left(\overline{t_{\mathrm{b}}}(i, n)+t_{h}(i)+t_{\text {protocol }}\right)  \tag{3.16}\\
& =t_{h}(i)+t_{\text {protocol }}+\sum_{n=0}^{N-1} \pi(n) \overline{t_{\mathrm{b}}}(i, n)
\end{align*}
$$

Denoting $\overline{t_{\mathrm{b}}}(i)$ to be the average backoff duration for packets from AP $i$ to the joining STA:

$$
\begin{equation*}
\overline{t_{\mathrm{b}}}(i)=\sum_{n=0}^{N-1} \pi(n) \bar{t}_{\mathrm{b}}(i, n) \tag{3.17}
\end{equation*}
$$

Equation (3.16) can be simplified to:

$$
\begin{equation*}
t_{O H}(i)=t_{h}(i)+t_{\text {protocol }}+\overline{t_{\mathrm{b}}}(i) \tag{3.18}
\end{equation*}
$$



Figure 3.1. Markov Chain Model for 802.11 DCF BEB.

We now explain how $\pi=(\pi(0), \cdots, \pi(n), \cdots, \pi(N-1))$ and $\overline{t_{\mathrm{b}}}(i, n)$ can be estimated. IEEE 802.11 standards use Binary Exponential Backoff (BEB) to achieve random channel access. Before each node transmits, it is required to wait for a random amount of time slots uniformly chosen from $[0, C W(n)]$, where $C W(n)$ is the contention window size on the $n$th retry:

$$
\begin{equation*}
C W(n)=\min \left\{\left(C W_{\min }+1\right) \times 2^{n}-1, C W_{\max }\right\} \tag{3.19}
\end{equation*}
$$

where $C W_{\min }$ and $C W_{\max }$ are predefined maximum and minimum contention window size, respectively. The average backoff interval on the $n$th retry is:

$$
\begin{equation*}
\overline{t_{\mathrm{b}}}(i, n)=\frac{C W(n)}{2} \times T_{\mathrm{slot}} \tag{3.20}
\end{equation*}
$$

where $T_{\text {slot }}$ is the slot time defined for a particular 802.11 PHY layer.
To estimate $\pi(n)$, the probability that a node is in retransmission state $n$, we model the BEB behavior for MSDUs from AP $i$ to the joining STA by a Markov Chain (MC) shown in Figure 3.1. The MC state $n \in[0, \cdots, N-1]$ is the retransmission count of an MSDU, and $\pi$ is the stationary distribution of the MC. The $N \times N$ transition matrix $P(i)$ of the MC for AP $i$ can be constructed as:

$$
P(i)=\left(\begin{array}{cccccc}
1-P_{L}(i) & P_{L}(i) & 0 & 0 & \cdots & 0  \tag{3.21}\\
1-P_{L}(i) & 0 & P_{L}(i) & 0 & \cdots & 0 \\
\vdots & & & & & \vdots \\
1-P_{L}(i) & 0 & 0 & 0 & \cdots & P_{L}(i) \\
1 & 0 & 0 & 0 & \cdots & 0
\end{array}\right)
$$

where $P_{L}(i)$ is given by Equation (2.1). The stationary distribution $\pi$ of MC is the eigenvector of $P(i)$ corresponding to eigenvalue of 1 , and can therfore be estimated from $P_{L}(i)$. Combining Equations (3.17), (3.18) and (3.20), the average overhead time is

$$
\begin{equation*}
t_{O H}(i)=t_{h}(i)+t_{\text {protocol }}+\sum_{n=0}^{N-1} \pi(n) C W(n) T_{\text {slot }} / 2 \tag{3.22}
\end{equation*}
$$

Once $t_{O H}(i)$ and the corresponding values in Equations (2.6), (2.7), and (3.10) are estimated by the joining STA, Equation (3.9) can be used to evaluate eTMR(i).

### 3.2 Estimating $t_{\text {alloc }}(i)$

The $t_{\text {alloc }}(i)$ is a unit-less term representing the expected percentage of DL channel time that AP $i$ can allocate to the joining STA. We propose four different ways to estimate this quantity, resulting in four different decision metrics for selecting AP:

1. eTMR: $t_{\text {alloc }}(i)$ is a constant.
2. eTP $P_{n}: t_{\text {alloc }}(i)$ is estimated by the number of STAs that are already associated with AP $i$.
3. eTP $P_{r}: t_{\text {alloc }}(i)$ is estimated by the MAC rates of STAs that are already associated with AP $i$.
4. $e T P_{t}$ : $t_{\text {alloc }}(i)$ is estimated by calculating the average waiting time between consecutive unique MSDUs from AP $i$ to the joining STA.

