

# Fully Integrated CMOS Power Amplifier

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Fully Integrated CMOS Power Amplifier

by

Gang Liu

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## **Abstract**

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Doctor of Philosophy in Electrical Engineering and Computer Sciences

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Professor Ali M. Niknejad, Co-chair

Professor Tsu-Jae King Liu, Co-chair

Today's consumers demand wireless systems that are low-cost, power efficient, reliable and have a small form-factor. High levels of integration are desired to reduce cost and achieve compact form factor for high volume applications. Hence the long term vision or goal for wireless transceivers is to merge as many components as possible, if not all, to a single die in an inexpensive technology. Therefore, there is a growing interest in utilizing CMOS technologies for RF power amplifiers (PAs). Although several advances have been made recently to enable full integration of PAs in CMOS, it is still among the most difficult challenges in achieving a truly single-chip radio system in CMOS. This is exacerbated by supply voltage reduction due to CMOS technology scaling and on-chip passive losses due to the conductive substrate used in deep submicron CMOS processes.

Efficiency is one of the most important metrics in the design of power amplifiers. Conventional designs give maximum efficiency only at a single power level, usually near the maximum rated power for the amplifier. As the output power is backed off from that single point, the efficiency drops rapidly. However, power back-off is inevitable in today's wireless communication systems.

To date, there has been relatively little research on the design of a CMOS PA targeting good average efficiency. A new transformer combining architecture, which is suitable in designing highly efficient PAs in CMOS processes, is proposed to address this issue. A prototype was implemented with only thin-oxide transistors in a 0.13- $\mu\text{m}$  RF-CMOS process to demonstrate the concept. Experimental results validate our concept and demonstrate the feasibility of highly efficiency, fully integrated power amplifiers in CMOS technologies.

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# Chapter 1: Introduction

- 1.1 Recent developments of wireless communication technologies
- 1.2 Motivation
- 1.3 Overview of the work and its contribution
- 1.4 Organization of the thesis
- 1.5 References

## 1.1 Recent developments of wireless communication technologies

Recently the wireless communication industry has seen enormous change. The fast development of global wireless communications technology has made it the center of industrial development in the 21<sup>st</sup> century.

The wave started with cellular phones. Radio phones have a long history that stretches back to the 1950s, with hand-held cellular devices being available since 1983. In fact, some of the important fundamentals used in the mobile networks today were proposed in a patent granted on August 11, 1942 [1.1]. One of the inventors, Hedy Lamarr<sup>1</sup> was actually an actress in Hollywood. She patented an idea (Figure 1.1) about radio control with the concept of “frequency hopping”, with her friend George Antheil, a composer.

In the 1980s, cellular phones were first introduced. It was based on cellular networks with multiple base stations located close to each other, and protocols for the automated handover between two cells when phones moved from one cell to another.

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<sup>1</sup> In 1942, at the height of her Hollywood career, Hedy Lamarr patented a frequency-switching system for torpedo guidance that was two decades ahead of its time.

Analog transmission was used in every single system, with the support voice transmissions. These systems later became known as first generation (1G) mobile phones, such as Advanced Mobile Phone Service (AMPS), Nordic Mobile Telephone (NMT), and Radio Telefono Mobile Integrato (RTMI). Phones of those days were much larger than the ones that we use nowadays. They were sometimes better known as “brick phones” (Figure 1.2 (a)). In the 1990s, second generation (2G) mobile phone systems such as Global System for Mobile Communication (GSM), Digital AMPS (IS-54 and IS-136 “TDMA”) and IS-95 (CDMA) began to be deployed by service carriers. The availability of low-cost digital circuits paved the way to adopting advanced digital modulation schemes. Due to the increased level of usage, service providers started to add more base stations which led to higher density and smaller size of cellular sites. With other technological breakthroughs such as more advanced batteries and more power-efficient electronics, larger “brick phones” were replaced with tiny hand-held devices (Figure 1.3. (b)). Not long after the introduction of the second generation systems, efforts were initiated to develop third generation (3G) systems. Before the debut of third generation systems, 2.5G systems were developed as a stepping stone. 2.5G systems such as General Packet Radio Service (GPRS), CDMA and Enhanced Data rates for GSM Evolution (EDGE), can provide some benefits of third generation systems and use some of the existing second generation network infrastructures. At the beginning of the 21<sup>st</sup> century, third generation mobile phone systems such as Universal Mobile Telecommunication System (UMTS), CDMA 1xEV and Time Division-Synchronous Code Division Multiple Access (TD-SCDMA) have now begun to be available. High

data rates are guaranteed to provide services such as live streaming of video and music downloading.

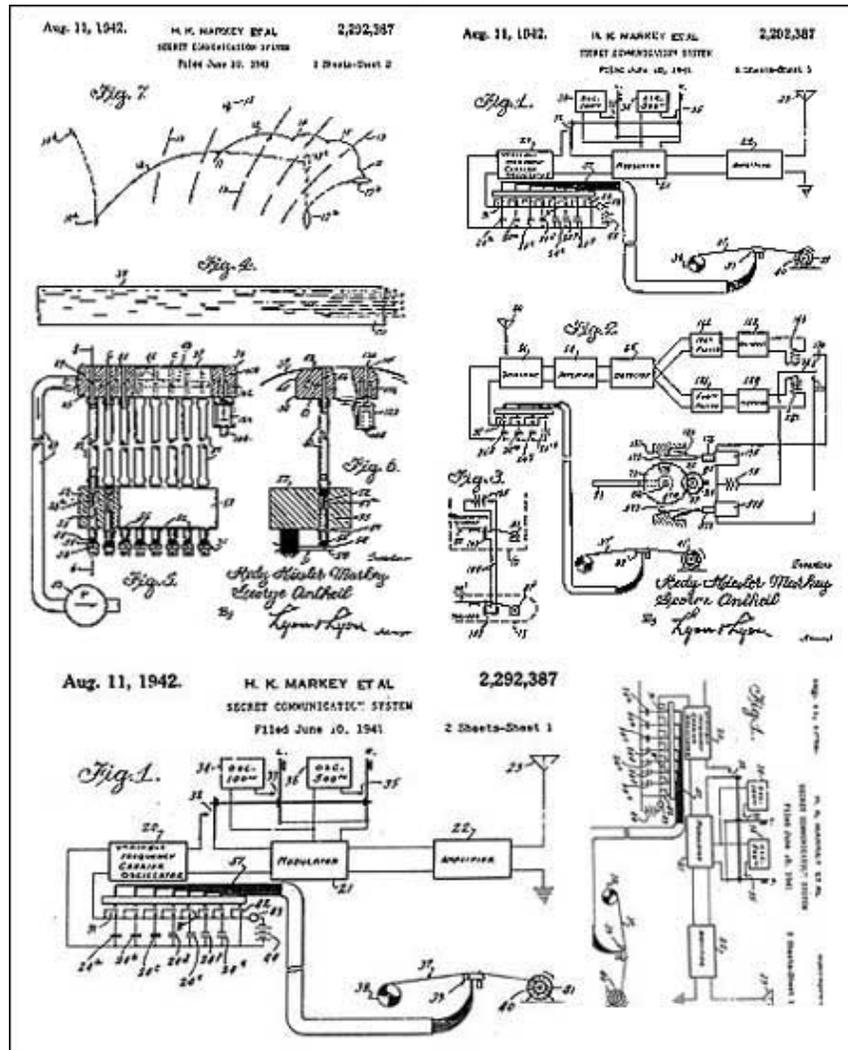


Figure 1.1: Two pages of drawings from Lamar and Antheil's patent. Markey is the name of Hedy Lamarr's second of six husbands.

In less than twenty years, mobile phones have gone from rare and expensive pieces of equipment mainly used for business to a pervasive personal item. In many countries, mobile phones now outnumber land-line telephones, with most adults and

many children now owning mobile phones. It is not uncommon for young adults to simply own a mobile phone instead of a land-line phone for their residence. In some developing countries, where there is little existing fixed-line infrastructure, the mobile phone has become widespread. By the end of 2005, the global mobile phone market grew to 2 billion subscribers. Yet this market is still growing (Figure 1.3).



(a)



(b)

Figure 1.2: (a) Martin Cooper was making a phone call with a Motorola DYNATAC (1973). This phone weighed around 2.5-lb, with 35 minutes talk time. (b) The famous “Can you hear me now?” guy was talking on a Motorola V325 (2005). This phone weighs 4.1-oz, with 200 minutes talk time and built-in video camera.

Besides mobile phones, other wireless communication markets are also growing explosively. Among them, the most well-known systems are probably applications related to Wireless Local Area Network (WLAN). The WLAN worldwide service revenues are projected to reach \$9.5 Billion by 2007 (source: Alexander Resources). The looming global rollout of WiMAX will push its way into the 3G market and generate \$53 billion in mobile revenue in 2011 (source: TelecomView).

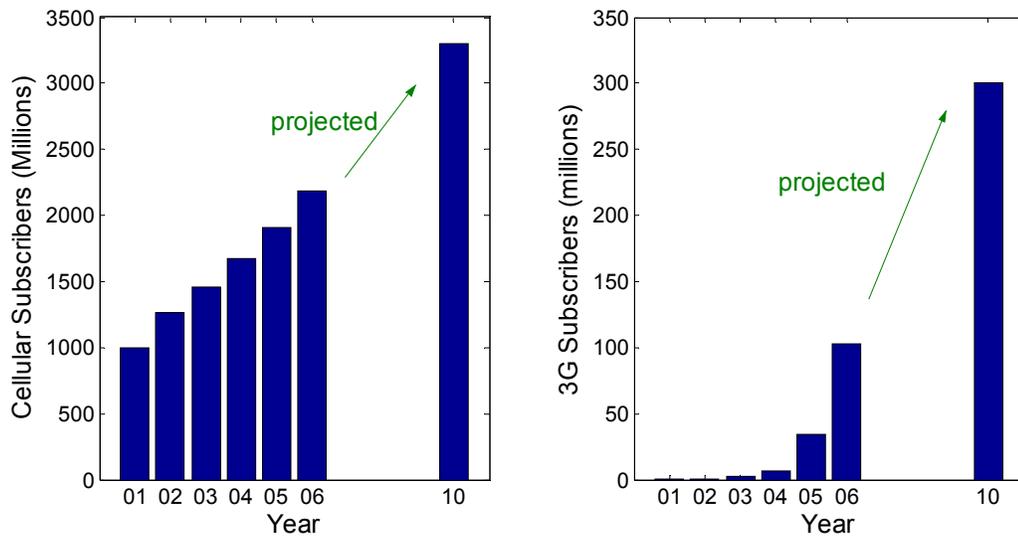


Figure 1.3: (a) Recent and projected worldwide cellular phone subscribers. (b) Recent and projected 3G service subscribers (sources: ITU & Micrologic Research).

Concurrent with the developments in the wireless communication industry, there are several tremendous advancements in semiconductor technologies. In fact, those advancements build up the solid foundation for the proliferation of wireless communication systems. Among them, the most significant progress made is in CMOS technologies. The remarkable characteristic of CMOS transistors is that their speed increases, while they consume less power per function in digital circuits, and cost decreases as their size is reduced.<sup>2</sup>

As technologies advance, today's savvy consumers demand wireless systems that are low-cost, power efficient, reliable and have a small form-factor. High level integration has been proven in practice to be an effective way to reduce cost and achieve compactness simultaneously for high volume applications. Hence the long term vision or

<sup>2</sup> In 1954, the average price of a transistor was \$5.52. In 2004, the average cost was 191 nano-dollars, or 191 billionth of a dollar.

goal for wireless transceivers is to merge as many components as possible, if not all, on to a single die using an inexpensive technology. CMOS was first invented purely for digital integrated circuits. Gradually CMOS became the predominant technology in digital integrated circuits since its invention. This trend is essentially because manufacturing cost, energy efficiency, operating speed and occupied area have benefited and will continue to benefit from the dimension scaling of CMOS devices that comes with every new technology generation. All the features mentioned above have allowed for integration density not possible for other technologies such as silicon bipolar technology. Besides, radio frequency (RF) and microwave integrated circuits implemented in CMOS [1.2-1.4] are making a strong appearance in the chip industry. It is believed that CMOS technology is probably the only viable vehicle at present time to fulfill the dream of an entire system on a single die at the present time.

## **1.2 Motivation**

Although it was certainly a non-trivial task to realize system-on-chip (SoC), engineers from industry together with researchers from universities have figured out ways to put the almost entire system on a single chip [1.5, 1.6]. Yet there is still one piece missing on the integration chart, the power amplifiers (PAs). Today, almost all power amplifiers in market are manufactured with III-V compound semiconductors. This is necessary because high output power and high power efficiency are required power amplifier specifications in various applications. It is very difficult to satisfy those requirements with CMOS technologies because of fundamental limitations. On the other hand, due to the high manufacturing cost associated with those exotic III-V technologies,

as well as the incapability of providing complete system solutions, there are growing interests to look at CMOS technology as an alternative for RF power amplifiers. Obviously, the ultimate goal is to put the PA, transceiver IC, digital baseband and power management module on a single piece of silicon.

The first CMOS RF power amplifier that could deliver hundreds mW power was reported in 1997, implemented in a single-ended configuration with a 0.8- $\mu\text{m}$  CMOS technology [1.7]. The power amplifier could provide 1-W of output power at 824~849MHz with 62% drain efficiency using 2.5-V supply. The impedance transformation network was built with off-chip passive components. Single-ended configuration was the designers' first choice when power amplifiers were implemented with discrete transistors. From the integration perspective, it is ill-suited for full integration since it increases the possibility of coupling with other components on-chip. The first CMOS RF differential amplifier that could deliver over 1W at GHz range was reported in 1998, implemented with a 0.35- $\mu\text{m}$  CMOS technology [1.8]. It leveraged high-Q bond-wires as inductors for the matching network, and micro-strip balun for differential-to-single-ended conversion at output. Using injection locking technique to reduce the input drive requirements, the power amplifier could transmit 1-W power at 2GHz with 41% combined power added efficiency using 2-V supply. Since then, there have been quite a few publications on CMOS RF power amplifiers [1.9-1.13]. They all rely on off-chip components such as bond-wires, off-chip inductors, off-chip capacitors to implement low-loss impedance transformation network, and thick-gate-oxide

transistors<sup>3</sup> to avoid overstressing devices. Since 2G systems were “THE” system at that time, the majority of published CMOS PAs are nonlinear power amplifiers.

Driven by the demands from customers, continuing efforts have been taken to look into fully integrated linear CMOS RF power amplifiers. Although there are some previous publications on fully integrated RF PAs, they were implemented with LDMOS transistors on a SOI substrate [1.14], or with SiGe HBT transistors in a SiGe BiCMOS technology [1.15], and other exotic technologies. Without using power combining techniques, reported fully integrated CMOS power amplifier with 55% drain efficiency could only achieve 85-mW power at 900-MHz [1.16], or could transmitter 150-mW at -1-dB compression point at 5-GHz but only with 13% power added efficiency [1.17]. If we could combine power from several efficient, small power amplifiers, medium-to-high output power could be achieved with good power efficiency.

Various methods have been used to split and combine RF signals. Among them, transformers have been widely used as means for combining RF power [1.18]. However, one serious problem associated with conventional on-chip transformers in CMOS technologies is high insertion loss which directly translates into loss in power efficiency. Therefore, this approach has only been adopted to implement inter-stage matching [1.19]. Circular geometry distributive active transformer, known as DAT, was proposed to overcome high insertion loss problem in on-chip transformers [1.20]. It functions as an eight-way power combiner with good efficiency at peak output power, implemented with 0.35  $\mu\text{m}$  CMOS transistors [1.21]. Despite many advantages of this approach, the circuit geometry DAT still has some problems inherently from its structure [1.22, 1.23].

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<sup>3</sup> Thick oxide devices are devices with recommended supply voltage of 3.3-V or 2.5-V.

Besides integration, there is another serious issue associated with PA design which is inherent to conventional PA. It is well known that a PA can only achieve maximum efficiency at peak output power. As output power decreases, efficiency drops rapidly. However, the need to conserve battery power and to mitigate interference to other users necessitates the transmission of power levels well below the peak output power of the transmitter [1.24]. Moreover, since spectrum is a scarce commodity, modern transmitters for wireless communications employ spectrally efficient digital modulations with time varying envelope. Because of these reasons, the PA transmits much lower than peak output power under typical operating conditions.

### **1.3 Overview of the work and its contribution**

To date, there has been relatively little research on the design of a CMOS PA targeting good average efficiency. This work proposes a power combining transformer to address this issue. This transformer provides measures for simple yet elegant power control and average efficiency enhancement by modulating the RF load. The control could be implemented using digital approaches or analog approaches. Average efficiency enhancement with digital control was successfully demonstrated with a fully integrated CMOS PA [1.25].

A prototype was fabricated with only thin-gate-oxide transistors in a 0.13- $\mu\text{m}$  CMOS technology to demonstrate the concept. With 1.2-V supply, it transmits linear power up to 24-dBm (250-mW) with 25% drain efficiency. When driven into saturation, it transmits 27-dBm (500-mW) peak power with 32% drain efficiency. As one of the four amplifiers is turned off for 2.5-dB power back-off from 27-dBm, drain efficiency is

improved from 26.5% to 31.5%, very close to instantaneous drain efficiency at peak power.

To the author's knowledge, this is the first reported fully integrated CMOS power amplifier with only thin-gate-oxide transistors in a state-of-the-art CMOS process. It is capable of transmitting hundreds of mW power. The instantaneous efficiency at peak output power is good, and can be further improved. The simple and elegant average efficiency enhancement technique was successfully demonstrated. The significance of this work is in the following:

1. It proves that fully integrated CMOS power amplifier is feasible and will continue to be feasible as scaling continues.
2. A power combining technique is proposed based on transformers. Load modulation can be implemented with digital switches or through outphasing combining. Extra circuitry overhead is minimum, especially for the digital approach with switches. The ability of active load pull greatly enhances the efficiency at power back-off. Other advantages, such as noise reduction or linearity improvement, could also be obtained, benefiting from parallelism.
3. It demonstrates that linearity required by advanced modulation schemes can be achieved with deeply scaled CMOS technologies. As digital signal processing power increases with the scaling of CMOS, it is the author's belief that it will further improve system linearity with little power overhead and cost penalty.

4. Quite rare in power amplifier design, the measurements and simulation results match pretty well. Therefore, the design methodology used in this work has been proven to be effective<sup>4</sup>.

## **1.4 Organization of the thesis**

Chapter 2 presents an overview of power amplifiers, introducing transconductance power amplifiers, switching power amplifiers, and metrics to evaluate power amplifiers' performance. Chapter 3 overviews some prevalent technologies for RF power amplifier, compare characteristics of CMOS technologies with other technologies. The trend in supply voltage as technologies advance is touched upon. At the end, fundamental limitation of CMOS technologies and the impact of scaling for RF power amplifiers are studied. Chapter 4 presents various existing techniques to generate high output power with low voltage devices. Then the proposed power combining transformer will be introduced. Its advantages and potential applications are examined in detail. In Chapter 5, the design of impedance matching network, especially transformer, is analyzed. It will give readers a clear picture of what issues should be addressed when designing on-chip power combining transformer. Chapter 6 presents a detailed description of design process of the prototype that proves the concept of the power control and average efficiency enhancement technique. Experimental results are shown with comparison to simulation results. At last, chapter 7 concludes this work and gives some suggestion for future research.

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<sup>4</sup> The author is very indebted to the excellent device models provided by the foundry.

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## **Chapter 2: Fundamentals of Power Amplifiers**

- 2.1 An overview of classifications and specifications of PAs
- 2.2 Efficiency of PAs
- 2.3 Linearity of PAs
- 2.4 Summary
- 2.5 References

### **2.1 An overview of classifications and specifications of PAs**

The real world is “analog” in nature. PAs are used, ideally, to amplify signals without compromising signal integrity, so that information could be transmitted into the media and recovered by the recipient. PAs may be categorized in several ways, depending on different criteria. Usually they are classified according to their circuit configuration and operation conditions into different classes, from class A to Class S. Since most of the subjects in this section have been covered comprehensively in many textbooks, what is presented in this section is just a very brief overview. Interested readers are encouraged consult other literature, such as [2.1-2.3], to probe further.

#### **2.1.1 Class-A, AB, B, and C power amplifiers**

These four types of power amplifiers have similar circuit configuration, distinguished primarily by biasing conditions (Figure 2.1). A class-A power amplifier, in principle, works as a small-signal amplifier. It is probably the only “true” linear amplifier, since it amplifies over the entire input cycle such that the output is an exact

scaled-up replica of the input without clipping. This “true” linearity is obtained at the expense of wasting power. To improve efficiency without sacrificing too much linearity, the concept of “reduced conduction angle” was proposed. The idea is to bias the active devices<sup>5</sup> with low quiescent current and let the input RF signal to turn on active devices for part of the cycle. As the conduction angle shrinks, the amplifier is biased from class-AB, to class-B and eventually class-C. Regardless of conduction angle, active devices are used as current sources. Therefore, they are often referred to as “transconductance” PAs.

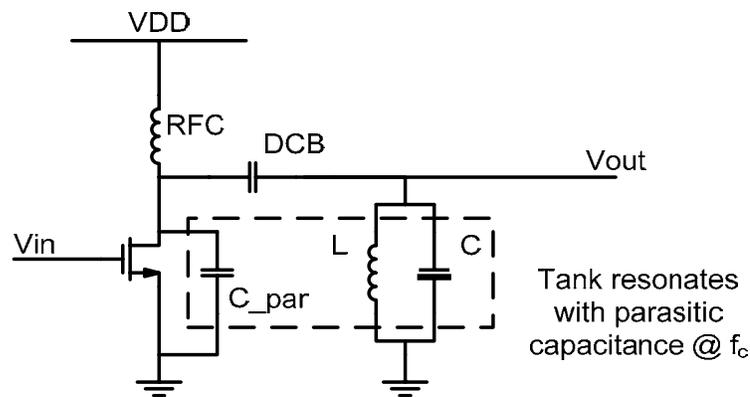


Figure 2.1: A generic topology for class-A, AB, B, and C power amplifiers

Using a class-A power amplifier with 1.2-V supply voltage as an example, ideal maximum output power delivered to the 50-Ω antenna is calculated as:

$$P_{out} = \frac{V_{dd}^2}{2 \cdot R_L} = \frac{1.2^2}{2 \cdot 50} = 14.4mW$$

<sup>5</sup> Power amplifiers can be either designed in single-ended or pseudo-differential topology. *pl.* are used to describe amplifiers in text, though illustrations are shown in single-ended topology.

Obviously this output power is not high enough for most of the applications today. Therefore impedance transformation is necessary. For example, in order to transmit 300-mW power, the 50-Ω load should be transformed to:

$$R_L = \frac{V_{dd}^2}{2 \cdot P_{out}} = \frac{1.2^2}{2 \cdot 0.3} = 2.4\Omega$$

In real practice, due to various losses,  $R_L$  need to be even lower for the same output power which poses a serious challenge. This issue will be revisited.

### 2.1.2 Class-D power amplifiers<sup>6</sup>

A class D amplifier is composed of a voltage controlled switch and a filtering tank. Figure 2.2 shows a voltage switching class D amplifier. The output tuned network is tuned to the fundamental frequency. It will thus have negligible impedance at fundamental frequency and high impedance at harmonic frequencies. The analysis of such an amplifier is very straightforward due to the simple drain voltage waveform. In an ideal situation, the drain efficiency of a class-D amplifier reaches 100% as other switching type PAs.

### 2.1.3 Class-E power amplifiers

Class-E PA stands out from other highly efficient switching PAs because parasitic capacitances of active devices may be absorbed into wave-shaping/matching networks. A simplest form of class-E PAs is shown in Figure 2.3. During operation, the waveforms

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<sup>6</sup> The letter D does not stand for “digital”, even though active devices are operated as switches. The letter D is used to designate this type of amplifier simply because “D” is the next letter after “C”.

of drain current and voltage are shaped such that they do not overlap. Furthermore, the voltage will decrease gradually to zero before the active device turns on. This avoids charging/discharging capacitors at the drain, thus improve efficiency. However, the class-E PA has its disadvantage in terms of peak voltage.

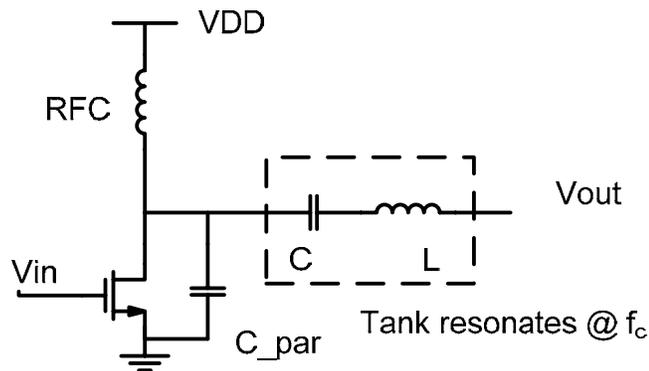


Figure 2.2: A voltage switching class-D amplifier

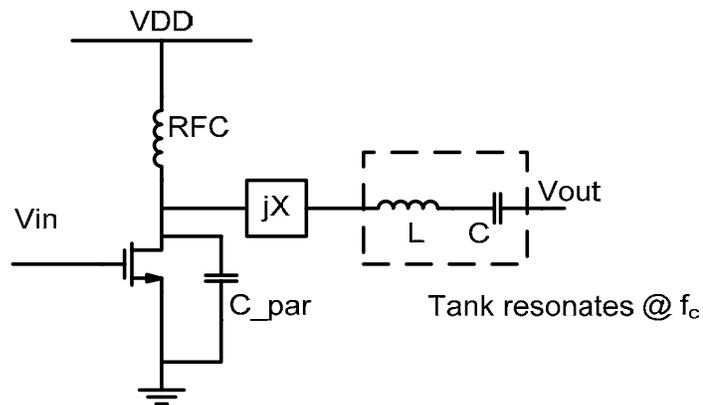


Figure 2.3: A simple class-E amplifier

### 2.1.4 Class F power amplifiers

Class-F is characterized by a load network that has resonance at one or more harmonic frequencies as well as at the fundamental frequency (Figure 2.4). To the author's knowledge, class-F was first proposed to improve the efficiency of overdriven transconductance amplifiers. Therefore, the active devices typically operate as a transconductor (or a current source) as those in transconductance amplifiers. However, if the input drive is large, active devices will behave as switches just like those in switching amplifiers. In practice with lumped elements, it is rare to see class-F amplifiers with tuned harmonics higher than the 5<sup>th</sup> harmonic, due to the complexity of a waveform shaping network.