We now describe each method, and provide detailed evaluations in Chapter 4.

### 3.2.1 eTMR

The simplest way to estimate $t_{\text {alloc }}$ is to treat it as a constant. Without loss of generality, we can set $t_{\text {alloc }}=1$. Substituting this into Equation (3.3), the resulting metric becomes:

$$
\begin{equation*}
e T P(i)=t_{\text {alloc }}(i) \times e T M R(i)=e T M R(i) \tag{3.23}
\end{equation*}
$$

which is equivalent to $e T M R$. We denote this decision metric as $e T M R$ in subsequent sections.

### 3.2.2 $e T P_{n}$

In this case we denote $t_{\text {alloc }}$ as $t_{\text {alloc }}^{n}$. Let $N_{\text {assoc }}(i)$ be the number of STAs that are already associated with AP $i$, which can be broadcasted by the AP along with the BI signals. Assuming that APs can allocate equal amount of channel time to each associated STA, $t_{\text {alloc }}^{n}$ can be computed as:

$$
\begin{equation*}
t_{\text {alloc }}^{n}(i)=\frac{1}{N_{\text {assoc }}(i)+1} \tag{3.24}
\end{equation*}
$$

Substituting Equation (3.24) into Equation (3.3), we obtain:

$$
\begin{equation*}
e T P_{n}(i)=\frac{1}{N_{\mathrm{assoc}}(i)+1} \times e \operatorname{TMR}(i) \tag{3.25}
\end{equation*}
$$

### 3.2.3 eT $P_{r}$

In this case we denote $t_{\text {alloc }}$ as $t_{\text {alloc }}^{r}$. Let $R(i)$ be the MAC rate from AP $i$ to the joining STA, and $R_{i}(k)$ be the MAC rate from AP $i$ to the STA $k$. Assuming that APs can transmit equal amount of data in bits to each associated STA, $t_{\text {alloc }}^{r}$ can be estimated as:

$$
\begin{equation*}
t_{\text {alloc }}^{r}(i)=\frac{1 / R(i)}{1 / R(i)+\sum_{k \in \mathcal{S}_{i}} 1 / R_{i}(k)} \tag{3.26}
\end{equation*}
$$

where $\mathcal{S}_{i}$ is the set of STAs that are already associated with AP $i$. Intuitively speaking, the higher MAC rate one STA can get from AP $i$, the less time AP $i$ spends to transmit packets to the STA, and hence the less channel time AP $i$ would allocate to the STA. Specifically for the joining STA, the higher MAC rate other associated STAs can get from AP $i$, the more channel time AP $i$ can allocate to the joining STA.

Substituting Equation (3.26) into Equation (3.3), we obtain:

$$
\begin{equation*}
e T P_{r}(i)=\frac{1 / R(i)}{1 / R(i)+\sum_{k \in \mathcal{S}_{i}} 1 / R_{i}(k)} \times e T M R(i) \tag{3.27}
\end{equation*}
$$

Note the quantity $\sum_{k \in \mathcal{S}_{i}} 1 / R_{i}(k)$ can be computed by AP $i$ and broadcast along with BI signals.

### 3.2.4 $e T P_{t}$

In this case, we denote $e T P$ as $e T P_{t}$ and $t_{\text {alloc }}$ as $t_{\text {alloc }}^{t}$. In practice, $t_{\text {alloc }}(i)$ is not only determined by the number of associated STAs and the MAC rate of those STAs, but also determined by the success probability of packet transmission to each STA. For example, if one STA has excessively low packet success probability, the AP would have to keep retransmitting to it and hence spend less time on other STAs. $t_{\text {alloc }}(i)$ is also affected by how often AP $i$ has to wait for the transmissions of other APs and STAs due to CSMA.

In order to estimate $t_{\text {alloc }}^{t}(i)$, we introduce the concept of the expected transmission time $t_{u}(i)$ to deliver one unique MSDU from AP $i$ to the joining STA, and the expected waiting time $t_{w}^{\text {after }}(i)$ between two consecutive unique MSDUs for traffic from AP $i$ to the joining STA if the joining STA selects AP $i$ as its serving AP. By definition, $t_{\text {alloc }}^{t}(i)$ is the ratio between these two quantities:

$$
\begin{equation*}
t_{\mathrm{alloc}}^{t}(i)=\frac{t_{u}(i)}{t_{w}^{\text {after }}(i)} \tag{3.28}
\end{equation*}
$$

We now describe how to estimate $t_{u}(i)$ and $t_{w}^{\text {after }}(i)$.
$t_{u}(i)$ is defined to be the average time spent by AP $i$ to deliver one unique MSDU to the joining STA, which includes backoff time, possible retransmissions, and other protocol related overheads. To estimate $t_{u}(i)$, we need to determine how many retries $X_{i}$ are required to deliver one unique MSDU from AP $i$ to the joining STA.

The distribution of $X_{i}$ is the stationary distribution $\pi$ of the MC model shown in Figure 3.1.

Let $T_{u}(i)$ be the random variable for the time spent by AP $i$ to send one MSDU to the joining STA until the MSDU is successful after consecutive retries or until the MSDU is dropped due to exceeding retransmission limit. $T_{u}(i)$ can be written as:

$$
\begin{equation*}
T_{u}(i)=\sum_{x=0}^{X_{i}} t(i) \tag{3.29}
\end{equation*}
$$

where $t(i)$ is the average time that AP $i$ allocates to the joining STA for one PPDU transmission given by Equation (3.7). Then $t_{u}(i)$ is the expected value of $T_{u}(i)$ :

$$
\begin{equation*}
t_{u}(i)=E\left[T_{u}(i)\right]=E\left[\sum_{x=0}^{X_{i}} t(i)\right] \tag{3.30}
\end{equation*}
$$

Expanding Equation (3.30), we obtain:

$$
\begin{equation*}
t_{u}(i)=E\left[X_{i}\right] t(i) \tag{3.31}
\end{equation*}
$$

where

$$
\begin{equation*}
E\left[X_{i}\right]=\sum_{n=0}^{N-1}(n+1) \pi(n) \tag{3.32}
\end{equation*}
$$

Next we describe how to estimate $t_{w}^{\text {after }}(i) . t_{w}^{\text {after }}(i)$ depends on the amount of channel time AP $i$ needs to allocate to the joining STA and other associated STAs, as well as the amount of time AP $i$ has to wait when other nodes are active. This quantity cannot be measured before AP $i$ starts transmitting to the joining STA. However, assuming only one new STA joins the network, we can estimate $t_{w}^{\text {after }}(i)$ as:

$$
t_{w}^{\text {after }}(i)= \begin{cases}t_{w}^{\text {before }}(i) & \text { if } t_{\text {idle }}(i)>t_{u}(i)  \tag{3.33}\\ t_{w}^{\text {before }}(i)+t_{u}(i)-t_{\text {idle }}(i) & \text { if } t_{\text {idle }}(i)<t_{u}(i)\end{cases}
$$

where $t_{u}(i)$ is given by Equation (3.31), $t_{w}^{\text {before }}(i)$ is the minimum over all associated STAs' average waiting time to serve two consecutive unique MSDUs to the same STA from AP $i$ before the joining STA selects any AP, and $t_{\text {idle }}(i)$ is the minimum over all associated STAs' average idle time at AP $i$ for a duration of $t_{w}^{\text {before }}(i)$ before the joining STA selects any AP. Both $t_{w}^{\text {before }}(i)$ and $t_{\text {idle }}(i)$ can be computed at AP $i$, and be transmitted to the joining STA as additional fields in BI signals. The intuition in computing $t_{w}^{\text {after }}(i)$ is as follows: if AP $i$ is not too busy and has enough idle time to serve packets to the joining STA without sacrificing the TXOPs of other already associated STAs, the average waiting times $t_{w}^{\text {before }}(i)$ and $t_{w}^{\text {after }}(i)$ should be the same before and after the joining STA enters the network; otherwise, all STAs served by AP $i$ experience longer waiting times.
$t_{w}^{\text {before }}(i)$ depends on a number of factors such as the number of STAs associated with AP $i$, duration of interference that can pause backoff due to CSMA, as well as the


Figure 3.2. Illustration of $t_{w}(i, k)$.

MAC rate and the packet loss rate to each associated STA. Rather than estimating all these quantities, we simply require $\mathrm{AP} i$ to keep track of $t_{w}(i, k)$ which is the average time duration between two consecutive unique MSDUs transmitted by AP $i$ to STA $k$. Then:

$$
\begin{equation*}
t_{w}^{\text {before }}(i)=\min _{k \in \mathcal{S}_{i}} t_{w}(i, k) \tag{3.34}
\end{equation*}
$$