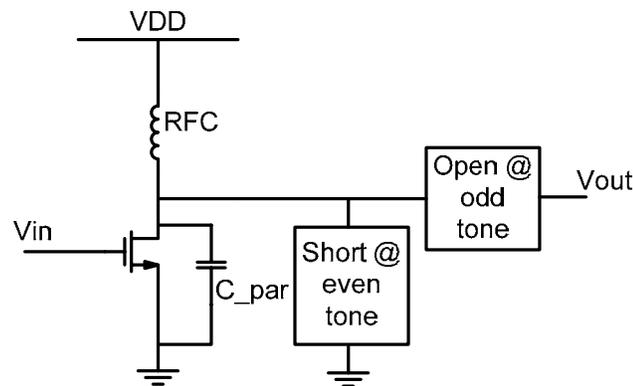


Figure 2.4: A class-F power amplifier with tuned harmonics for waveform shaping

### 2.1.5 Class-G and Class-H power amplifiers

Class-G amplifier is just a more efficient version of transconductance power amplifiers. This type of amplifier switches supply rails when necessary. This results in an overall improvement in efficiency for signals which do not continuously require the

higher voltage supply. Class-H amplifiers are similar to class-G, which takes the class-G design one step further. Instead of discretely switching supply rails, the power supply is modulated by the input signal, to provide just enough voltage for optimum efficiency. Sometime, it is referred as “kahn” technique or “envelope following” technique.

### **2.1.6 Class-S power amplifiers**

Class-S PAs looks like Class-D PAs, with one difference. The input to a Class-D PA has 50% duty cycle. Thus a standalone class-D PA cannot be used for modulation schemes with amplitude modulation. Class-S, however, may be used for amplitude modulation with excellent efficiency. The basic principle involves the creation of a rectangular waveform of variable duty-cycle, such that different pulse widths (duty cycles) produce different average outputs to form the desired waveform<sup>7</sup>.

### **2.1.7 Hybrid class power amplifiers**

The classes of power amplifiers have their advantages and disadvantages respectively. To overcome some limitations and further improve amplifier performance, several hybrid classes were proposed. Among them, a class-BD power amplifier [2.4] and a class-E/F family of power amplifiers [2.5] are of particular interest. The Class-BD power amplifier has a linear transfer characteristic, and efficiency higher than that of a class-B power amplifier with the same peak output power. The class-E/F family of amplifiers has class-E features such as incorporation of the transistor parasitic

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<sup>7</sup> The working principle of class S is somewhat similar to sigma-delta modulator.

capacitance into the circuit. Additionally, some number of harmonics may be shaped in the fashion of inverse class-F in order to achieve desirable voltage and current waveforms for improved performance.

### **2.1.8 Performance metrics of power amplifiers**

There are many metrics used to evaluate the performance of power amplifiers. Some of the metrics are specified by regulations or standards. Other metrics are not specified, though they are often used for comparing different power amplifiers for the same application. Depending on the type of applications, gain, output power, ruggedness, linearity, efficiency, size and/or noise could be the metrics that differentiate different amplifiers. Among them, efficiency and linearity are probably the most commonly used metrics. Those two metrics are correlated in the design process, and present two inherent problems to power amplification of amplitude modulated RF signals. In the following sections of this chapter, those two metrics will be studied in detail.

## **2.2 Efficiency of Power Amplifiers**

One of the most important metrics for a power amplifier is its power efficiency. It is a measure of how well a device converts one energy source to another. What does not get converted is dissipated into heat which is almost universally a bad product of energy conversion. In RF circuit design, power amplifier efficiency is calculated in three

ways with wide acceptance. The first one is drain efficiency<sup>8</sup>, usually denoted as  $\eta_D$ . This is defined as the ratio of output power  $P_{OUT}$  to DC power consumed from supply  $P_{SUPPLY}$ :

$$\eta_D = \frac{P_{OUT}}{P_{SUPPLY}}$$

Drain efficiency does not take input power into account. If the gain is high, it is safe to ignore the effect of input power. However, in RF power amplifiers, the input power can sometime be substantial, therefore measures that include the effect of input power are necessary. Power added efficiency (PAE), denoted as  $\eta_{PAE}$ , is the most common used measure which takes input power into account. It is calculated as the ratio of the difference between output power  $P_{OUT}$  and input power  $P_{IN}$  to DC power consumed from supply  $P_{SUPPLY}$ :

$$\eta_{PAE} = \frac{P_{OUT} - P_{IN}}{P_{SUPPLY}}$$

If the gain of the amplifier is known, PAE can be expressed in terms of the gain  $G$  and drain efficiency  $\eta_D$ :

$$\eta_{PAE} = \frac{P_{OUT} - P_{IN}}{P_{SUPPLY}} = \frac{P_{OUT} \left(1 - \frac{1}{G}\right)}{P_{SUPPLY}} = \eta_D \cdot \left(1 - \frac{1}{G}\right)$$

If the gain is high, PAE approaches drain efficiency. In a chain of cascaded amplifiers, if each amplifier has the same PAE, then the PAE of the entire chain will be exactly the same as the PAE of an individual amplifier. A less frequently used measure is called

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<sup>8</sup> Drain efficiency gets its name from FET devices, though it probably should be called collector efficiency when BJT devices are used.

total efficiency, denoted as  $\eta_{TOTAL}$ . It is calculated as the ratio of output power  $P_{OUT}$  to the sum of input power  $P_{IN}$  and DC power consumed from supply  $P_{SUPPLY}$ :

$$\eta_{TOTAL} = \frac{P_{OUT}}{P_{IN} + P_{SUPPLY}}$$

In fact, total efficiency is the measure that makes the most sense from a thermodynamic point of view. This can be seen by noting that the total dissipated power is simply a function of the output power  $P_{OUT}$  and total efficiency  $\eta_{TOTAL}$ . This measure can be used to evaluate the effectiveness of an amplifier and estimate heat removal requirements. Nonetheless, PAE is still the most popular measure in industry. One point that should be noted here is that all three measures mentioned above are for instantaneous efficiency.

Conventional power amplifier designs give maximum efficiency only at a single power level, usually near the maximum rated power for the amplifier. As the output power is backed off from that single point, the efficiency typically drops rapidly. However, back-off situation is inevitable in today's wireless communication. First, the need to conserve battery power and to mitigate interference to other users necessitates the transmission of power levels well below the peak output power. Transmitters will only use peak output power when necessary. Second, the requirement for both high data rate and efficient utilization of the increasingly crowded spectrum necessitates the use of both amplitude and phase modulation schemes. In a number of applications, it is more convenient and robust to use a large number of carriers with low data rates than a single carrier with a high data rate. For example, orthogonal frequency division multiplexing (OFDM) employs multiple carriers with the same amplitude modulation, separated in frequency and codes so that the modulation products from one carrier are zero at the

other carriers in an ideal system. The resultant composite signal has a peak-to-average ratio in the range of 12~17-dB.

Obviously, high instantaneous efficiency at peak output level is certainly desirable. However, what more important is the average efficiency. Or in other words, power amplifiers need to maintain high efficiency over a wide dynamic range. Therefore, average efficiency is a useful measure. Average drain efficiency, denoted as  $\bar{\eta}$ , is calculated as the ratio of average output power  $\overline{P_{OUTPUT}}$  to the average DC power from supply  $\overline{P_{SUPPLY}}$ , depending on both the instantaneous efficiency of the power amplifier  $\eta$  and the probability-density function (PDF) of the signal it's amplifying:

$$\bar{\eta} = \frac{\overline{P_{OUTPUT}}}{\overline{P_{SUPPLY}}}$$

If the PDF of the output power is  $p(P_{OUTPUT})$  is known, average output power is expressed as:

$$\overline{P_{OUTPUT}} = \int_0^{P_{OUT\_MAX}} P_{OUTPUT} \cdot p(P_{OUTPUT}) \cdot dP_{OUTPUT}$$

And average DC power from the supply is expressed as:

$$\overline{P_{SUPPLY}} = \int_0^{P_{OUT\_MAX}} P_{SUPPLY} \cdot p(P_{OUTPUT}) \cdot dP_{OUTPUT}$$

Therefore, average efficiency  $\bar{\eta}$  can be expressed in terms of instantaneous efficiency  $\eta$  and PDF of the output power  $p(P_{OUTPUT})$ :

$$\bar{\eta} = \int_0^{P_{OUT\_MAX}} \eta \cdot p(P_{OUTPUT}) \cdot dP_{OUTPUT}$$

As an example, average drain efficiency of an ideal class-A amplifier is studied. An ideal class-A amplifier has 50% drain efficiency at peak output power,  $\eta_{D\_peakpower}$ . If the input signal consists of two sinusoidal tones of equal amplitude, the average drain efficiency is 25%, half of the drain efficiency at peak output power. This can be generalized for a multi-tone signal consisting of  $N$  sinusoidal tones of equal amplitudes, the average efficiency is:

$$\bar{\eta} = \frac{1}{N} \cdot \eta_{D\_peakpower}$$

If  $N$  is 52, then average drain efficiency is less than 1%. Now let's look at somewhat more realistic OFDM signals with  $N$  sub-carriers. It is fair to assume that the signal power is uniformly distributed over the  $N$  sub-carriers using the same QAM constellation for each one of them. For a large value of  $N$  ( $>30$ ), the CDF of OFDM symbols can be well approximated by that of a two-dimensional complex Gaussian random process, according to the Central Limit Theorem. Consequently, the envelope of such an OFDM signal can be considered as Rayleigh distributed. The PDF of this OFDM signal is shown in Figure 2.5. For comparison, the PDF of a constant amplitude signal is also shown in Figure 2.5. While the average drain efficiency of an ideal class A amplifier for the constant amplitude signal is 50%, the average drain efficiency of such an amplifier for the OFDM signals is only 5%. For most other classes of amplifiers, similar but different level of degradation in average efficiency is inevitable when amplifying signals with amplitude modulation.

This is only part of the problem. In real life, transmitters seldom transmit full output power. The PDF of a single carrier mobile transmitter is shown in Figure 2.6 [2.6]. The PDF of the transmitted power depends on various factors, such as the distance to the

base-station, multi-path, attenuation by surroundings and antenna orientation. In urban environment, output power levels of transmissions are usually between 10~20-dB back-off from the peak value. In suburban environment, peak output power is needed in some scenarios. However, same as in urban environment, output power is usually between 10~20-dB back-off from peak output. And it is quite obvious that if the PA is operated in back-off, average efficiency is reduced even more.

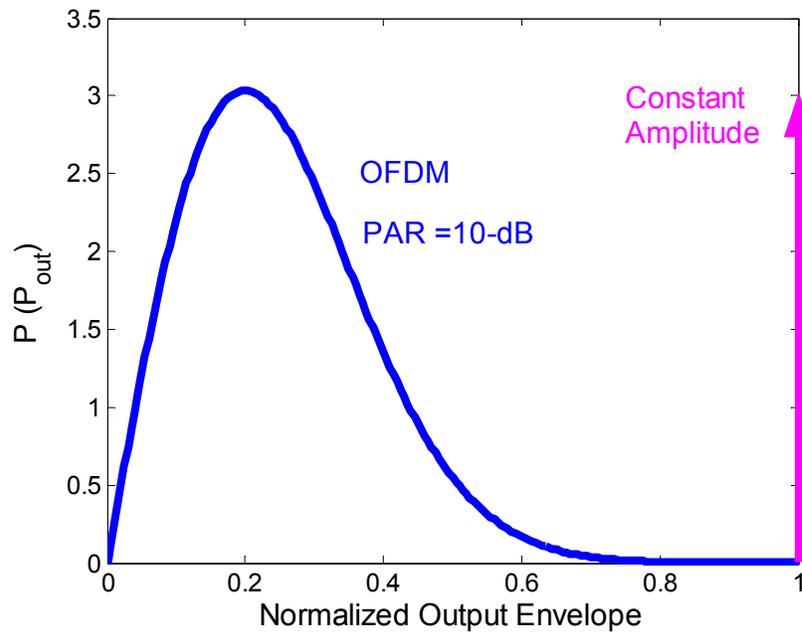


Figure 2.5: PDF of multi-carrier OFDM signals with Rayleigh distribution ( $\sigma=0.2$ ) at its maximum output. The corresponding PAR is approximately 10-dB. In contrast, the constant amplitude signal is always at peak power.

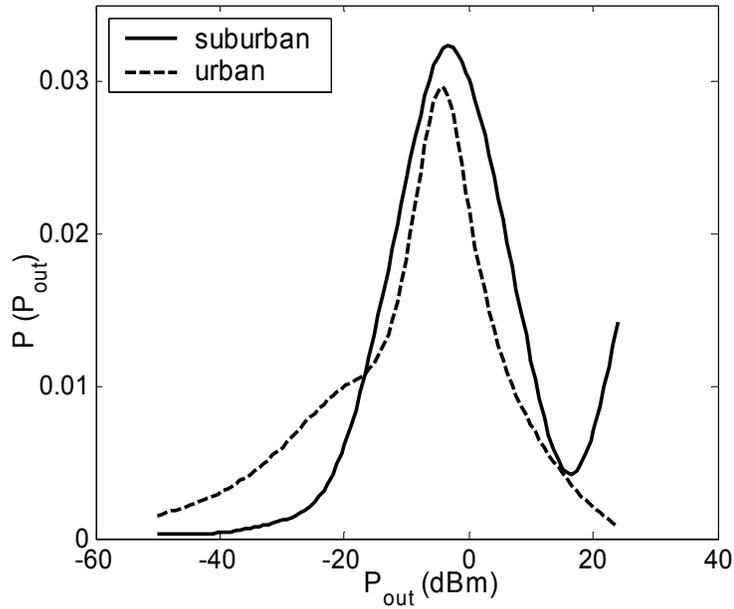


Figure 2.6: Output Power PDF of a single carrier mobile transmitter

Several efficiency enhancement techniques have been proposed to overcome this issue<sup>9</sup>. A brief review will be given here. To begin with, let's study the drain efficiency of a class-A amplifier first:

$$\eta_D = \frac{P_{OUTPUT}}{P_{SUPPLY}} = \frac{1}{2} \cdot \frac{P_{OUTPUT}}{V_{SUPPLY} \cdot I_{DC}}$$

Class-A is used as an example here for simplicity. Similar relationships exist for other classes of power amplifiers. From this simple equation, several ways can be pointed out to increase average efficiency. The basic idea is to design an adaptive power amplifier so that it can self-adjust to optimize efficiency based on the output power requirement:

- a. Dynamic bias: the idea of improving efficiency by changing the amplifier quiescent current is very straightforward. In class-AB mode, the dc average

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<sup>9</sup> Some techniques were proposed in the early days of radio broadcasting. The motivation was to solve the thermal management issue and to lower cost. In wireless communication, the motivation is to extend the battery time in between charging of portable devices.

current varies automatically with output power level. In class-B mode, the dc average current varies according to the square root of output power. As a result, drain efficiency varies proportionally to the square root of output power ( $P_{\text{OUTPUT}}^{0.5}$ ) in class-B mode, while it varies proportionally to  $P_{\text{OUTPUT}}$  in class-A mode. Hence, changing bias conditions as a function of input power can also be used. The limit of this method is set by the tradeoff between tolerance of gain variation and linearity [2.7].

- b. Dynamic supply: drain efficiency,  $\eta_D$ , is a strong function of the supply voltage. It is also possible to vary the dc supply voltage in accordance with the output power level<sup>10</sup>. Switching regulators are probably most suitable for battery-dependent applications because of their high efficiency compared to linear regulators. Furthermore, switching regulators are capable of producing output voltages that are both lower and higher than their input voltages. Implementations have been published many times recently. However, they are limited to narrow band applications [2.8, 2.9]. In addition, noise and intermodulation products from the switching supply need further careful investigation.
- c. Dynamic load: A different approach can be taken to increase the efficiency at power back-off. This can be seen in the equation below:

$$\eta_D = \frac{P_{\text{OUTPUT}}}{P_{\text{SUPPLY}}} = \frac{1}{2} \cdot \frac{V_{\text{OUTPUT}}^2 / R_L}{V_{\text{SUPPLY}} \cdot I_{\text{DC}}}$$

For a given output power,  $V_{\text{OUTPUT}}$  will increase proportionally to the square root of the load impedance. Therefore, load switching can also be employed to enhance the low power efficiency. Doherty amplifier [2.10] and Chireix's [2.11]

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<sup>10</sup> Recall Class G, Class H, Class S power amplifiers

amplifier are examples of this technique. Dynamic switched load technique has also been demonstrated [2.12].

For transconductance power amplifiers, the most desirable solution is to vary two variables simultaneously, such as DC current and supply voltage, or DC current and load.

### 2.3 Linearity of Power Amplifiers

Besides efficiency, another inherent problem of power amplifiers is linearity. All radio systems are required to induce the minimum possible interference to other users. Hence, they must keep their transmissions within the bandwidth allocated and maintain negligible energy leakage outside of the band. If signals are distorted due to nonlinearities, unwanted distortion products present to other users as interference. Furthermore, good linearity is mandated in order to preserve the integrity of the information in transmitted signals. Therefore, modulated signals could be recovered at the receive end.

A fully rigorous distortion analysis of a power amplifier is lengthy and highly mathematical. Instead, a traditional approach to analyze distortions with power series is adopted here<sup>11</sup>. The transfer characteristic of a differential power amplifier is expressed as<sup>12</sup>:

$$s_o(t) = a_1s_i(t) + a_3s_i(t)^3 + a_5s_i(t)^5 + \dots$$

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<sup>11</sup> Full treatment could be found in [2.13]

<sup>12</sup> In wide-band wireless communications, even order distortions are also falling in-band. Differential topology will greatly suppress distortion products from even order terms.

### 2.3.1 AM-AM Conversion

AM-AM conversion is a phenomenon of the nonlinear relationship between amplitude of input and output in all practical power amplifiers. The most commonly used metric for this one is probably -1dB compression point ( $P_{-1dB}$ ). A single sinusoidal input signal is applied to the circuit:

$$s_i(t) = s \cos \omega t$$

So the output is:

$$s_o(t) = a_1 s \cos(\omega_1 t) + a_3 s^3 \cos^3(\omega_1 t) + \dots$$

Consider the fundamental terms:

$$(a_1 s + \frac{3}{4} a_3 s^3 + \dots) \cos(\omega_1 t)$$

Ignore higher order (>3) terms, the gain becomes:

$$G = a_1 (1 + \frac{3}{4} \frac{a_3}{a_1} s^2)$$

If the coefficient  $a_1$  and  $a_3$  have opposite signs, the gain will compress when the input increases. At some point, the gain will be 1-dB lower than the small-signal gain:

$$P_{-1dB,input} = \sqrt{\frac{4}{3} \left| \frac{a_1}{a_3} \right|} \cdot 0.11$$

Another way to look at AM-AM conversion is to look at inter-modulation (IM) products, because IM products will overlay with wanted-signal band in modulated signals. If the input consists of two in-band RF signals with equal amplitude, whose spacing is much smaller than carrier frequency:

$$s_i(t) = s \cos(\omega_1 t) + s \cos(\omega_2 t)$$

the output becomes:

$$\begin{aligned}
 s_o(t) &= a_1 s[\cos(\omega_1 t) + \cos(\omega_2 t)] \\
 &\quad + a_3 s^3[\cos(\omega_1 t) + \cos(\omega_2 t)]^3 \\
 &\quad + a_5 s^5[\cos(\omega_1 t) + \cos(\omega_2 t)]^5 \\
 &\quad + \dots
 \end{aligned}$$

Consider the third-order terms:

$$\begin{aligned}
 &a_3 s^3[\cos(\omega_1 t) + \cos(\omega_2 t)]^3 \\
 &= \frac{a_3 s^3}{4}(\cos 3\omega_1 t + 3 \cos \omega_1 t) \\
 &\quad + \frac{a_3 s^3}{4}(\cos 3\omega_2 t + 3 \cos \omega_2 t) \\
 &\quad + \frac{3}{4} a_3 s^3 [2 \cos \omega_1 t + \cos(2\omega_2 - \omega_1)t + \cos(2\omega_2 + \omega_1)t] \\
 &\quad + \frac{3}{4} a_3 s^3 [2 \cos \omega_2 t + \cos(2\omega_1 - \omega_2)t + \cos(2\omega_1 + \omega_2)t]
 \end{aligned}$$

The products of most interest, in terms of their possible detrimental effects, are the IM products. A typical in-band spectrum is shown in Figure 2.7. The IM side-bands appear on both sides of each tone, at frequency spacing equal to the difference between the two input tones. It should be quite obvious to see the relations between distortion products and spectrum regrowth.

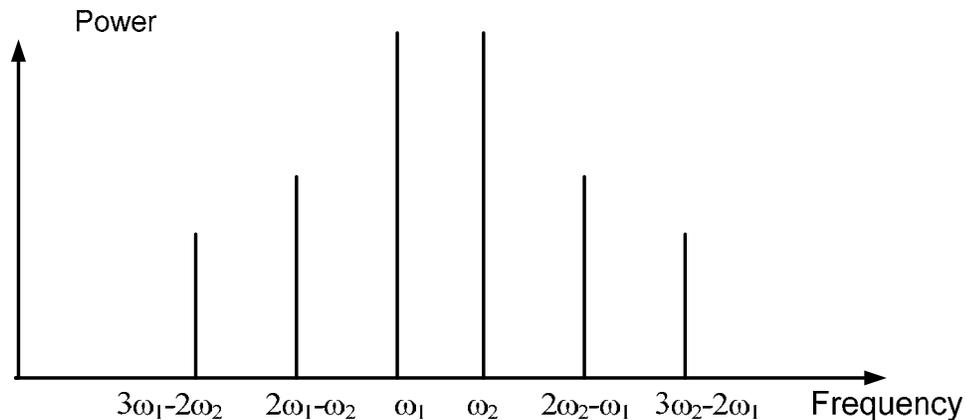


Figure 2.7: The spectrum of two-tone IM products

### 2.3.2 AM-PM Conversion

Comparing to well understood amplitude distortion, phase distortion effects are less seen in literature. This is probably due to the difficulty in AM-PM measurements, and the lack of metrics, such as  $P_{-1dB}$  for AM-AM conversion. Nonetheless, this becomes more and more important with modern modulation schemes<sup>13</sup>. This AM-PM conversion probably can be traced back to the signal-level dependency of parasitic capacitors in active devices, especially MOSFETs input gate capacitance [2.14]. It should not be a surprise that class-AB PAs will have worse AM-PM problems than class-A PAs. Figure 2.8 illustrates typical  $C_{gs}$  characteristic as gate bias varies<sup>14</sup>. As the amplitude of input signal varies, the average capacitance seen at the gate will vary. The amount of variation depends on biasing conditions.

As shown in Figure 2.9, AM-PM phase drift starts at a much lower power level in class-AB mode, well back into what would appear to be linear region based on the amplitude characteristic. This will cause substantial problems in some multi-carrier modulation schemes such as OFDM. This should be kept in mind when designing efficient class-AB PAs.

The linearity metrics for modulated signals are discussed in the following. Typically, narrow-band systems are limited by spectral mask specifications, while wide-band systems are limited by EVM specifications.

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<sup>13</sup> If AM-PM is good, it will require less power back-off for PAs to transmit signals with the same EVM.

<sup>14</sup>  $C_{gd}$  is also important for obvious reasons.

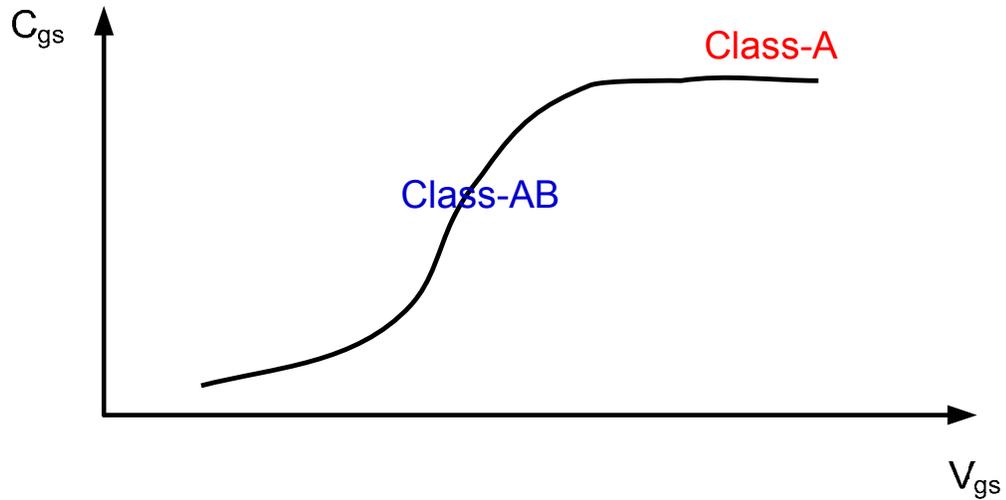


Figure 2.8:  $C_{gs}$  characteristic of typical NMOS devices vs.  $V_{gs}$

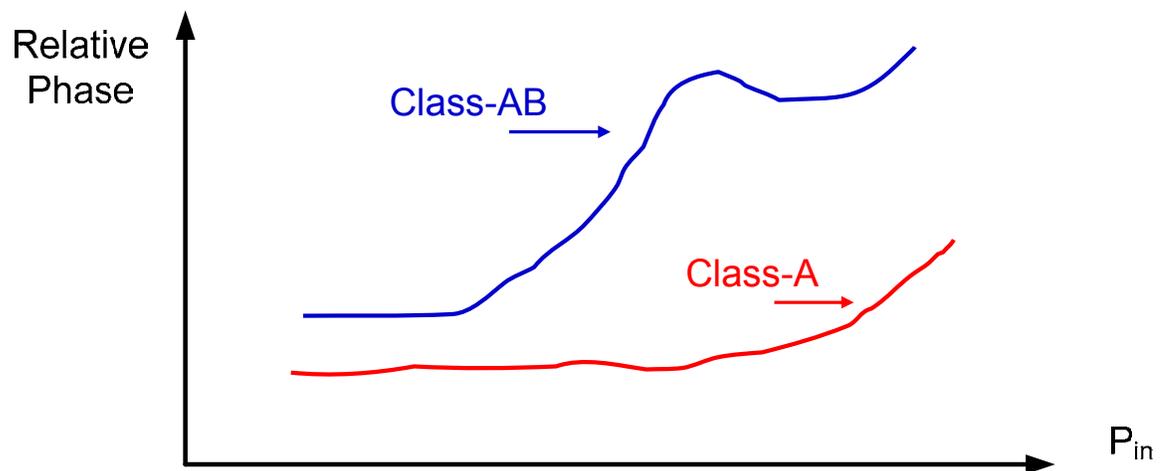


Figure 2.9 Conceptual AM-PM for different bias conditions

### 2.3.3 Adjacent Channel Power Ratio (ACPR)

ACPR is an important linearity metric. It is defined as the ratio of the total power with a certain bandwidth in the channel adjacent to the transmission channel to the total power in the transmission channel. If the modulation scheme is simple, ACPR could be

derived from IM distortion products accurately. However, as the modulation becomes more complex, sinusoidal representation is no longer adequate to address this problem. Table 2.1 gives examples of some current definitions of locations of measurement channels and their bandwidth (BW) for ACPR metric of two CDMA systems. For CDMA IS-95,  $ACPR_{30\_30spec}$  is -42-dBc at first frequency offset and -54-dBc at the second frequency offset.