where $\mathcal{S}_{i}$ is the set of STAs associated with AP $i$ before the joining STA selects any AP. Intuitively $t_{w}(i, k)$ can be described as follows: Assume upper layer applications are sending saturated traffic, all traffic streams have the same priority, and an AP does not switch to a new MSDU until the previous MSDU is successful or dropped due to its retransmission limit being exceeded. Then the average behavior of AP $i$ can be modeled as transmitting MSDUs to each of its associated STA in a round-Robin fashion. The intuition for $t_{w}(i, k)$ is that on average AP $i$ will be served one unique MSDU to STA $k$ within a time period of $t_{w}(i, k)$, as shown in Figure 3.2.
$t_{\text {idle }}(i)$ can be computed at AP $i$ as follows: Define the total idle time $t_{\text {idle }}^{\text {total }}(i)$ at AP $i$ to be the period of time when AP $i$ is ready to transmit but there is no packet in the queue during a certain observation period denoted by $t_{\text {count }}$. We opt to choose $t_{\text {count }}$ to be the same amount of time to collect BI signals, which is $3 s e c$ in this work. Let $N_{\text {MSDU }}(i, k)$ be the number of MSDUs transmitted from AP $i$ to STA $j$ during $t_{\text {count }}$. Then $t_{\text {idle }}(i)$ is given by:

$$
\begin{equation*}
t_{\text {idle }}(i)=\frac{t_{\text {idleal }}^{\text {total }}\left(i, t_{\text {count }}\right)}{\max _{k \in \mathcal{S}_{i}} N_{\mathrm{MSDU}}\left(i, k, t_{\text {count }}\right)} \tag{3.35}
\end{equation*}
$$

In estimating $t_{\text {idle }}(i)$ in the above equation, we assume $t_{\text {count }}$ to be large enough for the estimate to be independent of $t_{\text {count }}$.

Once the joining STA receives estimated $t_{w}^{\text {after }}(i)$ and $t_{\text {idle }}(i)$ from AP $i$, given by Equations (3.33) and (3.35) respectively, $t_{w}^{\text {after }}(i)$ can be computed as in Equation (3.33). Combing with $t_{u}(i)$ as in Equation (3.31), we can compute the decision metric in this case as:

$$
\begin{equation*}
e T P_{t}(i)=\frac{t_{u}(i)}{t_{w}^{\text {atter }}(i)} \times e T M R(i) \tag{3.36}
\end{equation*}
$$

### 3.3 AP Selection Algorithm

We have described four AP decision metrics, namely eTMR,eTP, eTPr, and $e T P_{t}$. In practice, one of the four metrics is used to estimate $e T P(i)$. The proposed AP selection algorithm is summarized in Algorithm 1.

```
Algorithm 1 AP Selection Algorithm
    The joining STA scans for APs and obtains candidate AP set \(\mathcal{A}\)
    Collect local BI for 3 seconds
    Receive BI signal and other fields from all APs in \(\mathcal{A}\)
    for each AP \(i \in \mathcal{A}\) do
        compute \(e T P(i)\)
    end for
    The joining STA selects AP with largest eTP
```


## Chapter 4

## Performance Evaluation

### 4.1 Simulation Methodology

We use NS-2.31 to simulate 802.11 b networks in infrastructure mode. This can be easily extended to other standards, such as $802.11 \mathrm{a}, 802.11 \mathrm{~g}$ and 802.11 n . The NS simulator has been modified to compute collision probability as described in [20]. The transmission range of nodes is about 32 m , and no fading or shadowing is used in our path loss model. Each STA receives DL traffic from its serving AP. Each DL stream consists of traffic from a Constant Bit Rate (CBR) application which is generating packets at a rate that saturates the network. UDP is used as the transport layer protocol. MAC retry limit is set to be 10. Both the transmit and receive antennae have 0 dB gain.

In all simulations, both APs and STAs are randomly placed in a $110 \mathrm{~m} \times 110 \mathrm{~m}$ region mimicking typical hyper dense scenarios observed in practice. The number of simulated APs and STAs are shown in Table 4.1, and selected example topologies are shown in Figure 4.1. To reduce simulation overhead, we pre-generate three different sets of random locations for a given number of APs with the following constraints: 1) the APs cover at least $95 \%$ of simulation area, 2) the APs have a minimum separation distance depending on number of APs as shown in Table 4.1. Each simulation trial places all APs according to one of the three sets of pre-specified random AP locations. The STAs are placed at random according to a spatial Poisson process.

To determine the ground truth, for each simulation trial we fix AP and STA locations and run the simulations to compute the throughput of the joining STA under

Table 4.1. Simulated Topology Parameters

| \# AP | 8 | 8 | 16 | 16 | 16 | 24 | 24 | 32 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \# STA | 20 | 40 | 20 | 40 | 60 | 40 | 60 | 40 |
| Minimum AP distance [m] | 30 | 30 | 20 | 20 | 20 | 10 | 10 | 10 |



Figure 4.1. Example Topologies. Small blue circles: STAs. Big black circles: AP's range. Black triangles: APs. Red star: the joining STA. A line connecting an STA to an AP: the STA is associated with the AP. (a) 8 APs and 40 STAs; (b) 16 APs and 40 STAs; (c) 24 APs and 40 STAs; (d) 32 APs and 40 STAs.
the exact same conditions except that the joining STA associates with different APs, in order to determine the highest throughput AP which we call "optimum". Next we run the AP selection algorithms with proposed metrics and compare their selections with those obtained from the traditional strongest received power (rxpwr) algorithm in which the AP with the strongest received power is chosen. For each pair of number of APs and STAs shown in Table 4.1, we run 900 trials and discard the trials whose optimal throughput is less than 1kbps. We call these discarded trials "invalid". We refer to a non-optimal AP selection for a given algorithm as a valid trial in which the algorithm does not result in the same AP as the optimum.

Table 4.2. Simulation Results: 24 APs and 60 STAs

|  | $\%$ non-optimal <br> selection | Average throughput <br> $[\mathrm{kbps}]$ | Throughput gain <br> vs. rxpwr |
| :---: | :---: | :---: | :---: |
| rxpwr | $54 \%$ | 551.58 | 0 |
| eTMR | $31 \%$ | 721.27 | $31 \%$ |
| eTPn | $28 \%$ | 771.10 | $40 \%$ |
| eTPr | $26 \%$ | 782.61 | $42 \%$ |
| eTPt | $21 \%$ | 838.92 | $52 \%$ |
| optimal | $0 \%$ | 865.92 | $57 \%$ |

Table 4.3. Reduction in Non-Optimal Selections By $e T P_{t}$ Compared to rxpwr

| Reduction in non-optimal selection | \# AP |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 8 | 16 | 24 | 32 |  |
| \# STA | 20 | $-57 \%$ | $-54 \%$ | n/a | n/a |
|  | 40 | $-51 \%$ | $-59 \%$ | $-57 \%$ | $-68 \%$ |
|  | 60 | n/a | $-52 \%$ | $-62 \%$ | n/a |

### 4.2 Comparing Algorithms

Using extensive simulations, we have found that all proposed metrics perform better than rxpwr for all topologies listed in Table 4.1, with $e T P_{t}$ being the best. As an example, Table 4.2 summarizes the results for a topology with 24 APs and 60 STAs. As seen, our proposed algorithms all outperform rxpwr in terms of both the percentage of non-optimal selections and the average throughput of the joining STA; furthermore, $e T P_{t}$ attains the best performance among all algorithms, achieving $97 \%$ of the average throughput obtained by optimal selection, with a $52 \%$ improvement in average throughput as compared to rxpwr. We focus on analyzing $e T P_{t}$ in the remainder of the thesis.

Table 4.3 summarizes the reduction in non-optimal AP selections made by $e T P_{t}$ as compared to rxpwr for all simulated topologies. As seen, $e T P_{t}$ can reduce the non-optimal selections by more than $50 \%$ in all cases. Table 4.4 shows the average throughput gain of the joining STA obtained by $e T P_{t}$ compared to rxpwr. In general, $e T P_{t}$ achieves positive throughput gain over rxpwr in every simulated topology, with up to $72 \%$ improvement. Table 4.5 shows the percentage of achieved throughput by $e T P_{t}$ compared to optimal, which is at least $94 \%$ in all topologies.

Table 4.4. Average Throughput Gain By $e T P_{t}$ Compared to rxpwr

| Throughput gain vs. rxpwr | \# AP |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 8 | 16 | 24 | 32 |
| \# STA | 20 | $4 \%$ | $22 \%$ | n/a | n/a |
|  | 40 | $9 \%$ | $29 \%$ | $38 \%$ | $72 \%$ |
|  | 60 | n/a | $42 \%$ | $52 \%$ | n/a |

Table 4.5. Percentage of Optimal Throughput Achieved By eTP $P_{t}$

| Percenage of optimal TP achieved | \# AP |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 8 | 16 | 24 | 32 |  |
| \# STA | 20 | $99 \%$ | $96 \%$ | n/a | n/a |
|  | 40 | $99 \%$ | $96 \%$ | $96 \%$ | $94 \%$ |
|  | 60 | n/a | $97 \%$ | $97 \%$ | n/a |

### 4.3 Increasing Node density

With the increasing popularity of WiFi enabled devices, for a fixed number of APs in a given region, the throughput of each STA drops as the STA density increases. To alleviate this problem, more APs are typically deployed in order to provide better throughput to each STA. This creates hyper dense WLANs where AP selection based on rxpwr results in sub-optimal performance. Even for scenarios with a fixed number of users in a given area, more APs are typically added in order to achieve higher throughput per STA. An inherent problem with WLANs is that there is no closedloop power control mechanism to adjust cell size of APs. Therefore, as the AP density increases, the joining STA can select from an increasing number of candidate APs, making the AP selection problem even more important.