	CDMA IS-95	WCDMA
Main channel measurement BW	1.23-MHz or 30-kHz	3.84-MHz
Adjacent channel location (from carrier)	$\pm 885$ -kHz	$\pm 5$ -MHz
Adjacent channel measurement BW	30-kHz	3.84-MHz
Alt channel location (from carrier)	$\pm 1.98$ -MHz	$\pm 10$ -MHz
Alt channel measurement BW	30-kHz	3.84-MHz

Table 2.1: Current definitions of locations of measurement channels and their bandwidth for ACPR of two CDMA systems

### 2.3.4 Spectral MASK

A similar metric to ACPR is spectral mask. The power spectral density of a power amplifier is sometimes referred as spectral emission. A spectral mask is generally

intended to reduce the interference by limiting excessive radiation at frequencies beyond the necessary bandwidth. Figure 2.10 shows the spectral mask specified in the GSM/EDGE standard. The graph illustrates the maximum allowed power density, normalized to the power density within the signal band, as a function of the frequency offset from the carrier.

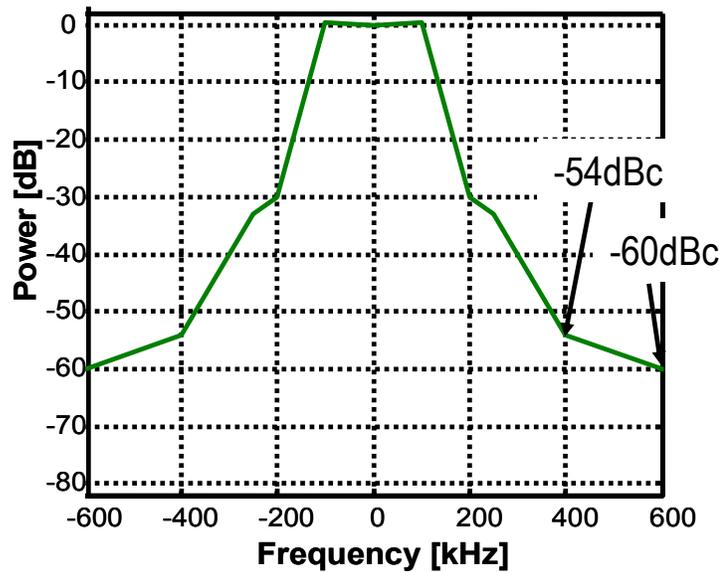
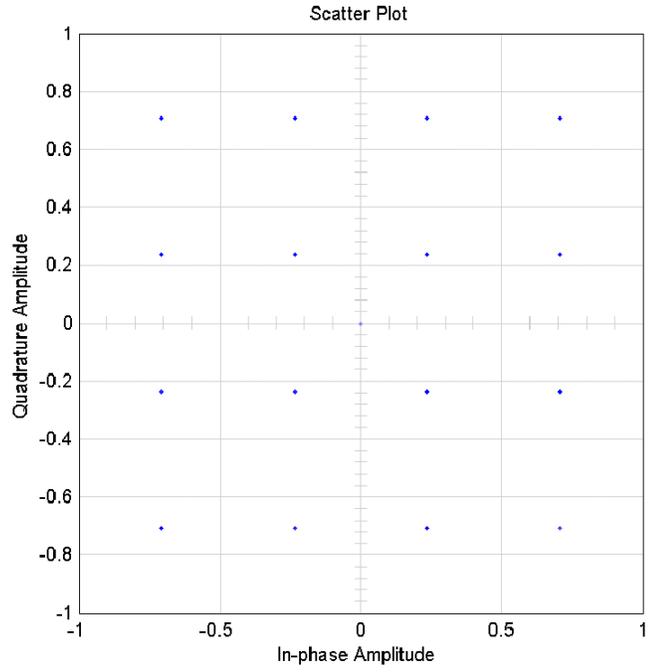


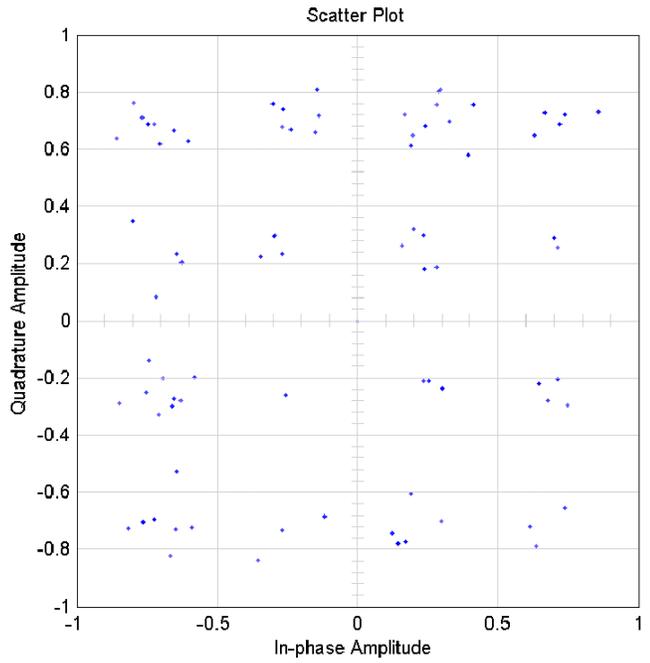
Figure 2.10: GSM-EDGE spectral mask

### 2.3.5 Error Vector Magnitude (EVM)

The EVM is a measure used to quantify the performance of a system with phase-shift modulation. Due to various impairments, the actual constellation points will move relative to the ideal constellation locations. EVM is a measure of how far the actual constellation points are from the ideal locations (Figure 2.11).



(a)



(b)

Figure 2.11: A rectangular 16-QAM constellation diagram: (a) ideal; (b) actual

### 2.3.6 Linearization Techniques

Because of the stringent requirement on linearity and the desire to increase battery time, several linearization techniques have been developed to enable linear systems with more efficient, but nonlinear or less linear power amplifiers. As wireless communication evolve, it seems that a standalone linear power amplifier cannot meet linearity requirements posed by the next generation wireless systems. Therefore, some degree of linearization around the amplifier is necessary even if the amplifier itself is “linear”. Reference [2.15] has quite extensive coverage on this topic. Here some techniques will be discussed very briefly.

Feedback is probably the most obvious method to reduce distortion of power amplifiers. The improvement on linearity is dependent on the loop gain which could be quite expensive to obtain at RF frequencies. And stability is also a concern because time-delay is not negligible at RF frequencies. Cartesian loop [2.16] and polar loop [2.17] are two most popular feedback techniques.

To avoid problems with feedback at RF frequencies, feedforward<sup>15</sup> techniques have been proposed for linear power amplifiers. The input signal is split into two paths, and then combined after amplification, such that wanted signal are in-phase and distortions cancel out [2.15].

Predistortion is conceivably the simplest linearization technique, since it is open-loop in nature. Nonlinearities of power amplifiers can be corrected for at the input of the amplifier by predistortion [2.18]. The predistortion, in theory, will be cancelled out by distortions of power amplifiers. An overall linear transfer characteristic can thus be

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<sup>15</sup> Actually, the inventor, H.S. Black, filed patent of feedforward 9 years earlier than the patent of feedback.

obtained. This technique was mainly used for base-station because it was power hungry. With the scaling of CMOS, it becomes practical to implement this technique on portable devices.

## **2.4 Summary**

A brief overview of different classes of amplifiers was provided. Among many metrics that evaluate performance of power amplifiers, efficiency and linearity are particularly emphasized, because they represent fundamental trade off in power amplifier designs in modern multi-carrier systems. This is even more exacerbated if CMOS technologies are used as the design platform.

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## **Chapter 3: CMOS Technology for RF Power Amplifiers**

- 3.1 Prevalent technologies for RF power amplifiers
- 3.2 Comparisons among prevalent technologies
- 3.3 Trends of supply voltages for portable devices
- 3.4 Limits in CMOS technologies and the impact of scaling
- 3.5 Summary
- 3.6 References

### **3.1 Prevalent Technologies for RF Power Amplifiers**

Over the past several decades, various technologies (materials and devices) have been used to implement power amplifiers in the radio-frequency/millimeter-wave frequency range. The benefits of each technology vary, as do the drawbacks. Only a few of those technologies are currently in use. Features of those technologies will be briefly reviewed in this section.

#### **3.1.1 GaAs HBT Technology**

The concept of Heterojunction bipolar transistors is not a new one and was described by Schockley in a patent [3.1] filed in 1948, though the technology was not feasible until recent years because of the improvements in epitaxial crystal growth. The HBT is basically a npn bipolar transistor consisting primarily of three layers of doped semiconductor to form two junction diodes [3.2], i.e. for a large current gain, electrons are required to pass from the forward-biased emitter-base junction, through the p-type

base region, into the collector depletion region, with a minimum recombination with holes on the way. In the meantime, reverse hole injection from the base to the emitter should be minimized. The difference between the HBT and the standard bipolar junction transistor lies in the materials used to form junctions. Using a wide band-gap emitter in an npn HBT presents larger barrier experienced by holes than by electrons, which restricts the flow of minority carriers (holes) from the base into the emitter regardless of the doping levels on either side of the junctions.

Figure 3.1 illustrates a representative npn GaAs HBT cross-section. A typical GaAs technology provides npn transistors, thin film transistors, several metal layers (usually two) for interconnects with plated thick Au ( $\sim 10\text{-}\mu\text{m}$ ) as low-loss top level metal. MIM capacitors could be available or finger capacitors could be formed using interconnects. Inductors can be realized by patterning the metal layers. Due to the semi-insulating substrate used, as well as thick top metal layer, high Q passive elements could be realized on-chip. The 12.9 dielectric constant and semi-insulating substrate make it an excellent media for micro-strip and CPW (coplanar wave) design. A GaAs HBT technology also features through-wafer vias which provide low inductance ground connections from the top side of the die to the underlying ground plane. HBTs only require a single supply voltage for normal operation, and have very good high-frequency power performance.

For the last several years, AlGaAs/InGaP GaAs HBT power amplifiers have dominated the handset transmitter market due to their excellent power added efficiency and superior linearity when used in the CDMA systems. However, the substrate of GaAs wafers is not a good thermal conductor, and has to be thinned for optimum performance

in power amplification. Furthermore GaAs is more fragile than silicon. Therefore, the yield of GaAs ICs is relatively low which significantly adds to the process cycle time and wafer fabrication cost. Also, due to the wide band-gap, a large turn-on voltage ( $\sim 1.1\text{V}$ ) is required which is not favored by the trend towards low voltage.

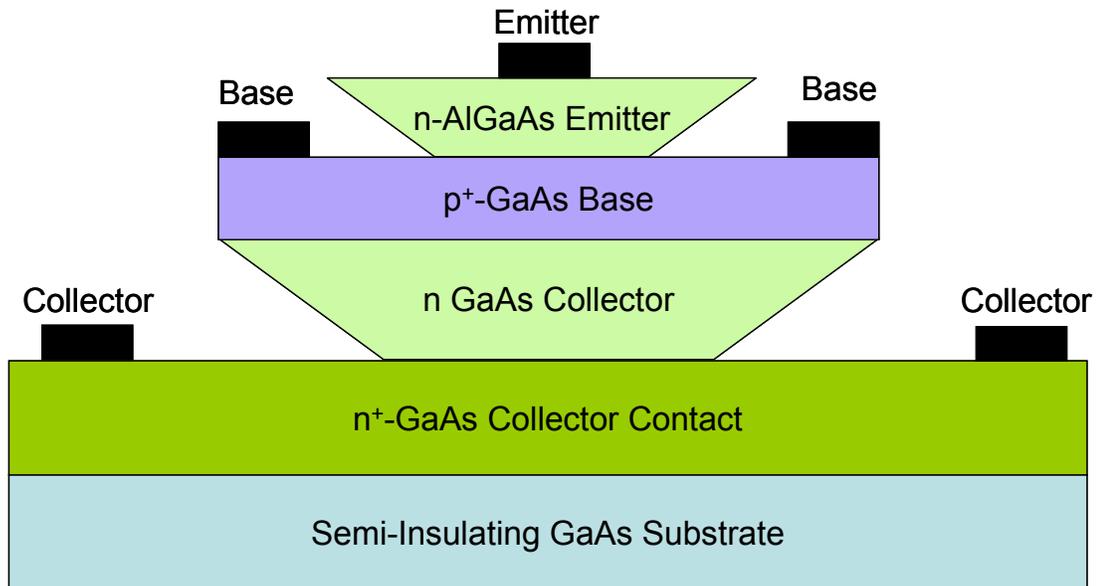


Figure 3.1: An npn GaAs HBT cross-section

### 3.1.2 GaAs MESFET Technology

GaAs MESFET was the original answer to “how can we make amplifiers at microwave frequencies?” It was the workhorse GaAs technology before technologists found out cost-effective ways to grow epitaxial layer reliably [3.3]. The operation of a MESFET is very similar to a JFET. The difference lies in the control electrode, where a reverse-biased pn junction is substituted by a Schottky barrier. Figure 3.2 shows the cross section of a GaAs MESFET device. This device consists of a barrier junction at the

input that acts as a control electrode (or gate), and two ohmic contacts through which output current flows. The output current varies when the cross section of the conducting path beneath the gate electrode is changed by changing the negative gate bias.

Very similar to GaAs HBT technology, GaAs MESFET technology usually features MESFET transistors, thin-film resistors, MIM caps and several metal interconnect layers. Through-wafer vias are also available in this technology. Comparing to GaAs HBT technology, MESFET technology is cheaper because no epitaxial layers are required. However, it requires negative bias for the depletion-mode transistors to work. These days it is being replaced by GaAs HBT.

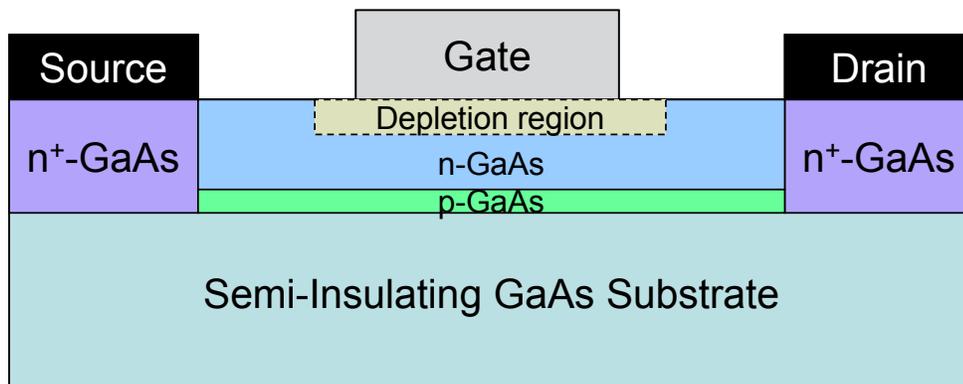


Figure 3.2: A GaAs MESFET cross-section

### 3.1.3 GaAs HEMT Technology

HEMT stands for high electron mobility transistor which was invented by Dr. Takashi Mimura [3.4]. A HEMT is actually a field effect transistor with a junction between two materials with different band gaps (i.e. a heterojunction) as the channel instead of an n-doped region. The effect of this junction is to create a very thin layer

where the Fermi level is above the conduction band, giving the channel very low resistance, or in other words “high electron mobility”. Figure 3.3 shows the cross section of a GaAs HEMT. As with MESFETs, a negative bias is required for depletion-mode transistors to work. As the HEMT technology developed, the details of the device layer structure also evolved [3.5]. In fact, the original GaAs/AlGaAs HEMT is now obsolete.

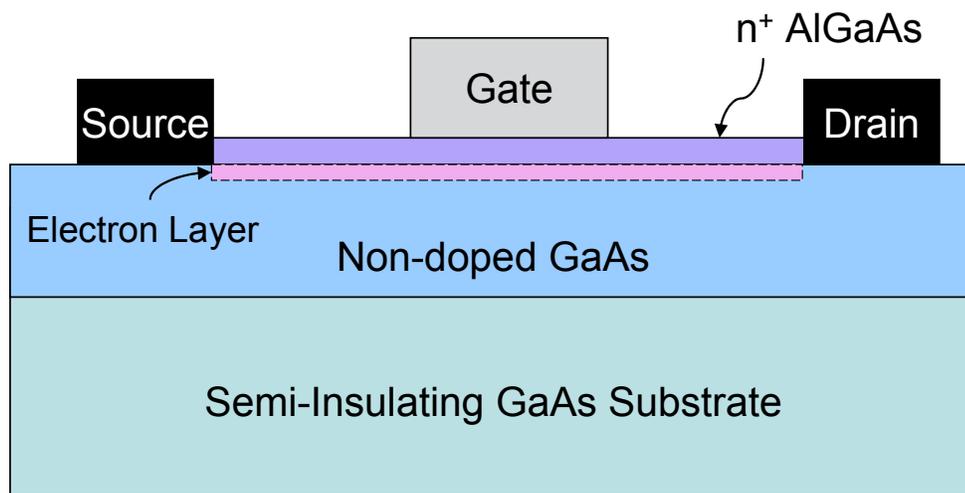


Figure 3.3: A GaAs/AlGaAs HEMT cross-section

Usually the two different materials used for a heterojunction should have the same spacing between atoms (lattice constant). Any mismatch will cause discontinuities at the interface which act as a kind of “trap”, which greatly reduce device performance. However, PHEMT (Figure 3.4), standing for pseudomorphic high electron mobility transistor, is a HEMT which violates this rule. It turned out that it is also possible to grow such heterostructure from materials with different natural lattice constants provided the thickness of the grown layer does not exceed a critical value. If the grown layer is thinner than the critical value  $t_c$ , its crystalline structure conforms to that of the substrate

materials. This causes a lattice deformation of the grown layer and a strained (or fancier, pseudomorphic) layer is created. The amount of strain depends on the lattice mismatch between substrate and the layer, and of course, on the layer thickness. The fabrication process of PHEMTs is very similar way to the process of MESFETs, except the starting material has epitaxial layers on it.

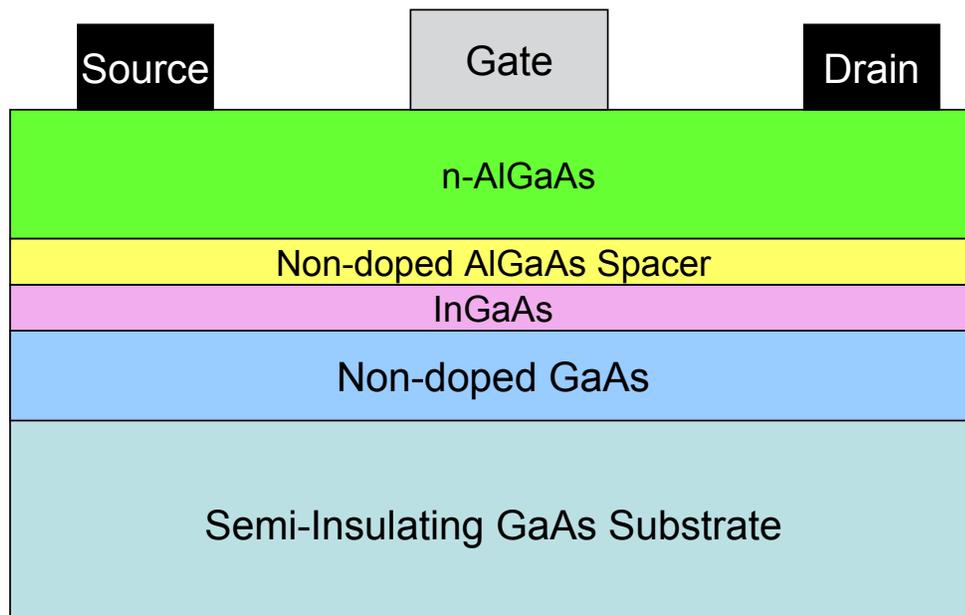


Figure 3.4: An InGaAs PHEMT cross-section

Yet there is another way to use materials of different lattice constants. Transistors based this heterostructure is so-called MHEMT (metamorphic HEMT, Figure 3.5). The basic concept [3.6] is to grow a graded buffer layer on a substrate, with a thickness much greater than the critical thickness  $t_c$  mentioned in PHEMT. The buffer layer serves as a relaxed pseudo-substrate for the actual device channel. Because the buffer is thick, dislocations arising at the substrate/buffer interface will be trapped and prevented from propagating into device channel. The buffer layer also transforms the lattice constant

from that of a GaAs substrate to that of the device layer. These approaches allow fabricating very fast transistors with “relatively” cheap GaAs substrate. Again, very similar to GaAs HBT technology, HEMT process usually includes HEMTs, metal interconnect layers, MIM capacitors, thin-film resistors, through-substrate vias. And they have the same disadvantage as GaAs MESFET, requiring both positive and negative supply.

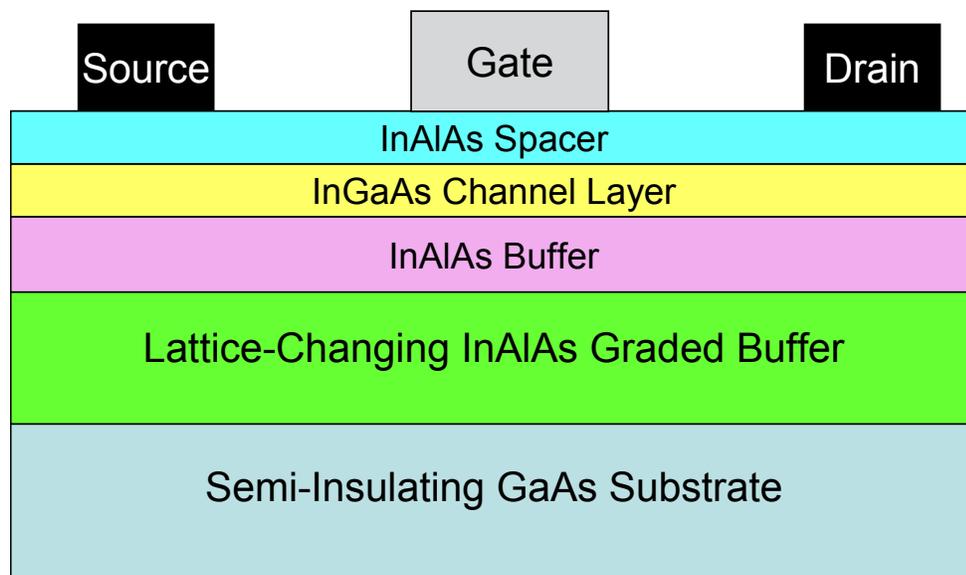


Figure 3.5 An InGaAs MHEMT cross-section

### 3.1.4 Si CMOS Technology

The concept of the MOSFET was actually developed well before the invention of the bipolar transistor [3.7]. In 1926 patents were issued to Lilienfeld for devices that resembled the modern silicon MOSFET, but which were made from combinations of materials not including silicon [3.8]. It took another 34 years before Kahng and Atalla

successfully built a working MOSFET. Since then, the growth of digital technologies such as the microprocessor has provided the motivation to advance silicon<sup>16</sup> MOSFET technology faster than any other semiconductor technology. The primary reason for the success of Si MOSFET technology is the development of CMOS logic, since Si MOSFET technology can provide both n-channel and p-channel MOSFET with comparable performance. However, the MOSFET's strengths as the workhorse transistor in most digital circuits did not translate into its supremacy in RF circuits until recently [3.9].

The MOSFET actually has four terminals: source, drain, gate and back gate. Figure 3.6 shows the cross section view of a typical CMOS process. Physically, the operation of the MOSFET can be understood in terms of water analogy [3.7]. The free carriers correspond to water droplets. The source and drain are deep reservoirs whose relative elevation difference is like a canal with a depth that depends on the local value of the gate-to-channel voltage. In a NMOS transistor, if the voltage on the gate increases, the majority carriers (holes) will be pushed away towards substrate, and be depleted as gate voltage continues to increase. Eventually, generations of carriers will exceed recombination. The generated hole-electron pairs are separated by the field, the holes being swept into the bulk and the electrons moving to the oxide-silicon interface where they are held because of the energy barrier between the conduction band in the silicon and that in the oxide. When a drain-to-source voltage is imposed, the current will flow in the channel. As the drain-to-source voltage increases, the current also increases. Beyond a certain drain-to-source voltage, the current will saturate.

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<sup>16</sup> Silicon is exclusively used for manufacturing MOS transistors because of silicon dioxide superior qualities as an insulator.

An unwanted byproduct of the bulk-Si CMOS structure is a pair of parasitic bipolar transistors, forming a parasitic pnpn path as shown in Figure 3.7(a), a basic p-substrate CMOS cross section. Vertical PNP transistors are formed by a p-substrate, an n-well, and a p-source or drain and lateral NPN transistors are formed by an n-source or n-drain, a p-substrate and an n-well. The collector of each BJT is connected to the base of the other bipolar transistor, forming a positive feedback structure. In order for latch-up to occur, the structure must be regenerative, in that it must provide a mechanism to increase the internal current to high values after it exceeds a certain threshold condition. In addition, external network must be capable of supplying current required by the regeneration. A two-transistor model, as shown in Figure 3.7(b), was proposed to explain how latch-up is triggered [3.11]. Usually the gain of parasitic transistor structures is typically more than sufficient to allow latch-up to occur. It is the presence of the shunting parasitic resistor ( $R_{\text{well}}$ ,  $R_{\text{sub}}$ ) between the base-emitter junctions that reduces the regeneration conditions in the parasitic devices with sufficient gain to otherwise exhibit latch-up. Substrate and n-well are heavily doped to reduce the resistance of  $R_{\text{well}}$  and  $R_{\text{sub}}$ . This effectively reduces the voltage drop across base-emitter junctions with the same current, which means more current is needed to trigger latch-up. Hence state-of-the-art bulk-Si CMOS processes use heavily doped silicon substrate to prevent latch-up and improve yield. However, this causes detrimental impact to lower passive components quality factor. This will be addressed in detail later.

State-of-the-art digital CMOS technologies usually feature NMOS and PMOS transistors with different threshold voltages, bipolar devices with reasonable quality, poly-silicon resistors, more than 6 levels interconnect metal layers with a relatively thick

top metal for global buses. Multiple metal layers can be used in sandwiched structures to form finger capacitors with high quality factors and modest capacitance density. Inductors are usually formed by patterning the top metal layers. MIM capacitors and ultra-thick top metal layer can be available if the CMOS process is tuned for mixed-signal or RF applications.