Figure 4.2 shows the NS simulation results for the distribution of the number of candidate APs for the joining STA, in a number of scenarios as the number of APs in a $110 \mathrm{~m} \times 110 \mathrm{~m}$ area increases from 8 to 32 . As expected, the joining STA can select from more candidate APs as the number of APs increases. For topologies with 32 APs, in $96 \%$ of simulation trials there are four or more candidate APs to choose from, and as such, AP selection becomes a significant issue. On the other hand, for topologies with 8 APs, the joining STA has one or two candidate APs in more than $85 \%$ of simulated trials, and therefore the AP selection problem is not as severe, so we do not expect much throughput gain in this case.

To evaluate the throughput performance of $e T P_{t}$ compared to rxpwr and optimal as a function of node density, we plot the average throughput of the joining STA over all valid simulation trials obtained by different selection algorithms in Figure 4.3.


Figure 4.2. Distribution of the number of candidate APs for the joining STA: (a) 8 APs; (b) 16 APs; (c) 24 APs; (d) 32 APs.

The results in Figure 4.3 are the same as those shown in Tables 4.3, 4.4, and 4.5. As expected, the average throughput for all AP selection algorithms drops with number of STAs, or equivalently the STA density, as shown in Figure 4.3(a). If more APs are placed in a WLAN to accommodate the increase in the number of STAs, the rxpwr throughput drops with total node density, while the $e T P_{t}$ throughput stays almost invariant and is very close to the optimal throughput, as shown in Figure 4.3(b). Specifically in Figure 4.3(b), the throughput gain of $e T P_{t}$ over rxpwr increases with total node density, growing from $4 \%$ for 28 nodes to $52 \%$ for 84 nodes. As seen in Figure 4.3(c), if the AP density is increased while STA density is fixed, the rxpwr throughput indicates a diminishing return, while the optimal and $e T P_{t}$ throughput


Figure 4.3. Average throughput of the joining STA achieved by different AP selection algorithms as a function of: (a) STA density with 16 APs; (b) total node density with STA to AP ratio fixed at 5:2; (c) AP density with 40 STAs.
both increase almost linearly. ${ }^{1}$ In particular, the throughput gain for $e T P_{t}$ over rxpwr increases with AP density, growing from $9 \%$ for 8 APs to $72 \%$ for 32 APs.

In order to examine the relative performance of $e T P_{t}$ and rxpwr as a function of node density, we plot the percentage of their achieved throughput as compared to

[^0]

Figure 4.4. Percentage of throughput achieved by different AP selection metrics for the joining STA compared to optimal as a function of: (a) STA density with 16 APs; (b) total node density with STA to AP ratio fixed at 5:2; (c) AP density with 40 STAs.
optimal in Figure 4.4. Specifically, Figures 4.4(a), 4.4(b) and 4.4(c) plot this quantity as a function of STA density, node density and AP density, respectively. The number of APs increases in the latter two cases, with the difference being that in Figure 4.4(b) the STA to AP ratio is maintained as 5:2, while in Figure 4.4(c) the number of STAs is fixed at 40 . As seen, $e T P_{t}$ remains within $6 \%$ of the optimal throughput in all three scenarios. In contrast, the relative throughput of rxpwr with respect to optimal decreases with STA density. This is mainly because rxpwr does not take into account collisions and TXOPs, which are important factors in determining throughput as the AP density increases. Overall, the throughput gain achieved by $e T P_{t}$ over rxpwr increases with node density, be it AP density, STA density, or both.


Figure 4.5. Histogram of the logarithm of ratio of $e T P_{t}$ over rxpwr throughput when decisions are different for 24 APs and 60 STAs.

So far, we have examined average throughput over all valid simulation trials, which is not a representative of the distribution of the throughput among trials. To examine the distribution of throughput gain, in Figure 4.5 we plot the histogram of the logarithm of the ratio of $e T P_{t}$ over rxpwr throughput of the joining STA for trials in which their selections are different, for the case with 24 APs and 60 STAs. In this case, $e T P_{t}$ achieves higher (lower) throughput compared to rxpwr in $50 \%$ $(14 \%)$ of the trials. In the remaining $36 \%$ of trials they select the same AP and hence have identical throughput. The histograms for other topologies show similar trends. In general for all simulated topologies, the number of trials in which $e T P_{t}$ achieves throughput gain over rxpwr is larger than those with throughput loss.