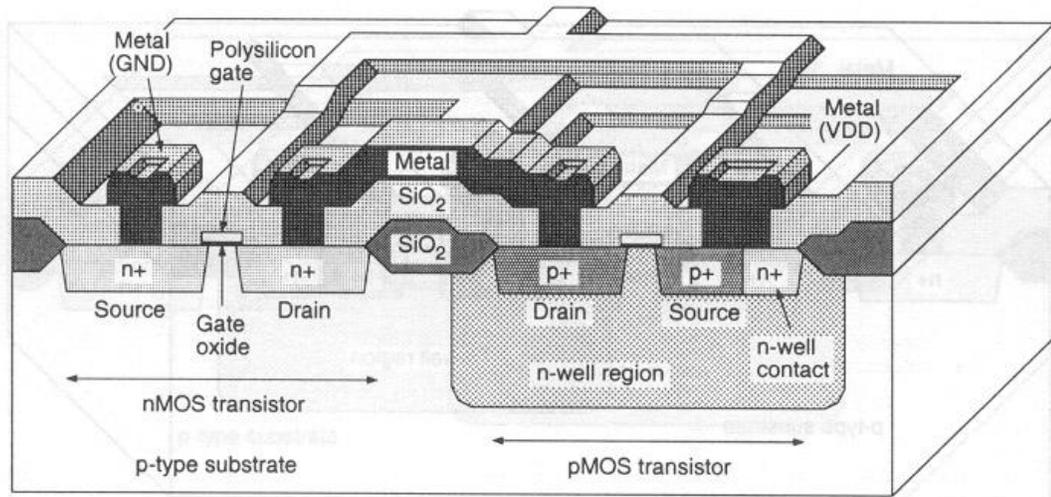
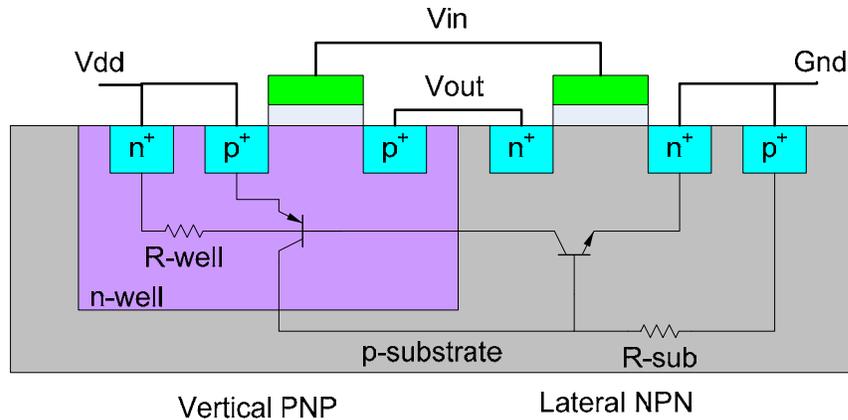


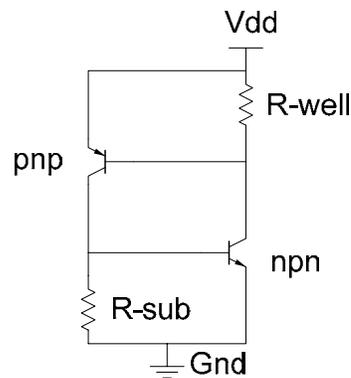
Figure 3.6: After “Atlas of IC Technologies” by W. Maly [3.10]

### 3.1.5 SiGe HBT Technology

The concept of combining Si and Ge into an alloy for use in transistor engineering is an old one, and was envisioned by Shockley in his early transistor game. However, because of difficulties in growing lattice-matched SiGe alloy on Si, this concept was reduced to practical reality only in the last 15 years. SiGe HBT technology was originally developed at IBM for the high-end computing market. That effort, however, lost to CMOS, primarily because of its high static power consumption.



(a)



(b)

Figure 3.7: (a) A representative schematic of parasitic bipolar transistors; (b) A circuit model to explain CMOS latch-up

Unlike its sibling GaAs HBT, SiGe HBT is manufactured on conventional silicon wafers and leverages conventional silicon processing toolsets. And because of this fact, this technology allows CMOS logic to be integrated with heterojunction bipolar transistors, and is so called BiCMOS, as shown in Figure 3.8. However, many of the improvements to CMOS technology do not directly transfer to BiCMOS technology. Fine tuning of both BJT and MOS components is impossible without adding many extra

fabrication steps, and consequently significantly increase the cost. Conflicting CMOS/HBT thermal budget requirements presents very difficult process integration issues. Therefore, CMOS devices available in the-state-of-the-art BiCMOS technologies are typically one generation behind those available in the-state-of-the-art CMOS technologies.

A SiGe BiCMOS process usually features SiGe HBT devices, CMOS transistors, and passives including capacitors and resistors. Because it is positioned for analog/mixed-signal circuit design, the top metal is usually thicker than the thickness of top metal in a generic CMOS process, around 4- $\mu\text{m}$  or so.

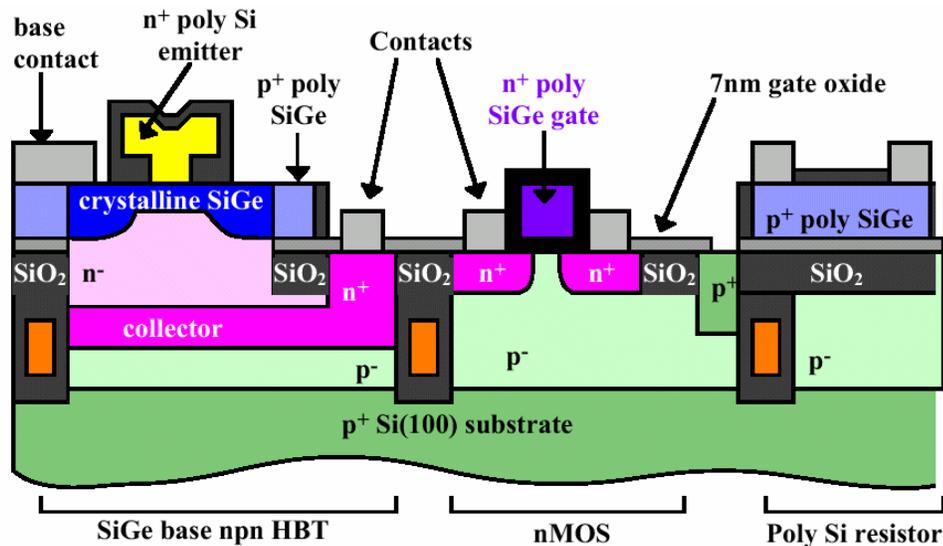


Figure 3.8: Diagram of SiGe HBT based BiCMOS by IBM

### 3.1.6 Si LDMOS Technology

LDMOS stands for lateral diffused MOS transistors. It was primarily developed for RF power application in 1972 [3.12]. The originality of the LDMOS structure is its

ability to achieve short channel (high frequency) and high voltage operation at the same time. Figure 3.9 shows a cross-section view of a LDMOS. It is typically manufactured on P<sup>+</sup> Si wafers with a lightly doped p-type epi layer. Gates are fabricated with WSi or CoSi on polysilicon. P<sup>+</sup> sinker is widely used in LDMOS. The obvious advantage is in decreasing number of contacts. The bulk-source connection eliminates the extra surface bond wires. The RF performance of such a connection is better, because the source inductance is reduced [3.12]. High frequency properties of a LDMOS transistor are usually determined by the length of the channel, with a trade off in breakdown voltage. And it is usually limited to operations below 5GHz. The processing is similar to CMOS with the addition of thick interconnect metallization. So it could be integrated with CMOS together at added cost.

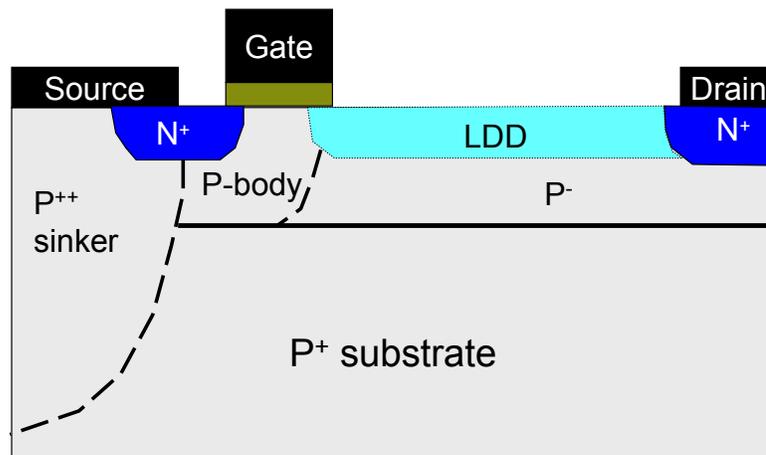


Figure 3.9: A LDMOS cross-section

### 3.2 Comparisons among Prevalent Technologies

After reviewing features of several prevalent technologies for RF power amplifiers, it is obvious that they are differentiated in terms of materials (GaAs or Silicon)

and devices (BJT or MOSFET). By the late 1990's, GaAs semiconductor had taken over more than half of the handset PA market, with silicon LDMOS and bipolar accounting for the rest. Figure 3.10 shows today's handset PA market share with GaAs market share increasing to about 80%. In the wireless LAN PA market, SiGe BJT and CMOS are the major players in 2.4 GHz applications, while GaAs dominates the 5.2 GHz arena. Before comparing different technologies, Table 3.1 summarizes the most important properties of Si and GaAs. In the following, comparisons will be made among four technologies, Si CMOS, Si LDMOS, SiGe BiCMOS, and GaAs HBT, from several perspectives. At the end, Table 3.2 will summarize this section.

Material	Si	GaAs
Band Gap (eV)	1.12	1.43
Breakdown field (V/cm)	$3 \cdot 10^5$	$4 \cdot 10^5$
Saturated Electron Drift Velocity (cm/sec)	$1 \cdot 10^7$	$1 \cdot 10^7$
Thermal Conductivity (W/cm-°C @ RT)	1.5	0.55

Table 3.1: Material properties of Si and GaAs

- AlGaAs/InGaP HBT GaAs
- LDMOS Si
- PHEMT/MESFET GaAs
- Other (SiGe BJT...)

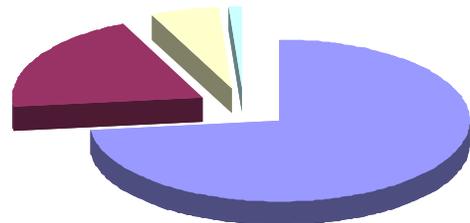


Figure 3.10: Handset PA market share as of 2004 (courtesy of Rob McMorrow)

### 3.2.1 Substrate

In GaAs HBT technologies, a semi-insulating substrate is used as the starting material. So devices fabricated on such a substrate will have good isolation. Moreover, semi-insulating substrates provide greatly reduced parasitic capacitances, thus faster devices. The down side is the thermal conductivity of the substrate used in GaAs processes. It is especially a problem in power applications.

Very low resistivity substrate is desirable in Si LDMOS technologies, on the order of 0.007  $\Omega$ -cm. This highly conductive substrate is favored because bulk-source can be tied together to reduce required bond wires and lower the source parasitic inductance for better performance. State-of-the-art Si CMOS and SiGe BiCMOS technologies usually adopt silicon substrate with resistivity on the order of 1  $\Omega$ -cm in non-epi processes. Much lower resistivity substrates ( $\sim$ 0.01  $\Omega$ -cm) are used in epi processes for digital circuits to avoid latch-up and improve yield.

Unfortunately this conductive substrate causes a headache in designing high quality factor passives. It is known that the skin depth  $\delta$  of a substance is the distance to which incident electromagnetic radiation penetrates [3.13]:

$$\delta = \sqrt{\frac{2}{\mu\sigma\omega}}$$

Where  $\mu$  is the permeability,  $\sigma$  is the electrical conductivity, and  $\omega$  is the frequency of interest. Assuming that the substrate resistivity in the selected Si CMOS technology is 0.01  $\Omega$ -cm, and the frequency of the application is at 1GHz. The corresponding skin depth is only 159  $\mu$ m. Because actual substrate thickness (after thinning) is thicker than this value, its effect on magnetic field and eddy current induced loss should be considered.

Meanwhile, displacement currents flowing into the conductive substrate further increase loss. From this perspective, GaAs technologies are definitely favored.

### 3.2.2 Backside Vias

As mentioned previously, GaAs technologies usually feature backside vias that connect the front side metallization layers of the die to the back side ground plane. It is a critical element for MMIC technology. Electrically it provides a low resistance and low inductance ( $\sim 20$ -pH) path to the common ground plane. At the same time, it also serves as a heat dissipation path because GaAs is not a good thermal conductor. Usually in a GaAs technology process, wafer substrate will be thinned to  $30\sim 50$   $\mu\text{m}$  before backside via etching steps. Thinning the substrate makes backside via etching practical and affordable.

In Si processes, typical substrate thickness varies from  $300\sim 800$ - $\mu\text{m}$ . Therefore it is not realistic to etch through the wafer substrate with good yield. Thus, ground connections are realized using bondwires from pad on-chip to the package. In general, these bondwires have relatively large inductance<sup>17</sup> ( $\sim 1$ nH) which is certainly not desirable in RF applications. To minimize parasitic inductance, two approaches could be used. One is to increase the diameter of the wire to reduce self-inductance. The other one is to use several bondwires in parallel to reduce the parasitic inductance. The ultimate limit of the latter approach is the mutual inductance among wires.

Lower parasitic inductance is very desirable in RF design. Better stability, higher gain, and other performance improvements could be obtained with lower parasitic

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<sup>17</sup> The actual inductance depends on the loop.

inductance. The availability of backside vias in GaAs technologies was clearly a winner in the old days when single-ended power amplifiers prevailed. In Si technologies, flip chip packaging can be employed to achieve low parasitic inductance ( $\sim 100$ -pH), but with much higher cost.

### **3.2.3 Passives**

In analog/RF design, all the glory goes to the sophisticated high gain amplifiers, however, they are useless without passives to control/tune them. In a typical off-the-shelf cell phone, a passive to active component ratio of 20:1 is usual. A good portion of those passives are surface mount passives. To reduce the form factors of handheld devices, the growing trend is to have as many integrated on-chip as possible.

#### **3.2.2.1 Resistors**

Resistors are often used in power amplifiers, and all other analog and mixed-signal circuit blocks. For bipolar power amplifiers, emitter ballasting resistors are used to equalize current flow in unit devices. It is also often used to stabilize the circuit, and/or to bias up circuits. In GaAs technologies, precision thin film resistors with low tolerance, low parasitics and the ability to make the design changes with short cycle time are available. Resistors made of active layers are also available to designers. In Si technologies, doped/undoped poly resistors, diffusion resistors are usually available for designing circuits. However, precision BEOL (Back-end of the Line) thin film resistors are not at designers' hand in general.

### 3.2.2.2 Capacitors

To designers, three characteristics are of particular interests, capacitance density, parasitic capacitance to the substrate, and the quality factor. MIM capacitors and finger capacitors are available in both GaAs technologies and Si technologies. Because high-k dielectrics are used in MIM capacitors and many levels of metallization layers are available for finger capacitors in Si technologies, the capacitance density is usually much higher than it is in GaAs technologies. In Si technologies, designers are bothered with parasitic capacitance to the substrate because it is conductive. However if the capacitor is used as a part of a tuned tank, the stray capacitance could be absorbed into the tank. Nonetheless, the extra loss by displacement current in the conductive substrate degrades the quality factor of capacitors in Si technologies.

Figure 3.11 shows the schematic of a cross-section of a MIM cap [3.14] and the schematic of a cross-section of a finger cap [3.15]. In Si technologies, the capacitance density of MIM cap can reach  $3\sim 5\text{-fF}/\mu\text{m}^2$ , with Q above 100 at 2-GHz range. For finger caps, the capacitance density can reach  $1\sim 2\text{-fF}/\mu\text{m}^2$ , with superior Q above 100 at 10-GHz range. Capacitors in GaAs technologies have similar quality factor but less density comparing to Si technologies.

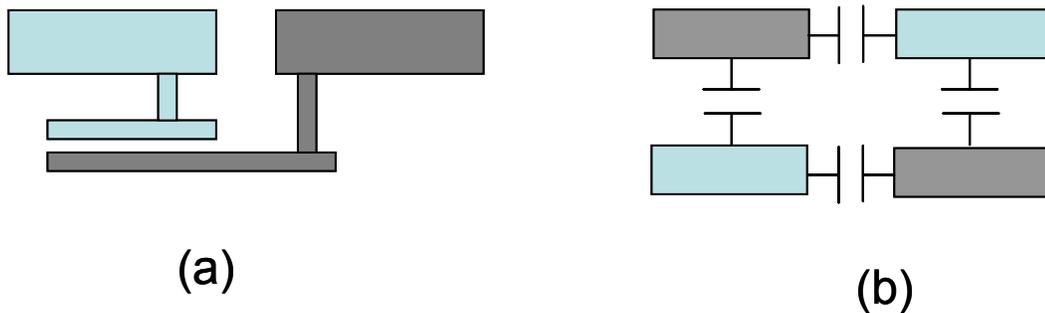


Figure 3.11: The cross section of (a) A MIM capacitor; (b) A finger capacitor

#### 3.2.2.4 Inductors

On-chip inductors can be formed by patterning the metal layers in a process. Usually, to obtain the best available quality factor, top metal layers are preferred for realizing inductors. Because on-chip capacitors have enough Q for most applications, high Q inductors have become the “holy grail” in integrated circuits design. In PAs, the efficiency of a PA is tightly related with the quality factor of inductors used in the design.

Several mechanisms contribute to the loss of on-chip inductors. First and foremost is the metallization thickness. At low frequencies, the series resistance can be calculated from the conductor sheet resistance. At microwave frequencies, the skin effect becomes dominant, further increasing series resistance. The loss due to the finite conductivity of the conductors is probably the only source of loss in a GaAs technology. And it contributes significant amount of the loss in a Si technology. In a typical GaAs technology, thick top metal (8~10  $\mu\text{m}$ ) in gold is available. In contrast, top metal around 2  $\mu\text{m}$  thick in copper or aluminum is typical in a standard state-of-the-art Si technology. Assuming the resistivity of copper is 17  $\text{n}\Omega\cdot\text{m}$ , and the frequency of the interest is 1GHz, the corresponding skin depth is 2  $\mu\text{m}$ . Therefore, thicker metal will definitely help to improve the quality factor at GHz range.

For Si technologies, additional significant degradation of inductor quality factor results from energy coupled in the conductive substrates. The first kind of coupling is through electrical coupling. Since an on-chip inductor is essentially one plate of a capacitor, displacement current will flow into the substrate and cause energy loss. To prevent this current flowing into the substrate, a lower layer of the metallization stacks could be patterned to act as pseudo-substrate as far as electrical field is concerned [3.16].

This improvement is obtained at the cost of lower self-resonance frequency of the inductor and enhanced frequency dependence of inductance. The second component of the coupling is magnetic coupling. The magnetic field generated by an inductor will induce an image current to flow in the lossy substrate. In the-state-of-the-art Si technologies, the skin depth of the substrate is thinner than the substrate thickness, therefore the effect of eddy current cannot be overlooked. Even if the substrate thickness is slightly thinner than the skin depth, the loss would be nearly the same. Some measures have been proposed to prevent image current in the substrate [3.17], although the effectiveness of those measures is in debate.

Due to loss mechanisms mentioned above, the quality factor of an optimized inductor in Si technologies is around 10 at 2-GHz range. Meanwhile, the quality factor above 30 could be realized in GaAs technologies. Since high Q passives are crucial to achieve efficient PAs, GaAs technologies outperform Si technologies without any doubt from this aspect.

### **3.2.3 Device characteristics**

Even though the physics of MOSFET and BJT are fundamentally different, they can be designed in circuits with similar topology/architecture to achieve certain functionality. Two parameters are often cited when comparing devices for RF applications, namely  $f_T$  and  $f_{max}$  [3.18]. The  $f_T$  is defined as the frequency where the magnitude of the short-circuit common-source/common-emitter current gain falls to unity. The  $f_T$  is bias dependent. For MOSFET (small signal model shown in Figure 3.12), it can be expressed as:

$$f_T = \frac{1}{2\pi} \frac{g_m}{C_{GS} + C_{GD}}$$

The  $f_{\max}$  is defined as the maximum frequency of oscillation or the frequency where the magnitude of power gain falls to unity, under matched condition. For MOSFET,  $f_{\max}$  can be expressed as:

$$f_{\max} = \frac{f_T}{2} \sqrt{\frac{1}{g_{DS}(R_G + R_S) + 2\pi f_T R_G C_{GD}}}$$

Besides biasing conditions, the  $f_{\max}$  is highly layout dependent. In high frequency applications, the  $f_{\max}$  is the most relevant figure-of-merit. GaAs technologies hold the record of the fastest device. Recently, a GaAs HBT transistor with a maximum operating speed of 604 GHz was developed by two researchers from UIUC [3.19]. The most Advanced SiGe HBT in production today has more than 200 GHz  $f_T/f_{\max}$  [3.20]. Si CMOS was not able to perform faithfully in the RF frequency range 15 years ago. As digital circuits keep driving MOSFET scaling, today CMOS can be useful, even up to 60GHz [3.21, 3.22]. Reported  $f_T$  and  $f_{\max}$  of 90-nm CMOS are more than 200GHz [3.23], comparable to SiGe HBT. In this arena, Si LDMOS is definitely not competitive at all because of the tradeoff between breakdown voltage and frequency response. Therefore, it is rare to find applications over 5GHz using Si LDMOS technologies.

Other than frequency response performance, the other absolutely important figure of merit of devices for power amplifiers is breakdown voltage, which directly influences the available voltage swing of the device. The breakdown is caused by various physical mechanisms at high electric fields that lead to device failure. When and how breakdown is going to kick off depend on the device structures as well as the semiconductor materials.

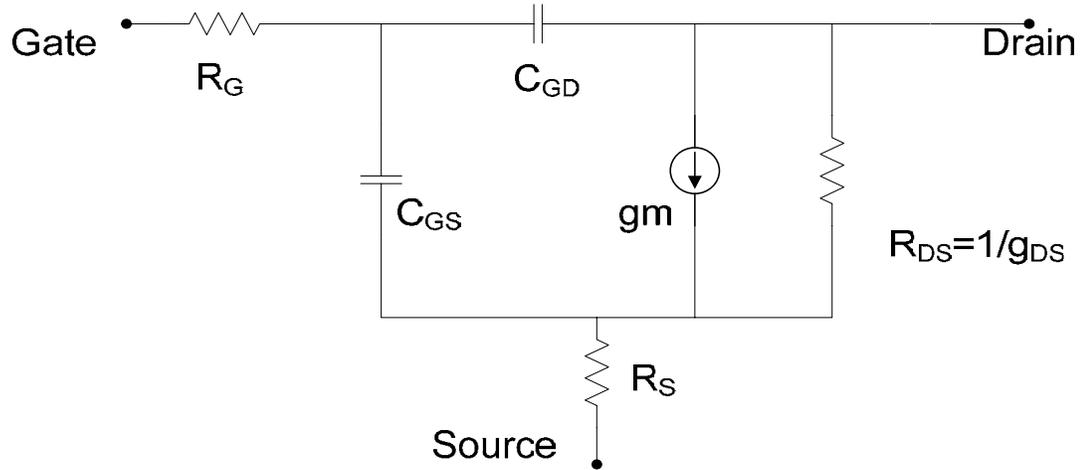


Figure 3.12: A simplified small-signal model for MOSFET

The bipolar device is fundamentally limited by avalanche breakdown in the collector-base junction [3.24]. The device can be characterized by the collector-emitter breakdown voltage when base is shorted to the emitter (BVCBO) or when the base is open-circuited (BVCEO). In 1965, Johnson published a paper which states the tradeoff between  $f_T$ <sup>18</sup> and breakdown voltage, known as Johnson limit [3.25]. Figure 3.13 plots the BVCBO for modern bipolar devices manufactured with different semiconductor materials.

There are various breakdown mechanisms that limit the operation of a MOSFET, including time-dependent dielectric breakdown (TDDB) due to channel hot carrier effects, gate oxide breakdown, snapback breakdown and junction breakdown [3.26]. From a reliability perspective (in digital circuits context), TDDB presents the most significant limitation on dynamic range in scaled MOSFETs. This effect is a result of damages to the silicon-oxide interface due to injection of hot carriers at the drain. This shifts the

<sup>18</sup> It seems that  $f_{max}$  is more appropriate here, however, it is highly layout dependent.

threshold voltage of the device and causes oxide quality degradation over an extended period of time. The recommended voltage limitations are typically based on dc or transient reliability tests on minimum channel length devices, whereas few results are available studying device performance degradation under RF operations, or studying reliability of devices with slightly relaxed channel length<sup>19</sup>. Although it is believed that further investigations, to assess reliability and lifetime of devices under RF operations, can relax the conservative upper limits on the supply voltage for MOSFETs, current designs in production have to obey the stringent reliability constraints on supply voltage.

A comparison of the BVCBO of bipolar transistors and the recommended operating voltage for MOSFETs as a function of  $f_T$  is shown in Fig 3.13. Benefited from wide band gap as well as high carrier mobility, GaAs HBT is clearly the star in this arena. And Si CMOS technologies obviously lag behind other technologies. It should be noted that LDMOS does exhibit excellent performance in terms of breakdown voltage, since the device is specifically tailored for power applications.

### **3.2.4 Manufacturing Cost**

High-volume proliferation of semiconductor products largely relies on costs being significantly reduced. Reducing manufacturing cost involves increasing chip yield, reducing cycle time, maintaining consistent product quality, improving equipment reliability, and maintaining stringent process control.

GaAs wafers are very brittle and fragile; often require modification to equipment to prevent wafer breakage. And because of that, GaAs wafers have only recently become

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<sup>19</sup> From communications with engineers in foundries, supply voltage can be boosted with non-minimum channel length transistors. However, such information cannot be obtained from a design kit.

available in 6 in. diameters as compared to the 8-12 in. diameters in Si. Yet the shift to 6 in. wafers is partly to utilize Si production equipment for reduced cost, and partly to supply the required volumes. The relative high cost of substrate materials, the slow pace to large diameter manufacturing have made GaAs an expensive choice.

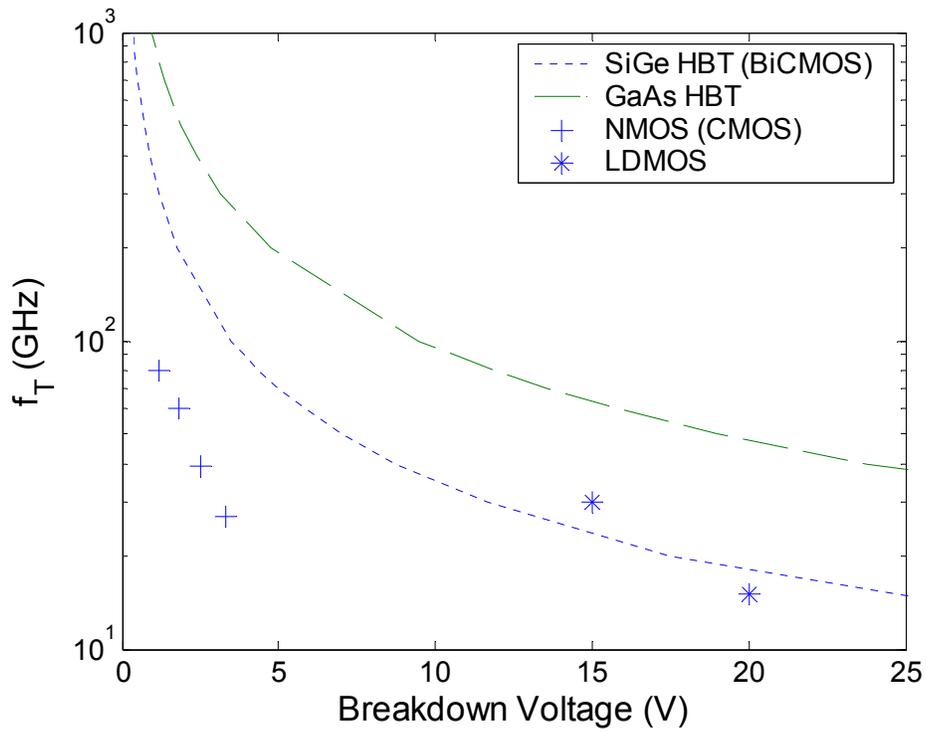


Figure 3.13: Comparison of breakdown voltages of different technologies. SiGe HBT and GaAs HBT are calculated from Johnson limit. NMOS breakdown voltages are taken from recommended supply voltage published on ITRS website. LDMOS breakdown voltages are taken from foundry online data provided by Jazz Semiconductors.

### **3.2.5 Integration**

Explosive growth in portable communication market has led to consumer demand for low-cost, small form factor, low power terminals. It has been proved in practice that high level of integration is the most effective way to provide such a solution. The VLSI capabilities of CMOS make itself a well-suited vehicle for high integration, since more and more functionalities are realized in digital domain. In GaAs technologies, hole mobility is far behind electron mobility, therefore p-type devices are too slow compared to n-type device. Besides, good quality insulator that is very crucial for MOSFET is not available in GaAs technologies. Thus Si is an ideal substrate for manufacturing MOS transistors for digital circuits, while it is extremely difficult to manufacture MOS Transistors on GaAs substrate. Therefore, Si technology has the potential to deliver a complete, low cost system

### **3.2.6 Availability & Capacity**

Traditionally, GaAs has been avoided by high-volume semiconductor device manufacturers in preference to the established silicon CMOS, Bipolar and BiCMOS designs and processing. Unlike its silicon equivalent, a “pure-play” GaAs foundry does not exist or at least is very hard to find. It was estimated in 2005 that the overall GaAs foundry industry is \$100 million business [3.27], only 0.3% of DRAM market. And because it is a small market that is only able to support only a few foundries, GaAs foundries availability and capacity are very limited. In silicon technology, LDMOS technologies are also not easy to get access compared to as other silicon technologies. In

fact, its availability is less than the availability of GaAs technologies for reasons that are unknown to the author.

Parameter	Excellent	Moderate	Challenging
Passive Quality	GaAs	--	CMOS, SiGe, LDMOS
$f_T$	GaAs, SiGe	CMOS	LDMOS
$V_{\text{breakdown}}$	GaAs, LDMOS	SiGe	CMOS
Cost	CMOS	LDMOS	GaAs, SiGe
Integration	CMOS	SiGe, LDMOS	GaAs
Availability & Capacity	CMOS	SiGe, GaAs	LDMOS

Table 3.2: Summary of comparisons among prevalent technologies for RF PAs

### 3.3 Trends of Supply Voltages for Portable Devices

For commercial handheld devices, reduced power consumption translates into longer battery lifetime and/or smaller lighter products through the reduction of battery size. These characteristics are very important to consumers, and thus key to product development. After reviewing relevant technologies, it is interesting to take a look at the trend towards low power and low voltage circuits/systems. Before we get into that, one thing should be bear in mind is that the semiconductor industry is driven by digital circuits to the first order.

Wireless electronics requires a power source which is generally rechargeable. The electro chemical properties of the batteries chemistry produce a specific voltage

potential which is commonly referred to as a cell. Table 3.3 provides a list of the some of the main battery technologies for use in portable electronics and their associated characteristics [3.28]. If the standard single cell voltage of a technology is higher than the desired operating level, then DC-to-DC conversion will be needed for a lower output voltage.

Fifteen years ago, power amplifiers in mobile handsets were primarily built using discrete transistors, operating from either 4.8-V or 6V power sources. Around 1996, a leading handset provider dropped their battery system down to 3V to reduce the size of handsets [3.29]. Due to the obvious trend towards low supply voltage, there is an interesting debate in the industry whether to completely rely on DC-to-DC converter or develop low cell voltage batteries. From Table 3.3, low cell voltage Li-Polymer battery is an attractive candidate, which has better energy density with comparable cost. Among various projections, Figure 3.14 shows the projection of battery voltage from a report released in 2004 by iNEMI<sup>20</sup>. Although the projection did not happen as scheduled, it does show the trend towards low battery voltage. One of the reasons that caused delay, according to the author's opinion, is the resistance from PA manufacturers. The developments of circuits to consume low power at lower supply voltages are consistent with the general trends of CMOS scaling. For digital circuits, active power consumption of a chip has quadratic relationship with the supply voltage:

$$P_{active} \propto CV^2 f$$

Smaller devices require less voltage to achieve the same electric field levels, thus reduced size also leads to reduced voltage requirements. Supply voltage of CMOS is scaled down

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<sup>20</sup> International Electronics Manufacturing Initiative, an industry-led consortium of approximately 70 electronics manufacturers, suppliers and related organizations, including Intel, IBM, TI.

by 15% every generation as shown in Figure 3.15. The aggressive scaling of supply voltage is employed to minimize power dissipation as well as to assure chip reliability during life time.

Characteristics	Ni-M-H	Li-Ion	Li-Metal	Li-Polymer
Unit Cell Voltage	1.25	3.6	3	2.2
Gravimetric Efficiency, Wh/kg	55	100	140	400
Volumetric Efficiency, Wh/l	170	225	300	500
Cost, \$/Wh	1.5	3	2	3
Self-Discharge Rate, %/month	25	8	1	8
Charge time, hr	0.5	3	3	3
Footprint	fixed	fixed	fixed	flexible <sup>21</sup>
Cycle Life	500	500	?	1000
Environmental Concerns	no	no	no	no
Memory Effect	no	no	no	no
Safety	good	good	?	good

Table 3.3: Properties of battery technologies for portable devices

<sup>21</sup> The flexible footprint is especially attractive to portable electronics manufacturers, to produce more compact, good looking products

For a power amplifier, the considerations are quite different from baseband digital circuits and/or RF transceiver circuits. Usually, the output power by a power amplifier is determined by applications. For instance, a power amplifier with 3V supply need transmit 27dBm for the CDMA IS-95 standard. Another power amplifier with 1V supply also needs to transmit 27dBm in order to meet standard requirements. Scaling down supply voltage does not save any power since it is predetermined. Instead, power amplifiers generally suffer from a performance hit with a lower power supply and PA designers have been very reluctant to lower the supply voltage<sup>22</sup>. This has resulted in a constantly growing disparity between the power supplies used for the PA and that of the rest of the components of a cell phone (Figure 3.16).

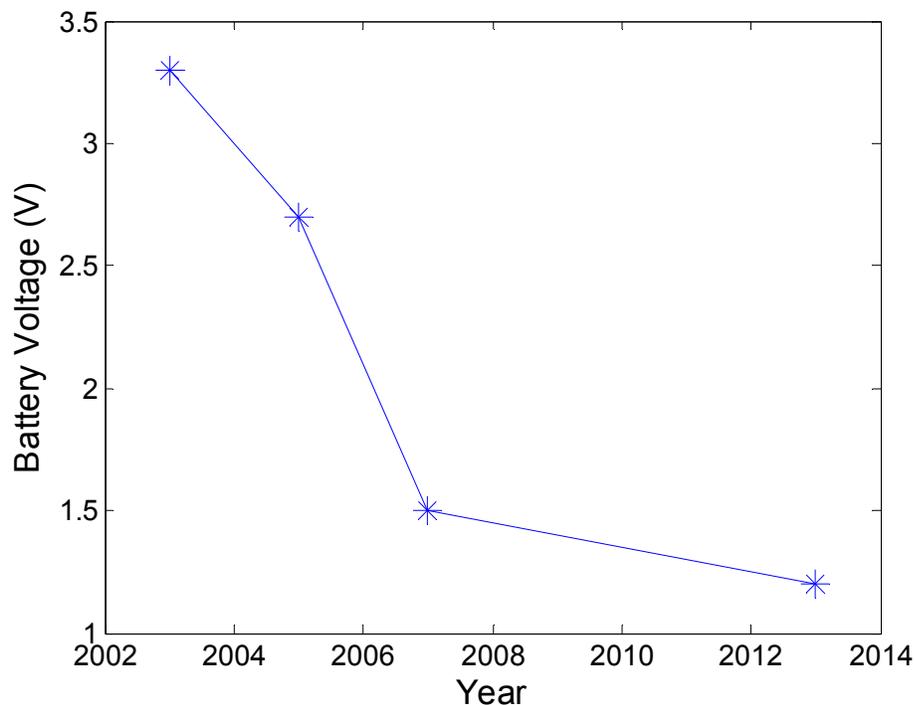


Figure 3.14: Battery voltage projection published by iNEMI

<sup>22</sup> This is due to high band gap, a two-sided sword, in compound semiconductors.

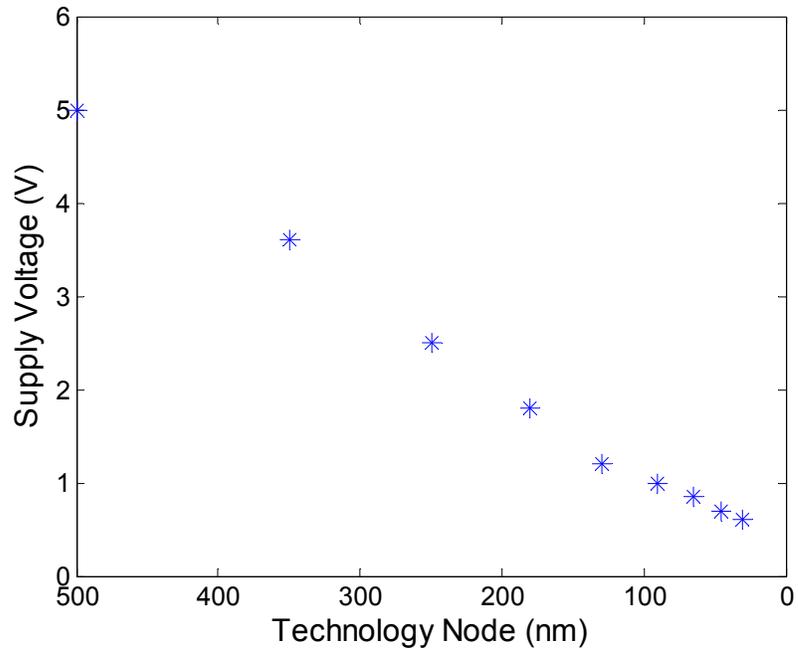


Figure 3.15: Recommended supply voltage as CMOS scaling continues (data collected from ITRS website)

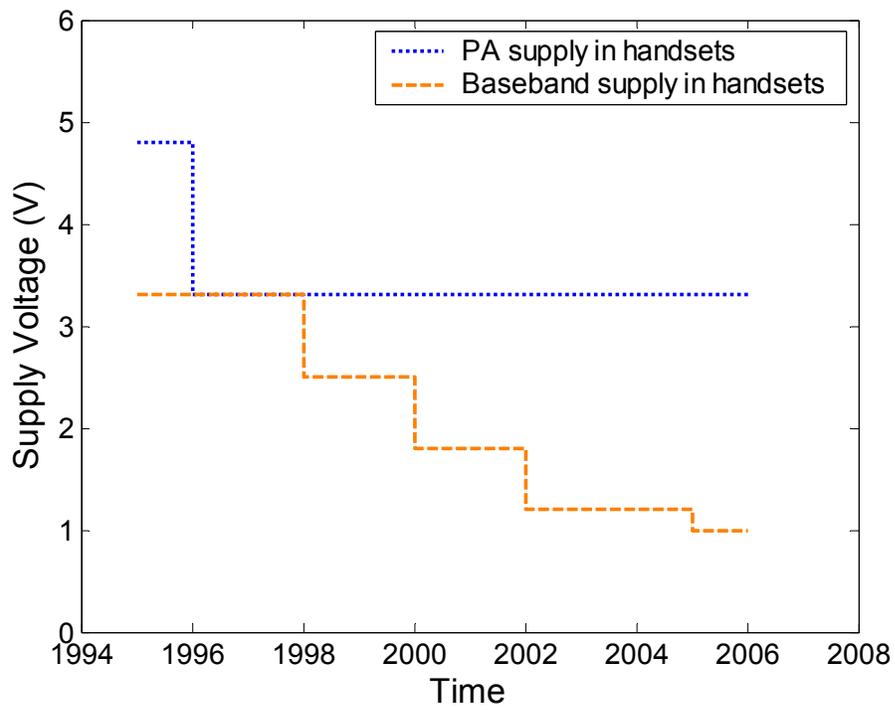


Figure 3.16: The disparity between supply voltages for PAs and that for digital circuits

### **3.4. Limits of CMOS and the Impact of Scaling**

Two major hurdles associated with the design of fully integrated power amplifiers are low transistor breakdown voltage/high threshold voltage, and high loss impedance transformation network consisting of lossy on-chip passives. The limitations are from semiconductor materials as well as device structures. In this section, challenges and opportunities presented by the continued scaling will be studied with data from ITRS [3.30].

#### **3.4.1 Device Scaling**

For devices available in today's technologies, GaAs or Silicon, MOSFET or HBT, they all have enough capabilities to be designed to operate at a few tens of GHz range. With respect to MOSFET devices for power amplifiers, frequency response is probably the only thing that will benefit from scaling. Other metrics such as linearity will inevitably degrade as scaling continues [3.31]. Fortunately technology scaling significantly lowers the cost of digital logic and memory, leveraging digital baseband processing power to improve the PA linearity demonstrates great potential. For example, predistortion techniques have been adopted in base station to improve the linearity of the PA [3.32]. As scaling continues, it will take less power and area to implement predistortion technique, making it suitable for portable devices as well.

As shown in chapter 2, the importance of large voltage swing at the output needs no introduction. A serious issue that designers have to face is the ever-decreasing voltage headroom which severely limits the power handling capability and the efficiency of power amplifiers. Although state-of-the-art CMOS technologies offer several thin-oxide

devices, with different threshold voltages and RF design usually pick low threshold voltage devices to maximize swing, the scaling of threshold voltage cannot track the scaling of the supply voltage because of the requirements to control the leakage power. This trend will continue in the future as predicted by ITRS (Figure 3.17). Today's state-of-the-art CMOS technologies offer I/O transistors with relaxed channel length and gate dielectric thickness. Strategic adoption of these I/O transistors might overcome some of the voltage limitations. However, there are several issues here. First, the device modeling of the I/O transistors may not be well characterized as the core transistors. And the process control is tuned for the core transistors instead of I/O transistors. Moreover, I/O transistors also scale with core transistors. The supply voltage for I/O devices will follow the scaling of supply voltage of core devices, maybe with different factor (Figure 3.17).

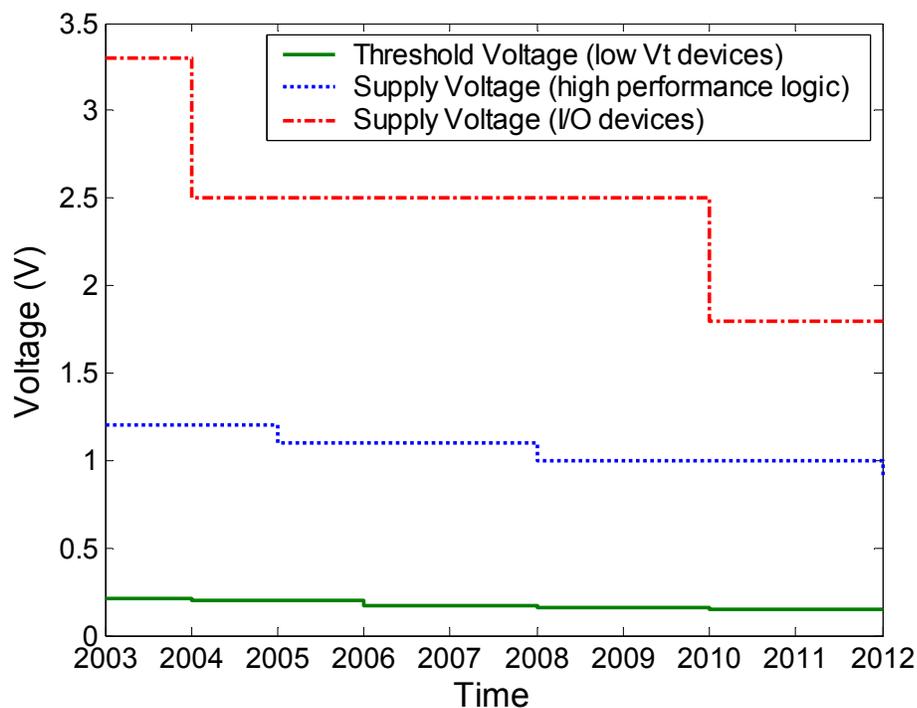


Figure 3.17: Scaling of supply voltages and threshold voltage for analog/RF circuits

### 3.4.2 Starting Materials

Historically, CMOS devices are fabricated using starting materials involved the choice of either polished Czochralski (CZ, non-epi) or epitaxial silicon wafers. Recently, silicon-on-insulator (SOI) wafers have become more than a niche technology, although the total number of SOI wafers shipped is still small compared to non-epi and epi wafers. The opportunity for SOI wafers to be used in mainstream high-volume application is being driven by improved high frequency logic performance and reduced power consumption, as well as enhanced device performance via unique device configurations such as multiple-gate transistor structure. In some cases, process flow simplification is also achieved. Meanwhile, the implementation of shallow trench isolation (STI) and the development of alternate doping means for achieving latch-up suppression make a heavily doped substrate as starting material unnecessary<sup>23</sup>. The possibility of eliminating conductive substrate would greatly reduce losses induced by lossy substrate, hence improving the quality factor of on-chip passives.

### 3.4.3 Metal Stack Scaling

In CMOS scaling, critical dimensions of active devices are scaling down. However, metal stack is scaled inversely. For example, number of metal layers increase with technology scaling (Figure 3.18). Meanwhile, low-k inter-metal dielectrics and copper are replacing conventional silicon-dioxide and aluminum in the metal stack. This metallization scheme is to minimize RC delay and voltage drop across the chip for those global interconnects and power grids in digital circuits. Nonetheless, the impact of

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<sup>23</sup> From cost perspective, an epitaxial wafer is more expensive than a non-epi wafer.

interconnect scaling on passive device quality is unclear at this point. For example, in a typical 0.35- $\mu\text{m}$  process, there are four metal layers, with the top layer about 1- $\mu\text{m}$  thick, and about 6- $\mu\text{m}$  above the substrate. State-of-the-art 90-nm technology typically offers 7 metal layers, but only with the top layer about 0.9- $\mu\text{m}$  thick, and about 5~6- $\mu\text{m}$  above the substrate. Therefore, it is likely that the quality of passives may degrade<sup>24</sup>.

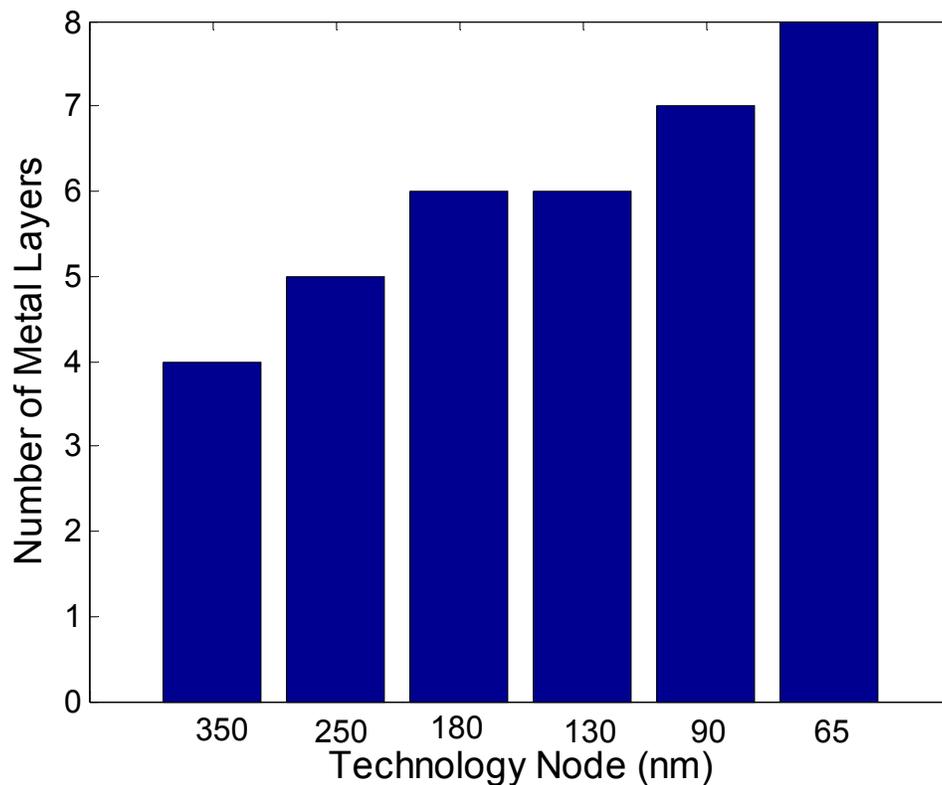


Figure 3.18: Number of Metallization layers vs. technology node

### 3.5 Summary

Because wireless device suppliers consistently face savvy consumers' demands for higher performance, lower costs and faster design turnaround, they are compelled to

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<sup>24</sup> RF CMOS processes provide thick top metal (2~4- $\mu\text{m}$ ), but with added cost.

rely more and more on their component suppliers to provide a system solution. As a result, part of this onus is passed on to component suppliers to help meet end-user needs including smaller size, enhanced performance, longer battery life, and lower prices. One way to meet these demands is by modifying manufacturing processes or changing manufacturing technologies used to fabricate RF power amplifiers. CMOS has proven itself a suitable vehicle to meet such stringent requirements. From performance and power dissipation perspective, data transfer on-chip can be significantly faster than off chip and requires less power. From cost perspective, it might be true that fully integrated system is not the cheapest solution at present time. However, it offers great potential for cost saving in the future.

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## **Chapter 4: Generating High Power with Low Voltage Devices**

- 4.1 Series power combining
- 4.2 Parallel power combining
- 4.3 Proposed power combiner
- 4.4 Summary
- 4.5 References

When a larger output is needed than can be obtained from a single device or pair of devices, multiple devices can be arranged in different ways to achieve the needed output power. This is precisely the situation that designers have to face when using CMOS technologies for RF PAs. In this chapter, two kinds of approaches will be discussed. The first approach, series combining through stacking devices, generates high output power by connecting devices together in a way so that they can operate reliably with a supply voltage much higher than recommended voltage. The second approach, parallel combining, combines power from several small amplifiers to generate high output power. The two approaches can be used alone, or in conjunction to generate even higher power.

### **4.1 Series Power Combining**

#### **4.1.1 Cascode Configuration**

The cascode configuration was first invented for vacuum-tube circuits. It is important mostly because it increases output resistance and greatly reduces unwanted

capacitive feedback. Therefore, the cascode configuration is generally used in operational amplifiers and other low-frequency designs. In MOS form, the cascode is a common-source – common-gate amplifier as shown in Figure 4.1. Only the gate of the common-source transistor is driven by input signals. The gate of the common-gate transistor is AC grounded.

In the case of RF power amplifiers, the cascode offers an important additional benefit. An advantage that the cascode configuration has over single transistor topology is it can sustain higher voltage before breakdown happens. In a state-of-the-art CMOS process, junction breakdown voltage is significantly higher than recommended supply voltage which is primarily determined by drain-to-source breakdown voltage. Therefore, in principle, the voltage stress could be shared between common-gate and common-source transistors.

However, the voltage stress is not usually evenly split between two transistors. Typically, the common-gate transistor is stressed more than the common-source transistor, depending on the biasing level at the common-gate. Hence it may become the bottle neck in terms of breakdown. Previous work used a combination of standard thin-gate-oxide transistors for common-source devices and I/O devices for common-gate devices to alleviate this problem [4.1]. Unfortunately, a thick-gate-oxide device does not have comparable high-frequency performance of a standard device. Therefore, the thick-gate-oxide device degrades the RF gain, and limits other high-frequency performance. Other work proposed an alternative solution [4.2]. Instead of AC grounding the gate of the common-gate device, the AC voltage at the gate is set to swing with the same polarity

as the AC voltage at the output. This will help to evenly distribute voltage stress between two transistors, at the expense of degraded RF gain.

Several disadvantages come with the cascode configuration for power amplifiers design. In both transconductance power amplifiers and switching power amplifiers, the common-gate device acts more or less like a switch. Since the switch is not ideal by all means and has finite on-resistance, power will be dissipated as current flows through the cascode device. This extra power dissipation inevitably degrades the power efficiency of the amplifier. Nonetheless, this drawback can be overcome through careful design. By sizing the cascode device judiciously, the reduction in efficiency caused by the common-gate device on-resistance is negligible compared to the increase in efficiency because of high supply voltage enabled by the cascode configuration. Another issue with the cascode is the potential instability. This will be elaborated in Chapter 6. Again, this can be overcome through careful design.

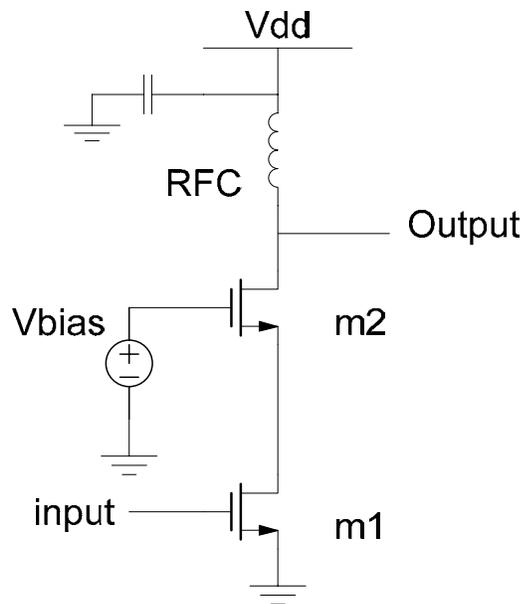


Figure 4.1: The cascode configuration with two NMOS transistors

### 4.1.2 Totem-Pole Technique

The totem-pole amplifier [4.3] is also known as “beanstalk” amplifier. It is a technique to obtain voltage swing greater than breakdown voltage by placing the output of several transistors in series as shown in Figure 4.2, so that the individual transistors do not have to withstand the full voltage swing at the output of the amplifier.

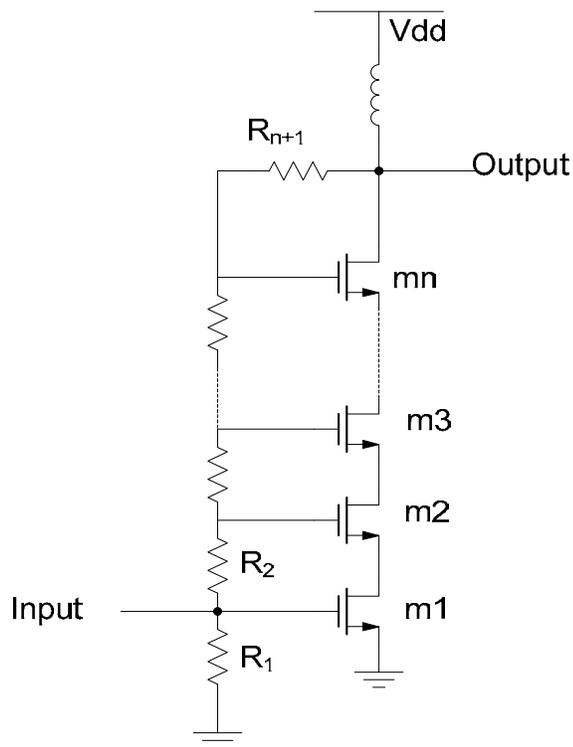


Figure 4.2: Beanstalk amplifier

The name “totem-pole” comes from the bias ladder. The resistors ladder will bias the circuit up and ensure a predictable division of drain-to-source voltage. For RF or microwave frequency operation, the signal from the input port would have to propagate up to the gate. This will cause a delay and imbalance of each device, so that the output is

not synchronized to add up in phase. This will degrade output power, power efficiency, and cause distortion in some applications.