## Chapter 5

## Conclusion

In this paper we proposed a class of AP selection algorithms which take into account TXOPs, inter-BSS interference and collisions. This is achieved by exploiting BI signals both at the AP and at the joining STA, as well as additional information such as the number of associated STAs, sum of inverse of MAC rates to associated STAs, and average waiting and idle times.

Our proposed AP selection algorithms can reduce the percentage of non-optimal selections and improve the average throughput of the joining STA in all tested scenarios. In particular, $e T P_{t}$ achieves the best performance among all AP selection algorithms, and performs better than rxpwr as the node density increases, be it AP density, STA density, or both. For a random topology with 24 APs and 60 STAs, the average throughput gain of the joining STA obtained by $e T P_{t}$ is $52 \%$ as compared to the traditional received signal power based method. In this scenario $e T P_{t}$ achieves as much as $97 \%$ of the optimal throughput.

Future work includes extending the current work to AP selection for UL traffic, examining the impact of our AP selection algorithm on aggregate network throughput, and extending current static algorithm to dynamic AP selection in which existing STAs can switch from one AP to another.

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## Appendix A

## Acronyms and Symbols

Table A.1. Acronyms

| Acronym | Meaning |
| :---: | :---: |
| AP | access point in WLANs |
| BEB | binary exponential backoff |
| BER | bit error rate |
| BI | busy-idle signal |
| BSS | basic service set |
| CBR | constant bit rate |
| CW | direct collision |
| DC | downlink |
| DL | extended service set |
| ESS | expected true MAC rate |
| eTMR | expected throughput |
| eTP | medium access control |
| MAC | MAC layer Protocol Data Unit |
| MPDU | MAC layer Service Data Unit |
| MSDU | Markov Chain |
| MC | physical layer |
| PHY | Physical layer Protocol Data Unit |
| PPDU | staggered collision of type 1 |
| SC1 | staggered collision of type 2 |
| SC2 | signal-to-noise ratio |
| SNR | non-AP station in WLANs |
| STA | receive or receiver |
| Rx | transmit or transmitter |
| rxpwr | strongest received power based AP selection algorithm |
| TP | transmit opportunities |
| Tx | uplink |
| TXOP | wireless local area network |
| UL |  |

Table A.2. Symbols

| Symbol | Meaning |
| :---: | :---: |
| $\mathbb{1}\{\cdot\}$ | indicator function |
| $\mathcal{A}$ | candidate AP set |
| $\mathcal{S}_{i}$ | Set of STAs associated with AP $i$ before the joining STA selects any AP |
| $\pi$ | stationary distribution of Markov Chain for backoff modeling |
| $i$ | index for AP |
| $j, k$ | index for STA. $j$ is usually used for the joining STA |
| $m$ | $m$ th PPDU transmission |
| $n$ | $n$th MSDU retry state |
| $A_{i}(m)$ | the event that the $m$ th PPDU sent by AP $i$ to STA $j$ is successful |
| $C W(n)$ | contention window size on retransmission state $n$ |
| $C W_{\max }$ | maximum CW size defined in 802.11 |
| $C W_{\text {min }}$ | minimum CW size defined in 802.11 |
| $e T M R(i)$ | expected true MAC rate from AP $i$ to the joining STA |
| $e T P(i)$ | expected throughput from AP $i$ to the joining STA |
| $e T P_{n}(i)$ | expected throughput from AP $i$ to the joining STA estimated using $t_{\text {alloc }}^{n}(i)$ |
| $e T P_{r}(i)$ | expected throughput from AP $i$ to the joining STA estimated using $t_{\text {alloc }}^{r}(i)$ |
| $e T P_{t}(i)$ | expected throughput from AP $i$ to the joining STA estimated using $t_{\text {alloc }}^{t}(i)$ |
| $L_{i}(m)$ | MAC payload (MSDU) size in bits on $m$ th transmission from AP $i$ to STA $j$ |
| $L$ | maximum MAC payload (MSDU) size |
| $L_{\text {MAC }}$ | MAC frame size in bits |
| $L_{\text {PHY }}$ | preamble and PLCP header size in bits |
| $N$ | packet retry limit |
| $N_{\text {assoc }}(i)$ | The number of STAs that are already associated with AP $i$ |
| $P(i)$ | transition matrix for modeling BEB from AP $i$ to the joining STA |
| $P_{C}$ | total collision probability |
| $P_{e}$ | channel error probability |
| $P_{L}$ | total packet loss probability |
| $P_{S}$ | packet success probability |
| $R_{\text {MAC }}$ | MAC modulation rate |
| $R_{\text {PHY }}$ | PHY modulation rate |
| $R(i)$ | The MAC rate from AP $i$ to the joining STA |
| $R_{i}(k)$ | The MAC rate from AP $i$ to STA $k$ |
| $T_{\text {ACK }}$ | time to transmit ACK packets |
| $T_{\text {DIFS }}$ | DIFS duration defined in IEEE 802.11 |
| $T_{\text {EIFS }}$ | EIFS duration defined in IEEE 802.11 |
| $T_{\text {SIFS }}$ | SIFS duration defined in IEEE 802.11 |
| $T_{\text {slot }}$ | slot time duration defined in IEEE 802.11 |