### 4.1.3 Stacked Transistors Amplifier

To eliminate the high frequency limitation of “bean-stalk” amplifier, McRory et al. proposed a stacked power amplifier using transformer coupling to supply input signals as shown in Figure 4.3 [4.4]. The resistors ladder is designed to bias the transistors up. Capacitors are large enough to be treated as AC short at the frequency of operation. This will bootstrap the input of each transistor with its source, so that the output swing can exceed the drain-to-source breakdown voltage as long as it is less than the junction breakdown voltage.

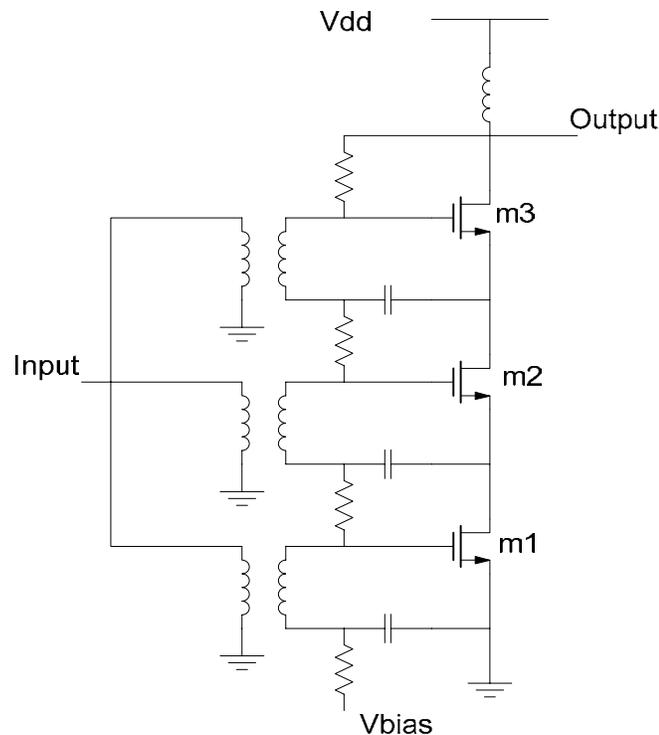


Figure 4.3: A three FET stacked power amplifier

## 4.2 Parallel Combining

Instead of increasing output swing by combining transistors in series, power could be combined from several small or unit amplifiers operating in parallel. Apparently direct connection of multiple small amplifiers is generally impractical as the PAs “talk” to each other. Interaction among small amplifiers should be judiciously managed so that outputs from small amplifiers are combined in a healthy fashion. Hence it is necessary to build power combiners to perform this function. There are many different ways to build power combiners, using lumped components or distributed approach. Among those, transmission-line based power combiner and transformer based power combiner are probably two most popular measures<sup>25</sup>.

### 4.2.1 Transformer Based Power Combining

This power combining approach was an old idea since 1960s [4.5]. Since then, transformers have been widely adopted as a means for splitting or combining RF power. To illustrate how transformer based power combining works, an example of a two-way power combined amplifier is used here (Figure 4.4). Two transconductance PAs are driven 180° out of phase with respect to each other.

For the push-pull operation, the amplitude of  $I_1$  equals to that of  $I_2$ , and the voltage amplitudes are also equal. It is obvious that

$$I_1 = I_2 = \frac{n}{m} I_o$$
$$V_1 = V_2 = \frac{1}{2} \frac{m}{n} V_o$$

---

<sup>25</sup> Because those elements are passive in nature, they can often be used to split power as well.

And each PA sees a load resistance of

$$R_1 = R_2 = \left(\frac{m}{n}\right)^2 \frac{R_L}{2}$$

Apparently, both PA deliver equal amount of power:

$$P_1 = P_2 = \frac{1}{2} \frac{V_1^2}{\frac{m^2}{n^2} \frac{R_L}{2}} = \frac{n^2}{m^2} \frac{V_1^2}{R_L}$$

or

$$P_1 = P_2 = \frac{1}{2} I_1^2 \frac{m^2}{n^2} \frac{R_L}{2} = \frac{1}{4} I_1^2 \frac{m^2}{n^2} R_L$$

The total power delivered to the load is:

$$P_L = \frac{1}{2} \frac{V_o^2}{R_L} = \frac{1}{2} \frac{\left(2 \frac{n}{m} V_1\right)^2}{R_L} = 2 \frac{n^2}{m^2} \frac{V_1^2}{R_L}$$

or

$$P_L = \frac{1}{2} I_o^2 R_L = \frac{1}{2} \frac{m^2}{n^2} I_1^2 R_L$$

Thus,

$$P_L = P_1 + P_2$$

Although transformer based power combining is straightforward to implement, high insertion loss of on-chip transformer (2~3-dB) has prevented its presence in PAs with CMOS technologies. Recently, fully integrated transformer based power combining has been demonstrated in [4.6], with so-called “slab” inductors to realize highly efficient on-chip distributive active transformer (DAT). Figure 4.5 shows the representative drawing of a PA implemented with DAT structure.

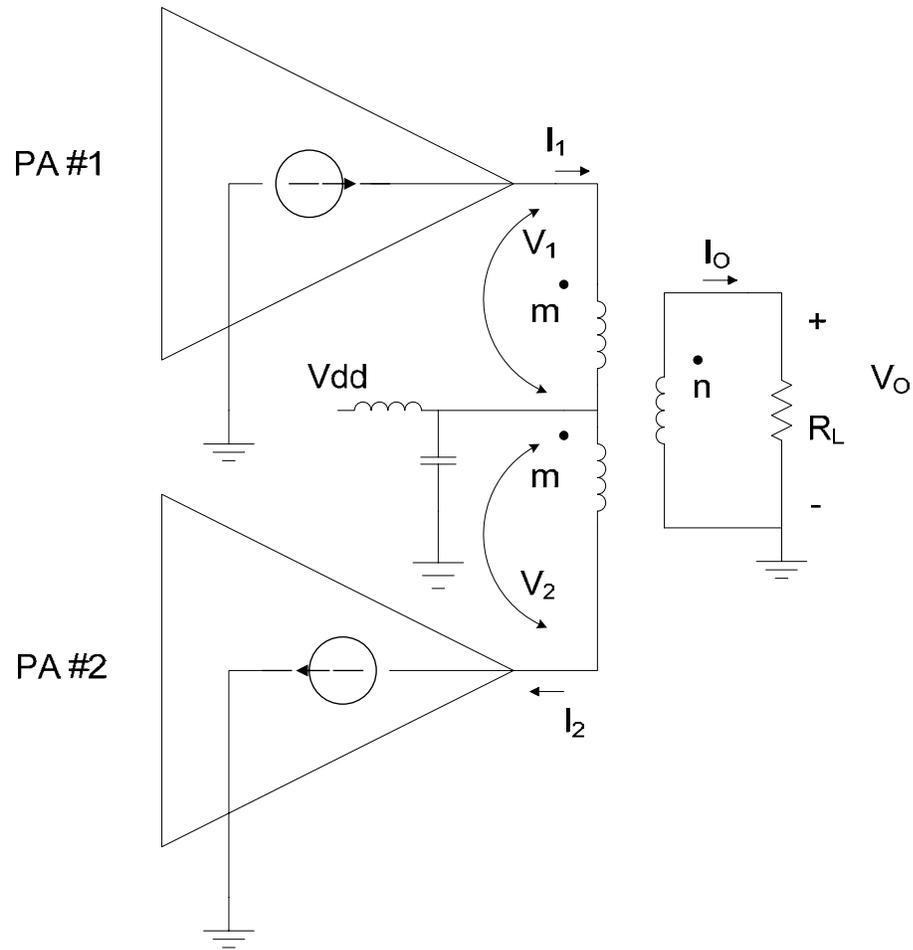


Figure 4.4: A two-way power combined amplifier with transformers

One of the primary advantages of the DAT is the use of high Q 1:1 transformer. By stacking the secondary of the 1:1 transformer in series, it combines the power from several parallel driven small amplifiers with high efficiency. Circular geometry is adopted as a means to create low-loss virtual ac grounds without using long metal leads. The double-differential architecture requires every transistor to be active to create low loss AC grounds on-chip. This approach effectively overcomes the layout limitation brought by slab inductors. It eliminates the need of long interconnects between two ports of a slab inductor, thus avoids compromising the amplifier performance. Despite these

advantages, the circular geometry DAT structure has some drawbacks. These drawbacks are inherent due to the structural characteristics [4.7-4.9]. Especially, it is not suitable to implement linear power amplifier, and suffers from inherent coupling between input and output.

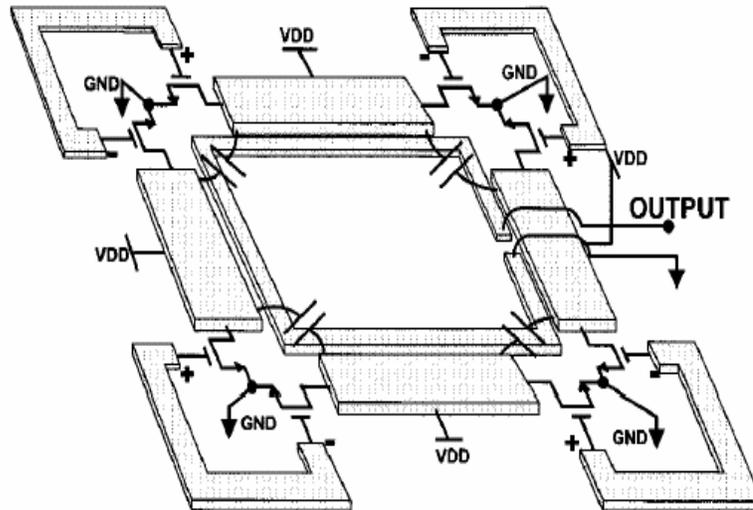


Figure 4.5: An 8-way power combined PA with DAT in [4.6]

#### 4.2.2 Transmission Line Based Power Combining

There are many ways to build a power combiner with transmission lines, usually quarter-wave transmission lines. Although the size of on-chip transmission lines may seem impractical at lower frequency, they become more and more important as frequency of emerging applications is moving up. Besides, techniques such as slow-wave structures [4.10] have been proposed to reduce the dimensions of on-chip transmission lines. And lumped equivalent elements have been used to synthesize transmission lines at low GHz range. In some applications, transmission line based

approach might even be a better choice. For the remaining part of this section, the Doherty combiner and the Wilkinson combiner will be briefly reviewed.

#### 4.2.2.1 Doherty Combiner

The Doherty amplifier, first proposed in 1936 by Doherty<sup>26</sup> [4.11], is primarily an average efficiency enhancement technique. There are many publications [4.12, 4.13] addressing this aspect. Interested readers are encouraged to consult those resources. Here, the focus is on power combining of the main amplifier and the auxiliary amplifier.

Figure 4.6 shows one possible configuration of Doherty amplifier where the main amplifier and the auxiliary amplifier contribute equal power at peak power. The outputs of two amplifiers are combined through quarter-wave transmission lines or networks. The auxiliary amplifier is biased with a smaller conduction angle compared to the main amplifier, such as in class C and class AB respectively. When the input signal amplitude is low, only the main amplifier is active. Both amplifiers contribute output power when the input signal amplitude is high.

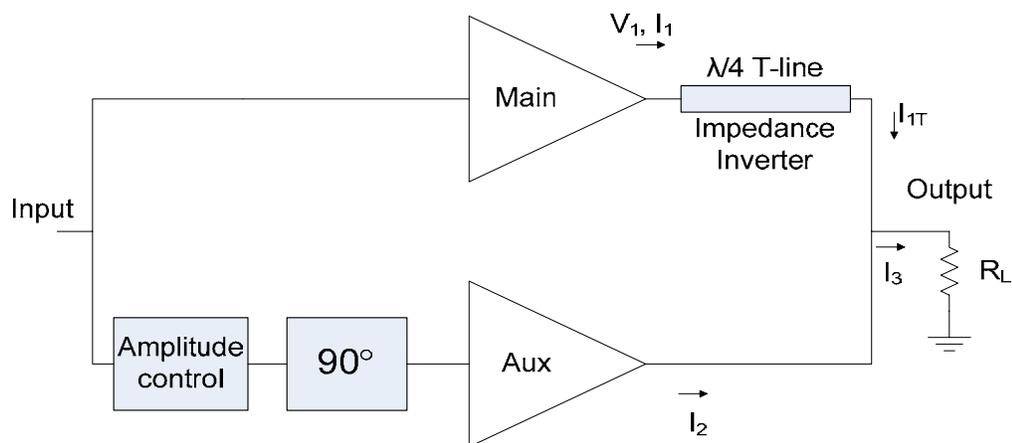


Figure 4.6: A possible configuration of Doherty Amplifier

<sup>26</sup> Just like many others, the Doherty amplifier was invented in Bell Labs.

To understand how the Doherty amplifier really works, active load-pull technique should be understood first. Since it is well explained in [4.12], it will not be repeated here. The operation of the Doherty amplifier can be explained by dividing it into low-power, medium power and high power region, assuming lossless matching networks.

In the low-power region (Figure 4.7(a)), the instantaneous amplitude of the input signal is not sufficient to turn on the auxiliary power amplifier, so it will remain off and appear as an open-circuit without any interaction with the main amplifier. The main amplifier sees the load inverted by the quarter-wave transmission line and operates exactly the same as an ordinary power amplifier. The output swing increases linearly with input until reaching the clipping point. As the input signal amplitude keeps increasing into the medium-power region, the Doherty amplifier enters into medium-power region (Figure 4.7(b)). The main amplifier is in the constant maximum voltage condition, but the effective load decreases dynamically with the increase of the input signal amplitude due to the load-pulling effect of the auxiliary amplifier. In this region, the auxiliary amplifier also sees load-pulling effect that the effective load also decreases with the increase in the input signal amplitude. Finally, when both amplifiers contribute same amount of power to the load, the Doherty amplifier is in the peak-power mode (Figure 4.7(c)). Note the importance of a quarter-wave transmission line between the resistive load and the main amplifier output. This transmission line acts as an impedance inverter, which causes the impedance seen by the main amplifier to decrease as the auxiliary amplifier ramps up. This guarantees highly efficient power combining between the two amplifiers.

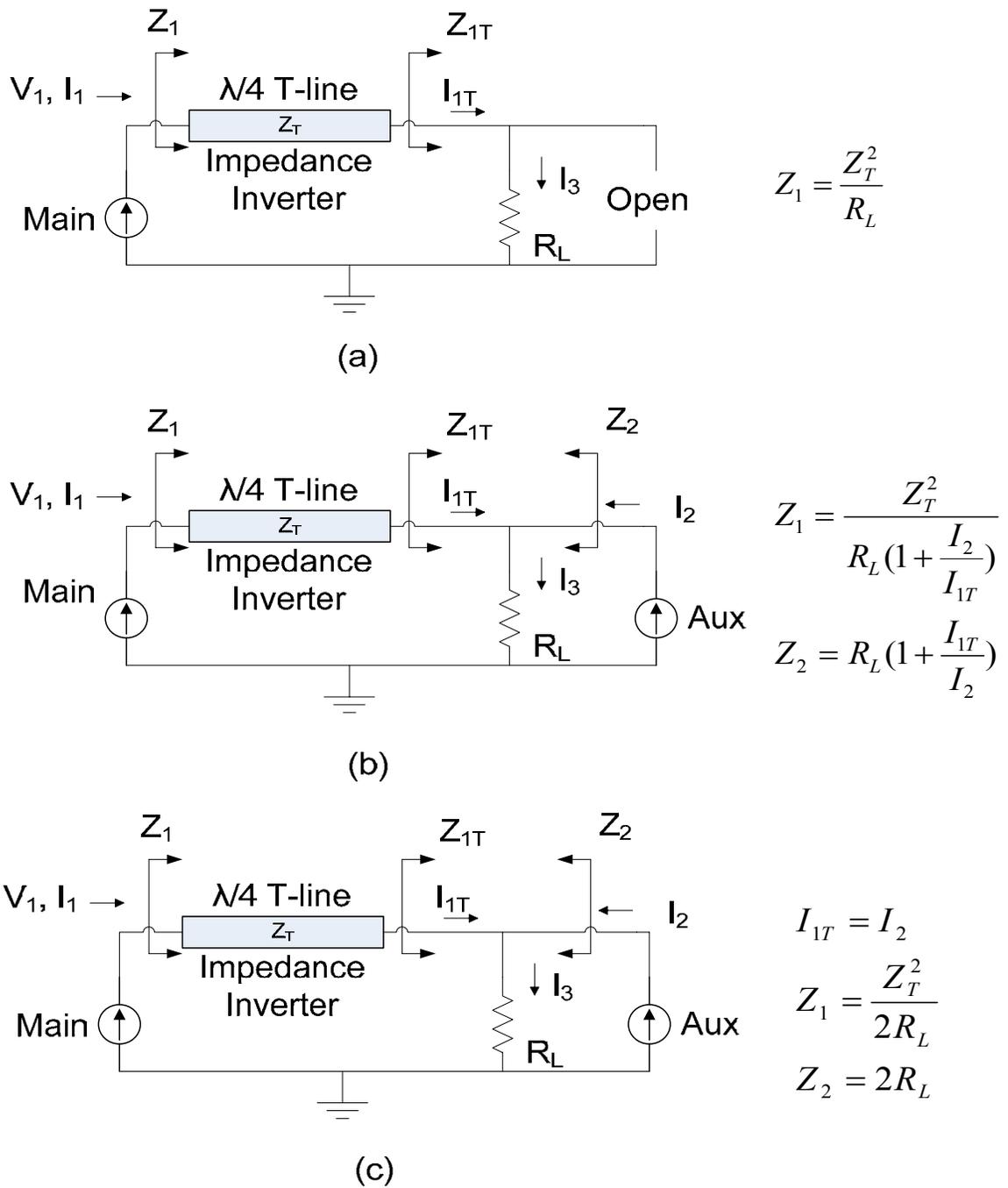


Figure 4.7: Operation of a Doherty amplifier, (a) low power mode; (b) medium-power mode; (c) peak-power mode

Although there are techniques to reduce dimensions of on-chip transmission lines, lumped equivalent circuits are used in some Doherty Amplifiers to save die area [4.1, 4.14]. A lossless transmission line element can be modeled with inductors and capacitors in a “ $\pi$ ” or “T” configuration (Figure 4.8). Either arrangement will work, although “ $\pi$ ” configuration is often preferred for on-chip implementation due to loss of on-chip inductors. For a given frequency of operation, if the characteristic impedance of the transmission line and the electric length are known, it is straightforward to calculate the value of inductors and capacitors.

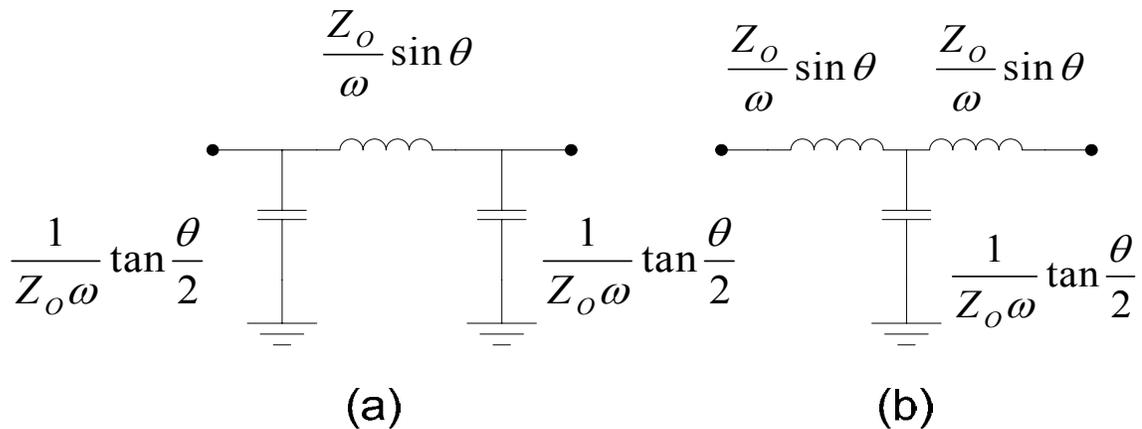


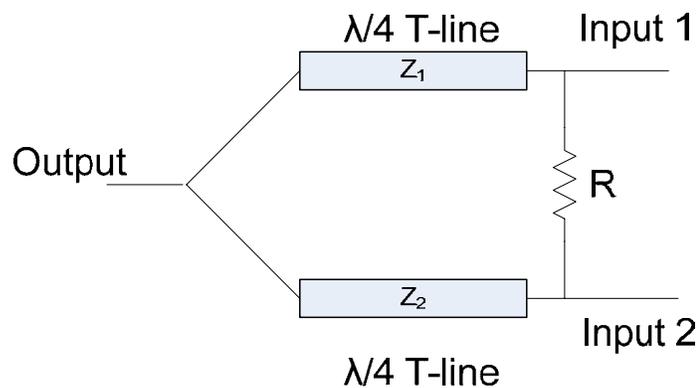
Figure 4.8: Lumped equivalent circuits of transmission lines, (a) “ $\pi$ ” configuration; (b) “T” configuration

To give a picture of using lumped components for quarter-wave transmission line synthesis, an example is given here. Assuming a quarter-wave length transmission line with 20- $\Omega$   $Z_0$  at 2-GHz is needed in a design, an inductor of 1.59-nH and two capacitors of 4-pF could be used instead to act as a quarter-wave transmission line. The ultimate limitation of building a highly efficient integrated Doherty combiner is again the quality

factor of on-chip passives, especially inductors. Another issue with this approach is the inherent narrow bandwidth.

#### 4.2.2.2 Wilkinson Power Combiner

In the RF/microwave community, the importance of Wilkinson power combiner is equivalent to that of Widlar current source in the analog community. It was invented around 1960, relying on quarter-wave transmission lines to match the split ports to the common port [4.15]. Figure 4.9(a) shows a 2-way Wilkinson power combiner. In the context of power amplifiers design, matching every port is not necessary at all. In fact, conjugate match should be avoided in almost every case for better performance. Since there are many excellent text books, for example [4.16, 4.17], covering Wilkinson power combiner extensively, it will not be analyzed in detail here. One note, however, should be pointed out here. When in-phase outputs are combined, there is no power dissipated in the isolation resistor. It is 100% efficient just like an ideal Wilkinson power splitter. Lumped components can be synthesized to implement a Wilkinson power combiner (Figure 4.9(b)).



(a)

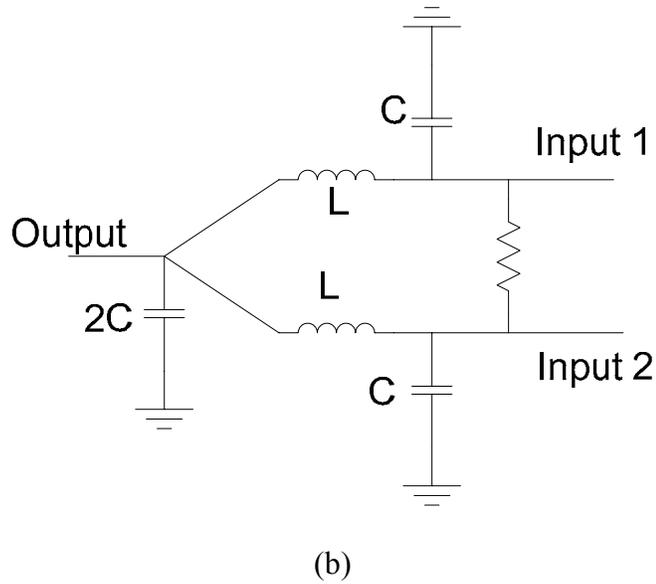


Figure 4.9: (a) A two-way Wilkinson power combiner; (b) Lumped equivalent

### 4.3 Proposed Power Combiner

#### 4.3.1 Power Combining Transformer

In previous sections of this chapter, several transformer based power combining approaches have been presented. They all have their advantages and drawbacks. A power combining transformer is proposed in this work for the first time. Figure 4.10 shows the conceptual diagram of the transformer. The main differentiation from other existing approaches is that the proposed topology provides great flexibility during implementation, and enables access and control of each unit. The ability for individual control allows designs exploring full benefits of parallelism.

To understand how the proposed power combining transformer works, a unity (1:1) transformer is briefly introduced (Figure 4.11). For an ideal 1:1 transformer, it works the same way as an ideal 1:n transformer, but without any impedance

transformation. And signals pass unmodified from the primary to the secondary side. However, a very important characteristic of transformers, electric isolation, is kept intact<sup>27</sup>. When the primary side is driven by a differential signal, a unity transformer acts as a balun, converting signals from differential to single-ended form.

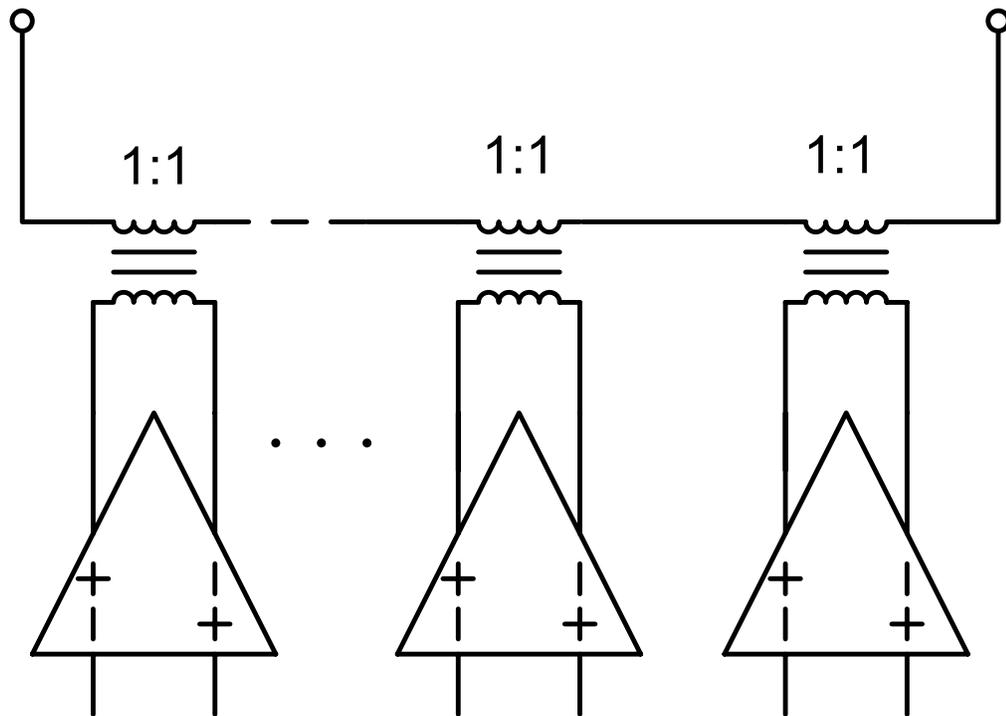


Figure 4.10: Transformer based power combining employing unity transformers<sup>28</sup>

One question may rise at this point. It is known that one of the advantages of transformer coupling is that transformer can be used as an impedance changer. Using 1:1 transformer does not offer any impedance change at all, which will certainly be a show-stopper in power amplifiers design. In this section, it will be shown that transforming

<sup>27</sup> This is the most important characteristic, in the author's opinion.