Table A.3. Symbols Continued

| Symbol | Meaning |
| :---: | :---: |
| $t(i)$ | average time that AP $i$ allocated to STA $j$ for one PPDU transmission |
| $t_{\text {alloc }}(i)$ | The potential percentage of channel time that AP $i$ can allocate to the joining STA |
|  | $t_{\text {alloc }}(i)$ estimated by using number of associated STAs to AP $i$ |
|  | $t_{\text {alloc }}(i)$ estimated by using MAC rates of associated STAs to AP $i$ |
| $t_{\text {alloc }}^{t}$ | $t_{\text {alloc }}(i)$ estimated by calculating the average waiting time between consecutive unique MSDUs from AP $i$ to the joining STA |
| $\overline{t_{\mathrm{b}}}(i, n)$ | average backoff duration on $n$th retry state for PPDUs from AP $i$ to STA j |
|  | average backoff duration for PPDUs from AP $i$ to STA $j$ |
| $t_{h}(i)$ | time to transmit PHY layer pramble, PLCP header, MAC header and MAC CRC from AP $i$ |
| $t_{i}(m)$ | the time that AP $i$ takes to transmit $m$ th PPDU to STA $j$ |
|  | average MAC payload (MSDU) tx time from AP $i$ to STA $j$ |
| $t_{\text {protocol }}$ | the overhead introduced by the 802.11 protocol for a single PPDU transmission, including inter-frame spacing, backoff time, and possible ACK time |
| $t_{O}$ | average overhead time associated with one MSDU from AP $i$ to STA $j$ |
| $t_{O H}(i, n)$ | average overhead time from AP $i$ to STA $j$, when the MSDU is in $n$th retry state. |
| $t_{h}(i)$ | time to transmit the PHY layer preamble, the PLCP header, the MAC header, and MAC CRC, from AP $i$ to STA $j$ |
| $t_{w}^{\text {after }}(i)$ | The average waiting time between consecutive unique MSDUs for traffic from AP $i$ to the joining STA |
| $t_{w}(i, k)$ | The average waiting time between consecutive unique MSDUs for traffic from AP $i$ to STA $k$ |
| $t_{\text {co }}$ | Time duration to collect BI signals. |
| $t_{w}^{\text {before }}(i)$ | The minimum average waiting time between consecutive unique MSDUs for traffic from AP $i$ to STAs that are already associated with AP $i$, before the joining STA selects any AP |
| $t_{\text {text }}^{\text {total }}$ (i) | total idle time at AP $i$ for a duration of $t_{\text {count }}$ |
| $t_{\text {text }}(i)$ | minimum average idle time at AP $i$ for a duration of $t_{w}^{\text {before }}(i)$ |
| $t_{u}(i)$ | average time spend by AP $i$ to send one MSDU to the joining STA, until the MSDU is successful or dropped due to exceeding retransmission limit |
| $T_{u}(i)$ | random variable for the time spent by AP $i$ to send one MSDU to the joining STA, until the MSDU is successful or dropped due to exceeding retransmission limit |
| $X_{i}$ | random variable for the number of retransmissions required to send one unique MSDU from AP $i$ to the joining STA |


[^0]:    ${ }^{1}$ Nonetheless, we speculate the optimal throughput for the joining STA to eventually reach diminishing return when the number of APs exceeds a certain threshold. This is because as the number of APs increases in a fixed area, the average distance between APs decreases, and the spatial frequency reuse of this WLAN decreases, which means more APs have to contend for the same amount of TXOPs. With fewer TXOPs for each AP, the throughput for each STA is likely to decrease. With proper AP selection, the threshold of diminishing return on average throughput for the joining STA is postponed to larger number of APs.