<sup>28</sup> It should be pointed out that this topology also works with transformation ratio other than 1:1.

impedance could still be achieved by connecting several 1:1 transformers together. And in the next chapter, it will be explained why 1:1 transformer is preferred as building blocks when implementing power combining transformer on silicon.

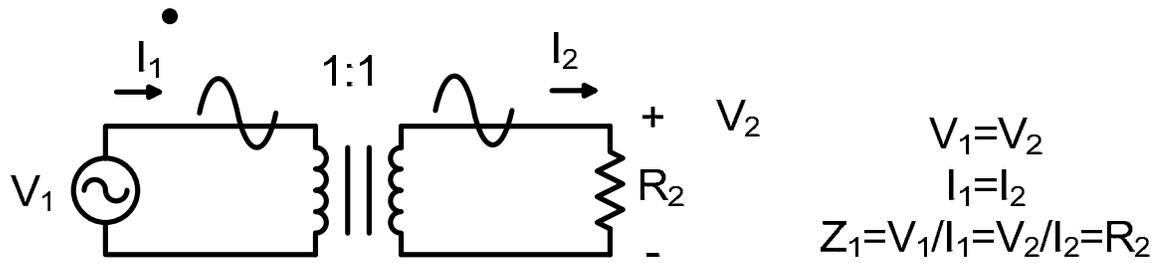


Figure 4.11: An ideal unity transformer

To obtain any impedance transformation, more than one unity transformer is needed. A four-unit power combining transformer is shown in Figure 4.12 as an example. The primary sides of four independent unity transformers are driven by four independent, nonetheless synchronized sources with the same signal level in parallel. The secondary sides of four independent unity transformers are stacked together in series. Assuming signal levels are equal on the primary sides, that is:

$$V_1 = V_2 = V_3 = V_4 = V_i$$

Because the secondary sides are connected in series, the “ac ground” of the secondary side of each unity transformer is lifted so that the ac voltages add on the secondary:

$$V_L = V_1 + V_2 + V_3 + V_4 = 4V_i$$

For current, since the secondary sides are connected in series, it forces the currents in the primary sides equal to each other:

$$I_1 = I_2 = I_3 = I_4 = I_L$$

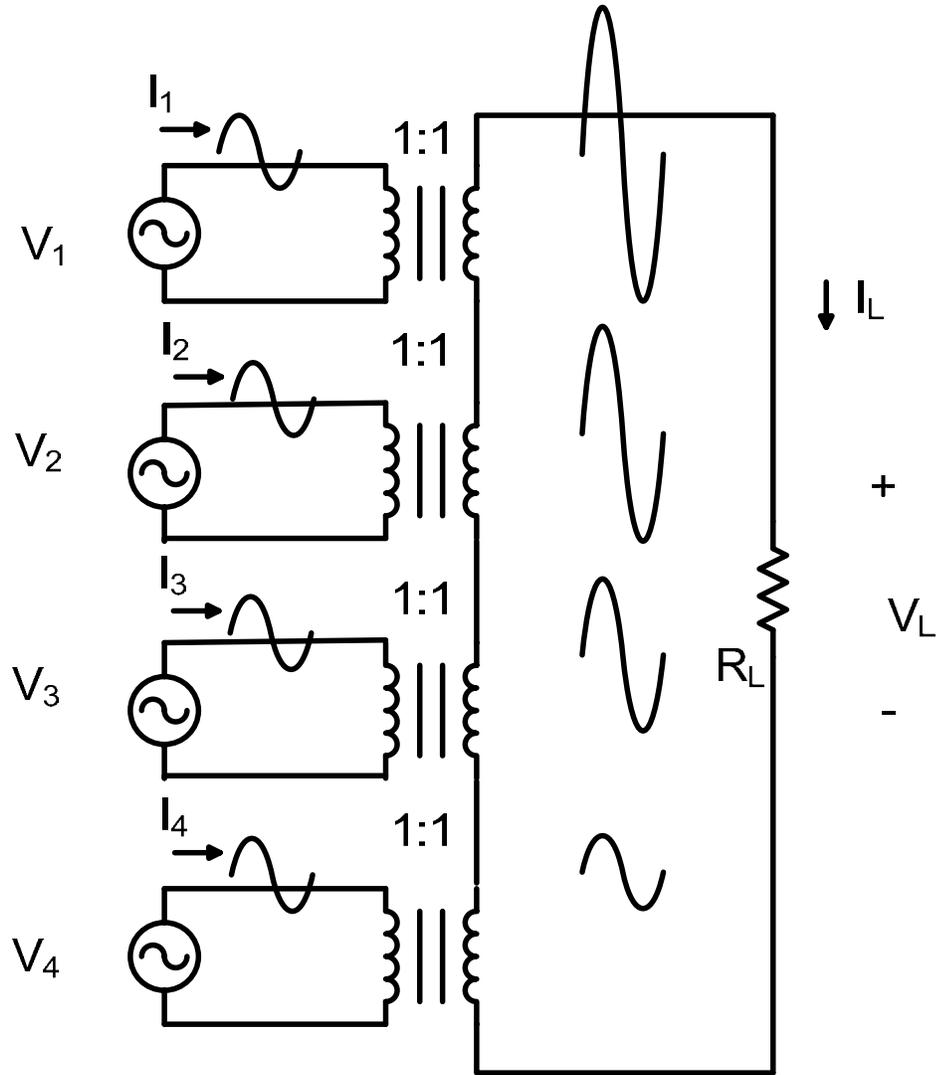


Figure 4.12: A four-way power combining transformer composed of 4 unity transformers

The impedance seen from the primary side of each unity transformer can be derived:

$$Z_1 = Z_2 = Z_3 = Z_4 = \frac{V_1}{I_1} = \frac{1}{4} \frac{V_L}{I_L} = \frac{1}{4} R_L$$

The power delivered to the load is:

$$P_L = \frac{1}{2} \frac{V_L^2}{R_L} = \frac{1}{2} \frac{(4V_i)^2}{R_L} = 8 \frac{V_i^2}{R_L}$$

And the power from each source is:

$$P_1 = P_2 = P_3 = P_4 = \frac{1}{2} \frac{V_i^2}{Z_1} = \frac{1}{2} \frac{V_i^2}{\frac{1}{4} R_L} = 2 \frac{V_i^2}{R_L}$$

Therefore, it is obvious that power is combined from each unity transformer and delivered to the load:

$$P_L = P_1 + P_2 + P_3 + P_4$$

Several important characteristics of the power combining transformer with N unity transformers are summarized here:

- a. Power generated from primary sides are picked up by the secondary side and then combined through magnetic coupling. The combining ratio is N.
- b. The ac voltages at the secondary sides add to achieve enough voltage swing. Due to electronic isolation of the transformer, the primary sides still work with low voltage, away from breakdown region. The voltage ratio between the swing at the load and the swing at one of the primaries is N.
- c. Contrarily, the current on both sides of the transformer equal to each other. The ratio of total currents between the two sides is 1/N. And the current ratio of current in the secondary sides to that of one of the primaries is obviously  $1^{29}$ .
- d. The impedance seen by each port at the primary sides is N times smaller than the load at the secondary. The impedance transformation ratio is N.

Several advantages and potential applications offered by this power combining transformer are presented, benefited from parallelism using power combining transformer.

#### 4.3.1.1 Noise

---

<sup>29</sup> This is an important feature in practice since it effectively reduces loss caused by parasitics. This will be examined later in detail.

It may seem irrelevant here to talk about noise in PAs. This impression is certainly invalid in a full duplex system. Due to finite rejection provided by duplex filter, excessive noise from the power amplifier will reduce the receiver sensitivity. Even worse, the disturbance might be dependent on the input signal level at the receiver input, which further complicates the system design. Considering an N-way power combining PA with N identical amplifiers, an equivalent model (Figure 4.13) is used to study signal and noise relationship between input and output.

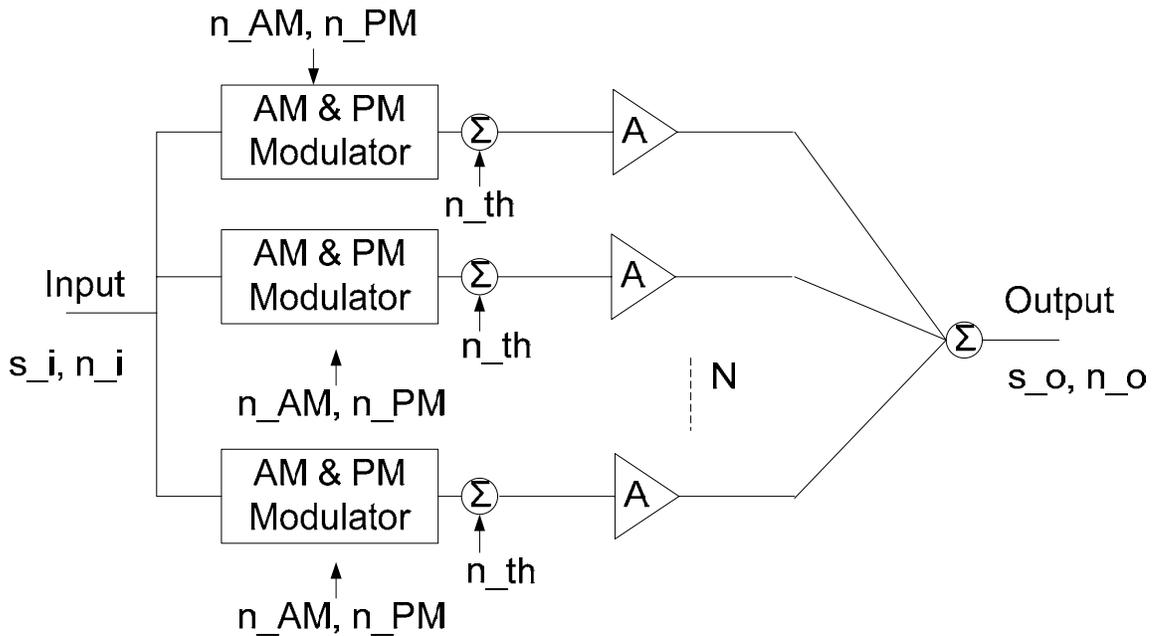


Figure 4.13: An equivalent model for an N-way power combining PA with additive noise<sup>30</sup>

Noise in the combining PA can be divided into the following categories:

<sup>30</sup> Signals are represented in voltage domain in the context of integrated circuit design

- a. Correlated noise from a source common to all the individual amplifiers, including thermal noise, amplitude modulation (AM) and phase modulation (PM) noise generated by circuits preceding PAs.
- b. Uncorrelated thermal noise generated in the individual amplifiers.
- c. Uncorrelated AM noise and PM noise generated by individual amplifiers as a result of the up-conversion of low frequency noise. Such noise is generally characterized by a 1/f noise spectrum.

Since AM noise and PM noise are up-converted 1/f noise, and will have exactly the same characteristics as thermal noise, the following derivations will only have thermal noise (Figure 4.14) in expressions to avoid lengthy equations.

Because the signals will be added in amplitude, the output voltage is:

$$s_o = N \cdot A \cdot s_i$$

The input signal has noise common to all individual amplifiers, therefore this noise will be added up in amplitude at the output. The noise generated by each branch is, however, uncorrelated. The total output noise power is:

$$n_o^2 = (N \cdot A \cdot n_i)^2 + N \cdot (A \cdot n_{th})^2$$

Then SNR at the output is:

$$SNR_{output} = \frac{s_o^2}{n_o^2} = \frac{s_i^2}{n_i^2 + \frac{1}{N} n_{th}^2}$$

Depending on the input noise level, the improvement to the SNR of an individual branch could be as high as N. Assuming that input signal level, input noise level, input

referred equivalent noise<sup>31</sup>, output signal level and total gain ( $G = N \cdot A$ ) are fixed for a certain application, the total output noise power can be written as:

$$n_o^2 = (G \cdot n_i)^2 + \frac{1}{N} \cdot (G \cdot n_{th})^2$$

Obviously as  $N$  increases, output noise is effectively reduced.

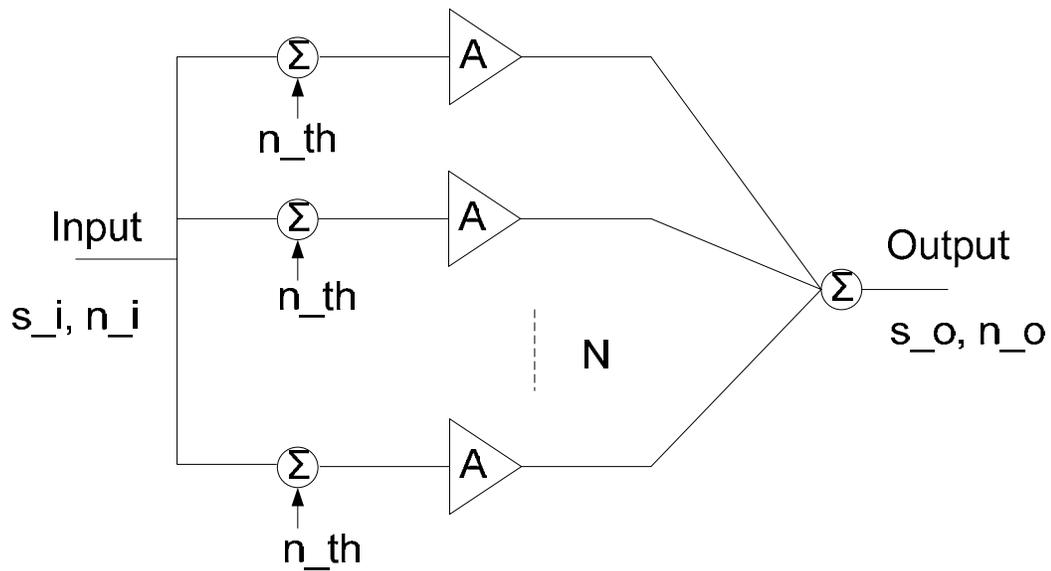


Figure 4.14: A simplified equivalent model for an N-way power combining PA with additive noise

#### 4.3.1.2 Average Efficiency Enhancement

One inherent problem of PAs is that conventional PA designs achieve maximum efficiency only at a single power level, around the peak output power. As the output power is backed off from peak, the efficiency drops sharply. Various average efficiency enhancement techniques have been proposed to solve this problem as reviewed in Chapter 2. Among those techniques, Dynamic Load Modulation (DLM) is an attractive

<sup>31</sup> It can be shown this is a valid assumption.

approach<sup>32</sup>. The power combining transformer proposed in this work has a useful property to modulate the load seen by individual amplifiers on the primary sides. Two types of load modulation could be implemented, namely digital and analog load modulation<sup>33</sup>. Here, digital control is introduced because of its simplicity, with a four-way (N=4) power combined amplifier as an example. Each amplifier acts as a current source with transconductance  $g_m$ . Maximum swing is  $V_o$  at the output of each amplifier, when input swing is  $V_i$ . At primaries, amplifiers are equally weighted. Individual amplifiers at the primaries will be turned on or off as required output power varies, controlled by a thermometric input code (Figure 4.15).

Full power: At the peak power, every individual amplifier is on. Now the load seen by each amplifier is:

$$R = \frac{1}{4} R_L$$

The efficiency of each amplifier, as well as the efficiency of power combined amplifier, reaches maximum.

$$\eta_{overall} = \eta_{unit} = \eta_{max}$$

Voltage gain of each amplifier is:

$$A = gm \cdot \frac{1}{4} R_L$$

Total gain of power combining amplifier is:

$$V\_Gain = N \cdot A = gm \cdot R_L$$

And the peak RF output power is:

---

<sup>32</sup> The Doherty Amplifier is an example.

<sup>33</sup> Analog load modulation is similar to Doherty technique.

$$P_{peak} = N \cdot P_{unit\_peak} = 4 \cdot \frac{1}{2} \frac{V_o^2}{\frac{1}{4} R_L} = 8 \frac{V_o^2}{R_L}$$

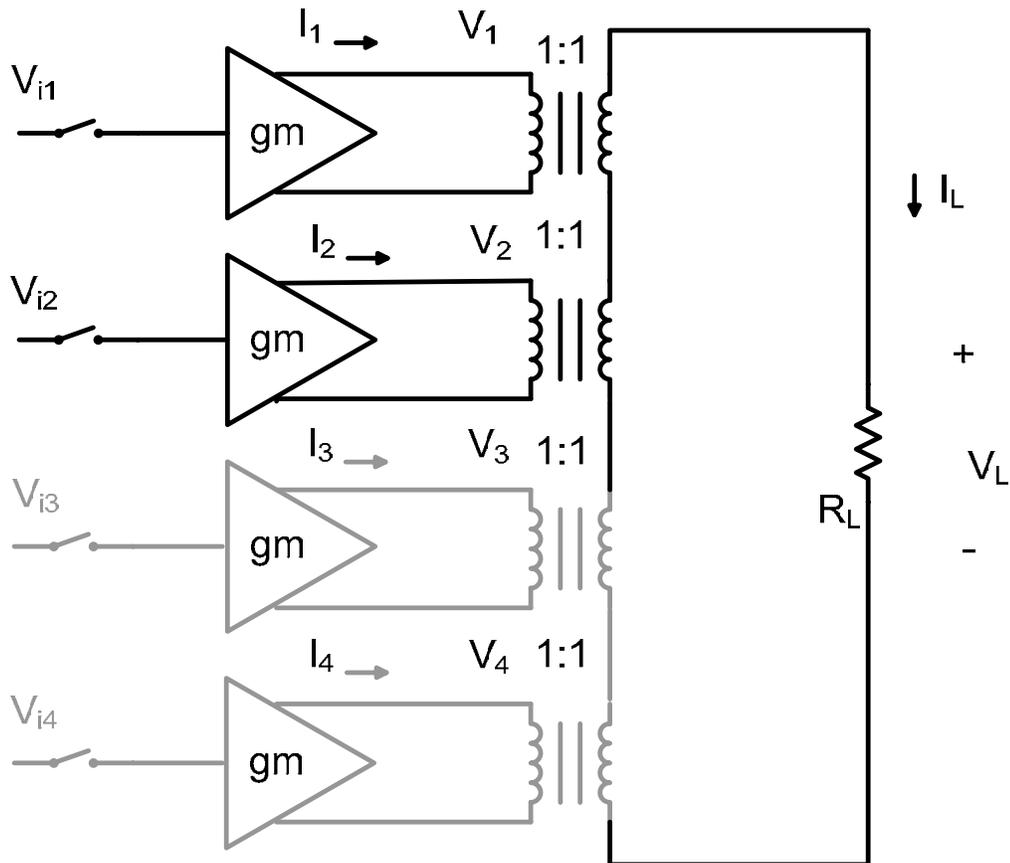


Figure 4.15: A four-way power combining amplifier is reconfigured to a two-way power combining amplifier with digital control for enhanced average efficiency.

2.5-dB back-off: As peak output is not needed, input drive is reduced to lower output power. When power is 2.5-dB backed off, input swing is reduced to  $3/4 \cdot V_i$ . At this point, the output swing of each individual amplifier is  $3/4 \cdot V_o$ . Therefore, the efficiency of each amplifier as well as that of the power combined amplifier drop rapidly. However, if one amplifier is turned off, efficiency could be greatly enhanced. Since there are only three

amplifiers (N=3) contributing to the output, a four-way power combined amplifier is reconfigured to a three-way power combined amplifier. The load seen by each active amplifier is now:

$$R = \frac{1}{3} R_L$$

Voltage gain of each amplifier becomes:

$$A = gm \cdot \frac{1}{3} R_L$$

The output swing of each active amplifier returns to the maximum value:

$$V_{output} = A \cdot V_{input} = gm \cdot \frac{1}{3} R_L \cdot \frac{3}{4} V_i = V_o$$

So do the efficiency of individual amplifiers and that of the power combined amplifier:

$$\eta_{overall} = \eta_{unit} = \eta_{max}$$

Total gain of power combining amplifier is:

$$V\_Gain = N \cdot A = gm \cdot R_L$$

And the RF output power at this point is:

$$P_{out} = N \cdot P_{unit} = 3 \cdot \frac{1}{2} \frac{V_o^2}{\frac{1}{3} R_L} = \frac{9}{2} \frac{V_o^2}{R_L} = \frac{9}{16} P_{peak}$$

6-dB back-off: If the input is further reduced to  $1/2 \cdot V_i$ , one more individual amplifier could be turned off to improve efficiency at back-off. Now a four-way power combined amplifier is reconfigured to a two-way (N=2) power combined amplifier. The load seen by each active amplifier is now:

$$R = \frac{1}{2} R_L$$

Voltage gain of each amplifier becomes:

$$A = gm \cdot \frac{1}{2} R_L$$

The output swing of each active amplifier returns to the maximum value:

$$V_{output} = A \cdot V_{input} = gm \cdot \frac{1}{2} R_L \cdot \frac{1}{2} V_i = V_o$$

So do the efficiency of individual amplifiers and that of the power combined amplifier:

$$\eta_{overall} = \eta_{unit} = \eta_{max}$$

Total gain of power combining amplifier is:

$$V\_Gain = N \cdot A = gm \cdot R_L$$

And the RF output power at this point is:

$$P_{out} = N \cdot P_{unit} = 2 \cdot \frac{1}{2} \frac{V_o^2}{\frac{1}{2} R_L} = 2 \frac{V_o^2}{R_L} = \frac{1}{4} P_{peak}$$

12-dB back-off: As the input is reduced to  $1/4 \cdot V_i$  at 12-dB back-off, only one amplifier need to be on ( $N=1$ ). The load seen by each active amplifier is just the load itself without any impedance transformation:

$$R = R_L$$

Voltage gain of each amplifier becomes:

$$A = gm \cdot R_L$$

The output swing of each active amplifier returns to the maximum value:

$$V_{output} = A \cdot V_{input} = gm \cdot R_L \cdot \frac{1}{4} V_i = V_o$$

So does the efficiency of the individual amplifier and that of the power combined amplifier:

$$\eta_{overall} = \eta_{unit} = \eta_{max}$$

Total gain of power combining amplifier is:

$$V\_Gain = N \cdot A = gm \cdot R_L$$

And the RF output power at this point is:

$$P_{out} = N \cdot P_{unit} = 1 \cdot \frac{1}{2} \frac{V_o^2}{R_L} = \frac{1}{2} \frac{V_o^2}{R_L} = \frac{1}{16} P_{peak}$$

It should be pointed out that voltage gain is constant as output power is backed off from peak, which is a desirable feature for system design. Figure 4.16 illustrates the efficiency of a four-way ideal transformer combined power amplifier with digital control.<sup>34</sup>

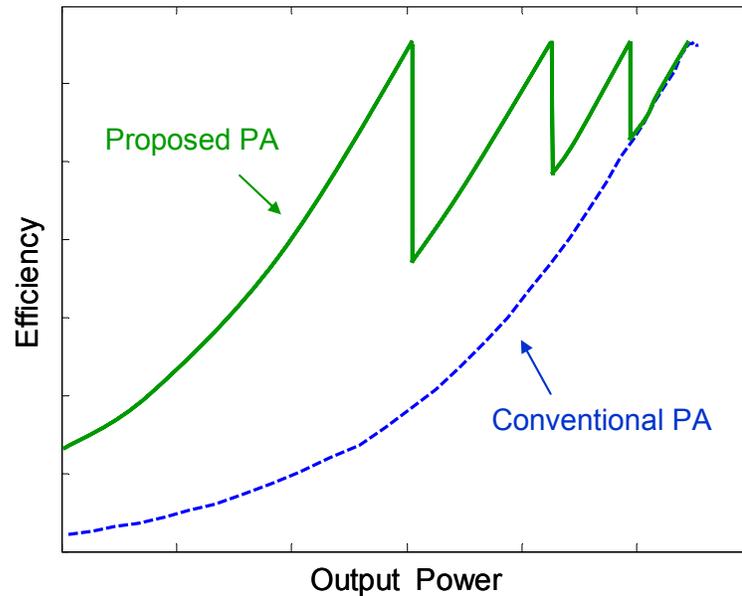


Figure 4.16: A comparison of efficiency between the PA based on proposed power combining transformer and the conventional PA

<sup>34</sup> If unit amplifier is class-A, the efficiency of unit amplifier degrades at power back-off. However, the overall power amplifier efficiency is still improved. Class A PA is rarely seen in practice. Most linear PAs are class-AB or class B.

### 4.3.1.3 Transformer Coupled Outphasing Amplifier<sup>35</sup>

Outphasing technique was proposed also in the 1930s [4.18] to improve efficiency (including average efficiency) and linearity of AM-broadcast transmitters. Over the years, the complexity of the analog signal separator implementation has prevented the outphasing approach from being widely accepted. As digital signal processing power improves vastly, however, it starts to attract more interests than before. In recent publications, it is often referred as a LINC (Linear amplification using Nonlinear Components) system. Although linear amplifiers could be used to build outphasing amplifiers, nonlinear amplifiers have inherent advantage in terms of efficiency<sup>36</sup>.

The basis for the outphasing amplifier (Figure 4.17) is that modulated signal is separated into two outphased signals with constant envelopes, which can be explained by the trigonometric identity <sup>37</sup>[4.12]:

$$\cos A + \cos B = 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$$

If the angles A and B now represent two time-varying signals,

$$A = \omega t + \varphi \qquad B = \omega t - \varphi$$

then

$$\cos(\omega t + \varphi) + \cos(\omega t - \varphi) = 2 \cos(\omega t) \cos \varphi$$

Now referring to Figure 4.16, if a modulated signal  $S_i(t)$  is applied to the input, the signal separator generates two equal, fixed amplitude signals,  $S_{i1}(t)$  and  $S_{i2}(t)$ , such that if

$$S_i(t) = A(t) \cos(\omega t + \theta(t))$$

---

<sup>35</sup> This is an analog way to improve efficiency at power back-off

<sup>36</sup> In practice, the nonlinear PAs are driven into saturation, and are a lot less sensitive to process variations compared to linear PAs.

<sup>37</sup> It can also be explained in a polar system.

then

$$S_{i1}(t) = \cos(\omega t + \theta(t) + \arccos(A(t)))$$

$$S_{i2}(t) = \cos(\omega t + \theta(t) - \arccos(A(t)))$$

$$\varphi(t) = \arccos(A(t))$$

If the amplifiers have a voltage gain of  $G$ , the combined outputs is:

$$S_o(t) = G(S_{i1}(t) + S_{i2}(t)) = 2GA(t) \cos(\omega t + \theta(t))$$

Since the input signals to the amplifiers have constant envelope, regardless of the amplitude of input signal to the signal separator, nonlinear amplifiers could be used to amplify the signals after the signal separator, and the amplitude information of the original input signal is then recovered at the output in a summing operation.

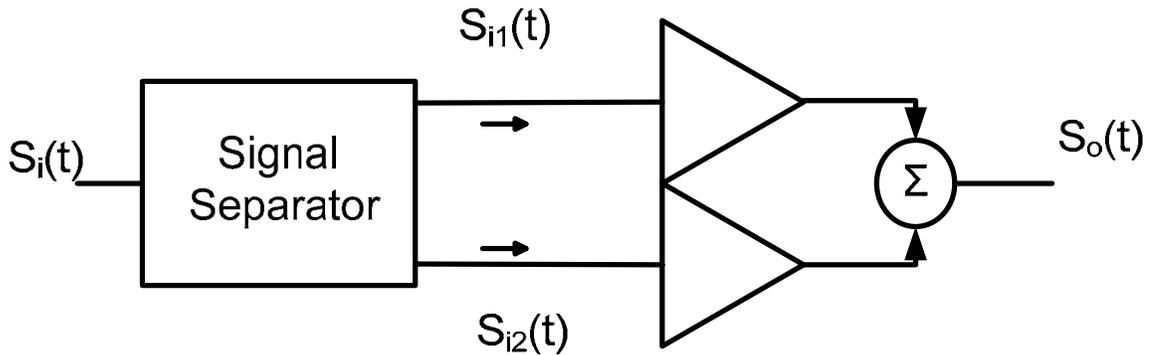


Figure 4.17: Simplified block diagram of an outphasing amplifier

At this stage, the outphasing technique appears more like a linearization scheme than an average efficiency enhancement technique. Although it permits high efficiency nonlinear amplifiers to be used, it would seem that the overall efficiency will still scale with power level. For example, at low power region, both amplifiers are still generating maximum output only to have most of the power “outphased” to produce appropriate

signal level at the output. If the combiner at the output only performs simple mathematical summing function, it will be true. This precisely explains the need for a non-conventional power combiner, because the key action of an outphasing amplifier takes place at the output and purely relies on the mutual active load pulling of the two devices delivering power into a common load. Conventionally, a solution so-called Chireix power-combining technique which adds transmission line couplers and shunt reactance [4.19] was used to fulfill that function (Figure 4.18). Here, it will be shown that the transformer proposed in this work can also satisfy the requirements.

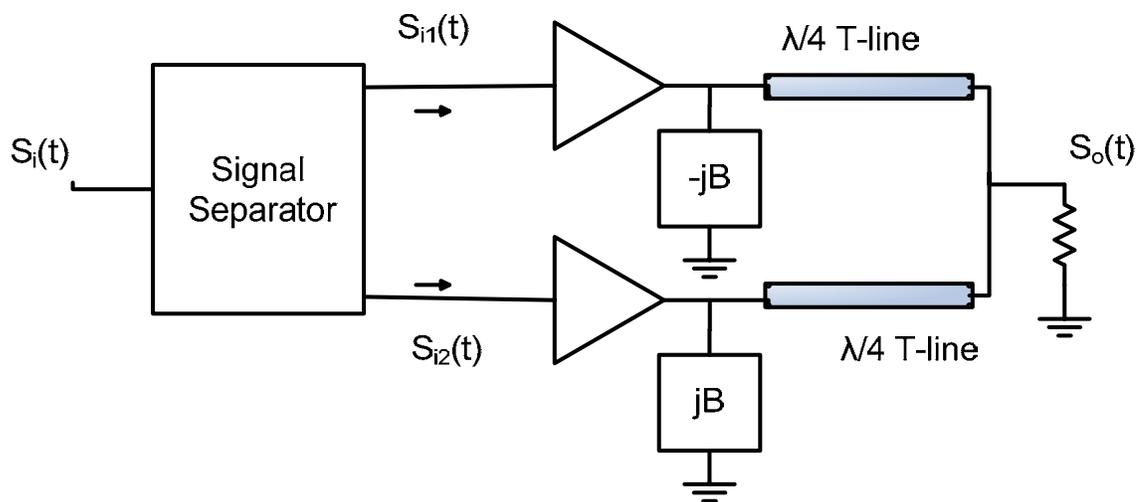


Figure 4.18: A Chireix's outphasing amplifier

Figure 4.19 illustrates an outphasing PA with two power amplifiers, combined with the proposed power combining transformer. Each power amplifier is designed as a switching power amplifier, which could be modeled as voltage sources. One thing that should be noted is that the winding is different from the previous implementation.

The signal separator circuits generate two sinewave signals with phases of  $\varphi$  and  $-\varphi$ . These two signals are then amplified by the nonlinear power amplifiers and added together to produce the output signal. The outputs of the two power amplifiers (Figure 4.20) can be written in phasor form<sup>38</sup> as:

$$\begin{aligned}V_1 &= V(\cos \varphi + j \sin \varphi) \\V_2 &= V(\cos \varphi - j \sin \varphi)\end{aligned}$$

The output across the load  $R_L$  is:

$$V_L = V_1 - V_2 = 2Vj \sin \varphi$$

so that the output voltage after summing is proportional to  $\sin \varphi$ . If the input signal separator generates a phase shift such that

$$\varphi = \arcsin(A(t))$$

then the output voltage at the load resistor fully recovers of the original AM signal. When  $\varphi = 90^\circ$ , two output voltages combine, resulting maximum amplitude. When  $\varphi = 0^\circ$ , zero amplitude is achieved.

Referring to Figure 4.19 (b), the current at the load,  $I_L$ , is given as:

$$I_L = \frac{V_L}{R_L} = \frac{V_1 - V_2}{R_L}$$

Therefore, the effective load seen by the two RF voltage generators  $V_1$  and  $V_2$  are:

$$\begin{aligned}Z_1 &= \frac{V_1}{V_1 - V_2} R_L = \frac{\cos \varphi + j \sin \varphi}{2j \sin \varphi} R_L = \frac{R_L}{2} (1 - j \cot \varphi) \\Z_2 &= -\frac{V_2}{V_1 - V_2} R_L = -\frac{\cos \varphi - j \sin \varphi}{2j \sin \varphi} R_L = \frac{R_L}{2} (1 + j \cot \varphi)\end{aligned}$$

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<sup>38</sup> The math will be easy to digest using phasor form because it is more intuitive.

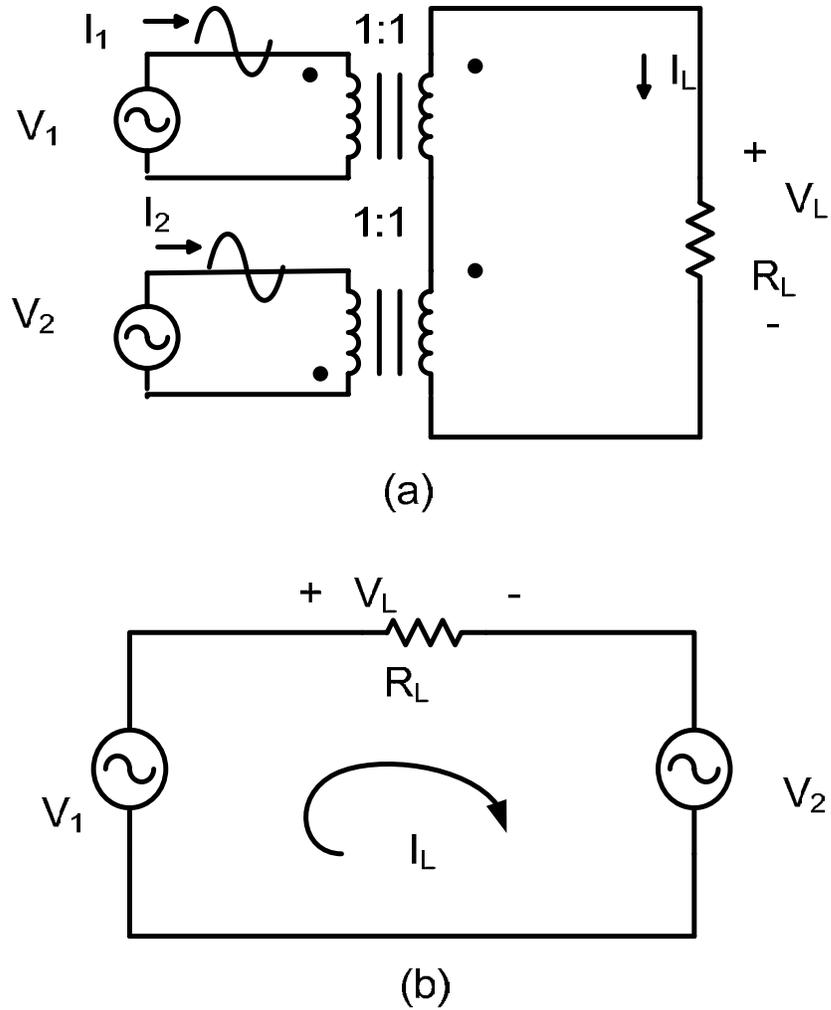


Figure 4.19: (a) An outphasing amplifier with the proposed power combiner; (b) An equivalent model of the outphasing amplifier

To further understand active load pulling effect, RF load seen by the RF generator  $V_1$  is shown in Figure 4.21 (a), a resistive component in series with a reactive component. The same kind of load modulation is also seen by  $V_2$  (Figure 4.22). The reactive component is caused by signal separator operation which generates the phase difference between two signal paths, and the reactance is a function of the phase modulation  $\phi$ . A

parallel equivalent is transformed from series configuration, shown in Figure 4.20 (b), to give more intuition for design.

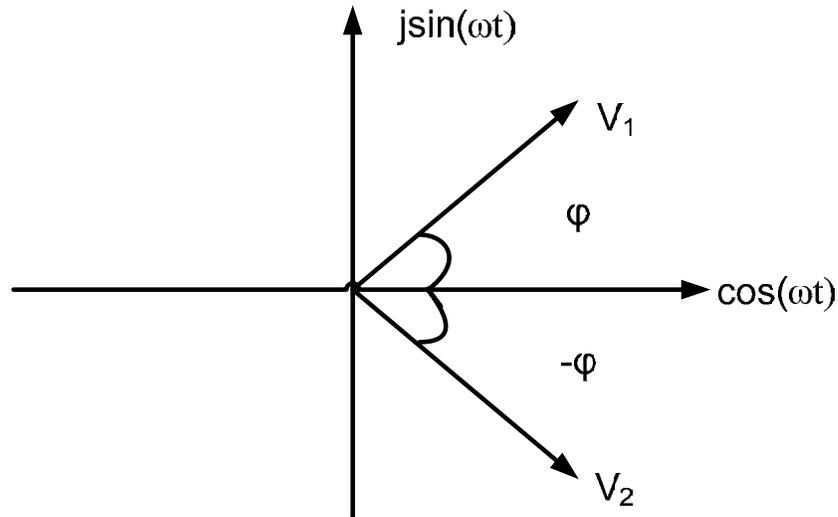


Figure 4.20: Phasor form of two voltages at the output of the two nonlinear power amplifiers for power combining.

The total output power is:

$$P_{out} = \frac{1}{2} \frac{4V^2 \sin^2 \varphi}{R_L} = 2 \frac{V^2 \sin^2 \varphi}{R_L}$$

Clearly, as the phase  $\varphi$  approaches zero degree when the output power is backed off, the reactive component value increases (Figure 4.23). This will hurt the efficiency of the RF generators at back-off region, which is certainly undesirable. As proposed by Chireix [4.18], those reactive components can be compensated. For instance, for the RF generator  $V_1$ , an inductor can be placed in shunt to resonate out the capacitive reactance. The same argument applies to  $V_2$ , where a capacitor can be placed in shunt to resonate out the inductive reactance. In practice, this could be done by switch in/out capacitor

bank. Although the magnitude of the compensating reactance will vary with phase modulation  $\varphi$ , this could be solved by switching capacitors as well.

One observation is that to deal with power back-off more than 20dB, phase modulation resolution down to several degrees is required. This is certainly achievable with today's DSP advances.

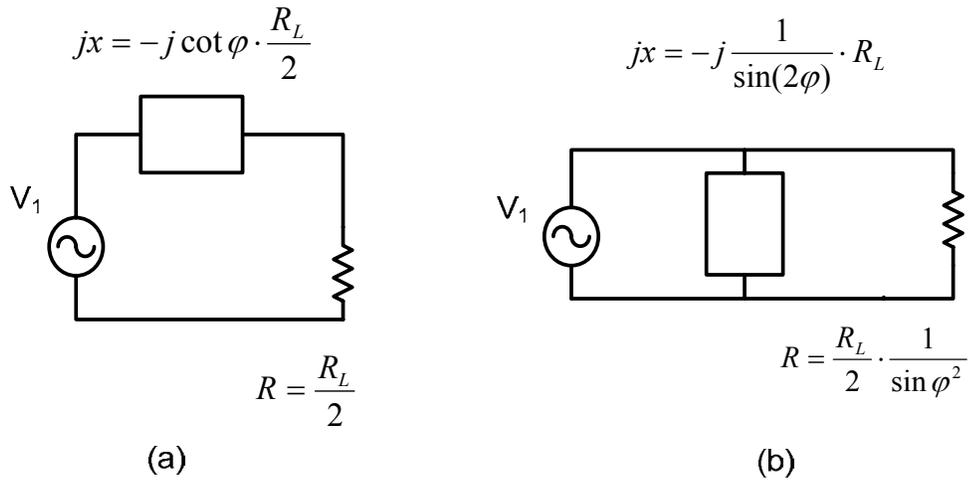


Figure 4.21: (a) RF load seen by the RF generator  $V_1$ ; (b) A parallel equivalent model

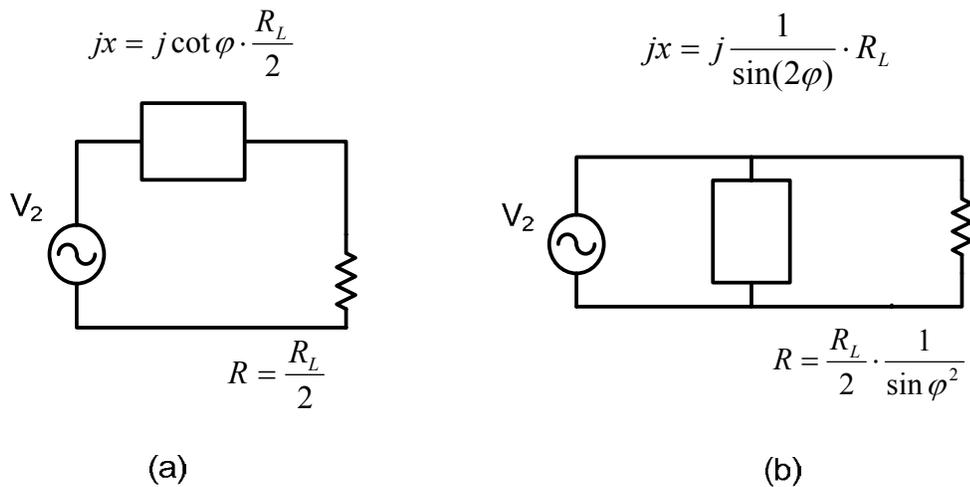


Figure 4.22: (a) RF load seen by the RF generator  $V_2$ ; (b) A parallel equivalent model

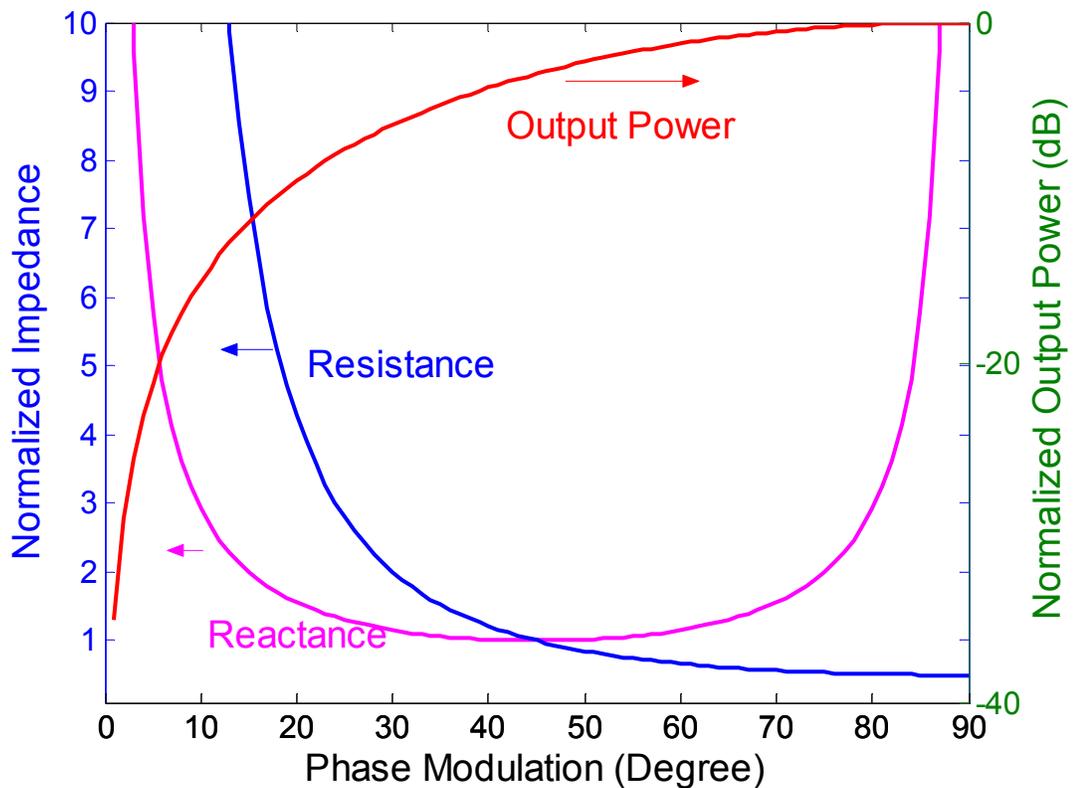


Figure 4.23: Resistance, reactance of the parallel equivalent circuit model, and total output power with phase modulation. (Note:  $R_L$  and  $V$  are normalized with the value of 1).

#### 4.4 Summary

The role of power combining in RF PA design is still not well appreciated by designers. They often opt for bigger, more exotic, high-voltage, or in other words, more expensive devices, although it is often not an optimal choice. Whether to use a number of smaller PAs versus a single bigger PA is one of the most important decisions in selection of architecture. Even when it is possible to design a single bigger PA, using a number of smaller PAs offers several advantages, such as better phase linearity, lower

chip temperature, and less heat removal requirements. When the required output power cannot be achieved by a single transistor, power combining is necessary to generate the required power from several units.

## 4.5 References

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## **Chapter 5. The Power Combining Transformer Design**

- 5.1 Impedance transformation
- 5.2 Design considerations of transformers for power amplifiers
- 5.3 Design and Implementation of the proposed transformer
- 5.4 Discussions and Summary
- 5.5 References

The power combining transformer proposed in this work is absolutely important in order to achieve highly efficient power amplifiers. In this chapter, LC resonant matching networks are compared to transformer matching, which explains why transformer matching is desired when impedance transformation ratio is high. Practical issues in designing low impedance inductors and highly efficient transformers will be considered next. The various topologies of on-chip transformer are studied. Based on those considerations, the topology of the proposed power combining transformer is introduced. At last, some design guidelines will be given.

### **5.1 Impedance Transformation**

The importance of impedance transformation needs no more introduction. In the context of power amplifier design, it is necessary to transform the load of a power amplifier to a value which is a function of the supply voltage and the required power<sup>39</sup>. Because lossless reactive components do not exist, all impedance matching networks will

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<sup>39</sup> It is well known that maximum power is transferred under conjugate matched condition. Besides it may not be realizable, the efficiency under this case is only 50%. Therefore, in power amplifiers design, the output is rarely conjugate matched.

have some insertion loss. These losses can be quite pronounced in PA circuits which degrade the efficiency directly. This issue is even serious when designing PA with state-of-the-art CMOS technologies, because of required high impedance transformation ratio and lossy on-chip passive components<sup>40</sup>. Three networks are often used in practice for impedance transformation: LC resonant matching networks and transformer matching networks, both lumped networks, and distributive networks with transmission lines. The analyses on those networks have been well documented. Interested readers should refer to the literature [5.1-5.3] to probe further. LC resonant matching networks and transformer matching networks are briefly discussed in this section. Similar analyses can be found in [5.4].

### 5.1.1 LC Resonant Matching Network

LC resonant matching is straightforward to implement. A single stage “L-match” is shown in Figure 5.1, composed of a capacitor and an inductor<sup>41</sup>. A lossy inductor can be analyzed with series equivalent circuits or parallel equivalent circuits by adding a resistor to model the loss (Figure 5.2), where

$$Q_L = \frac{\omega L_s}{R_s} = \frac{R_p}{\omega L_p}$$

$$R_p = R_s(Q_L^2 + 1)$$

$$L_p = L_s \left( \frac{Q_L^2 + 1}{Q_L^2} \right)$$

---

<sup>40</sup> Since on-chip capacitors Q is usually higher than inductors, only inductor loss is considered here for simplicity. This is especially true for low GHz range, which is the focus of this work.

<sup>41</sup> Both topologies can transform the load impedance to a lower value. With series capacitor approach, it will block DC current flowing into the load. With parallel capacitor approach, it will short high order harmonics automatically due to its low pass nature.

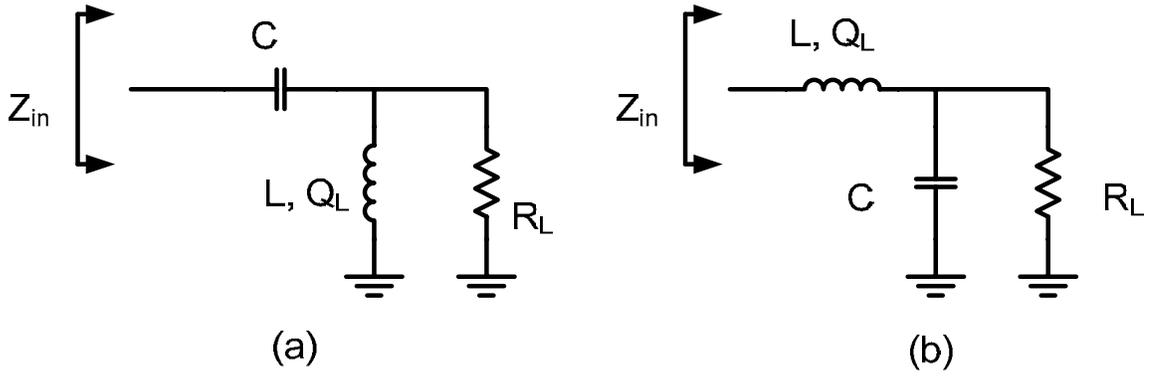


Figure 5.1: (a) A single stage “L-match” with a series capacitor and a parallel inductor; (b) A single stage “L-match” with a parallel capacitor and a series inductor

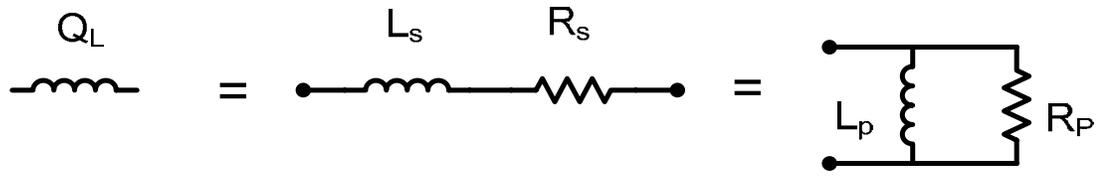


Figure 5.2: Equivalent models of an inductor with quality factor  $Q_L$

The “L-match” network shown in Figure 5.1(a) can be redrawn as in Figure 5.3:

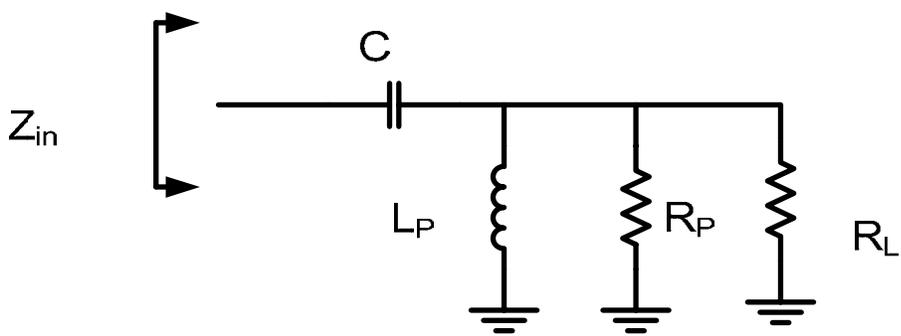


Figure 5.3: A single stage “L-match” resonant matching network with the inductor loss

Assuming at the frequency of interest,  $L_p$  and  $C$  resonate out, it could be shown that:

$$Q_{network} = \frac{R_p // R_L}{\omega L_p} = \frac{R_L}{\omega L_p + \frac{R_L}{Q_L}}$$

$$Z_{in} = \text{Re}(Z_{in}) = \frac{R_p // R_L}{1 + Q_{network}^2} = \frac{1}{1 + Q_{network}^2} \cdot \frac{R_L}{1 + \frac{R_L}{\omega L_p Q_L}}$$

The impedance transformation ratio (ITR) is:

$$ITR = \frac{R_L}{Z_{in}} = \frac{R_L}{R_p // R_L} (1 + Q_{network}^2) = \left(1 + \frac{R_L}{\omega L_p Q_L}\right) \cdot (1 + Q_{network}^2)$$

As the ITR increases, the  $Q_{network}$  also increases. The required inductance could be derived after the ITR, load  $R_L$  and the quality factor of an inductor  $Q_L$  are known:

$$\omega L_p = \frac{2(Q_L + 1/Q_L)}{ITR - 2 + \sqrt{ITR^2 + 4Q_L^2(ITR - 1)}} \cdot R_L$$

The power efficiency, or insertion loss, of the matching network can be calculated as the ratio between the power delivered to the load and the power delivered into the network:

$$\eta = \frac{P_L}{P_L + P_{diss}} = \frac{R_L // R_p}{R_L} \approx \frac{1}{1 + \frac{Q_{network}}{Q_L}}$$

or

$$\eta = \frac{Q_L^2 + 1}{Q_L^2 + \frac{ITR + \sqrt{ITR^2 + 4Q_L^2(ITR - 1)}}{2}}$$

As shown in Figure 5.4, the power efficiency drops quickly as ITR increases. In the resonant network,  $Q_{network}$  times higher energy circulates in the LC tank than the energy delivered to the load. As ITR increases,  $Q_{network}$  increases also such that more energy has

to be dissipated in the lossy tank in order to deliver the same power to the load. When ITR is between 40~50 which is required for PAs implemented in state-of-the-art CMOS technologies, the efficiency of passive network alone is below 55%<sup>42</sup> and the  $Q_{\text{network}}$  is around 6~7. Multi-stage LC resonant matching network can mitigate the loss, nonetheless it is usually limited to two stages<sup>43</sup>. Furthermore a multi-stage network has marginally better efficiency and bandwidth.

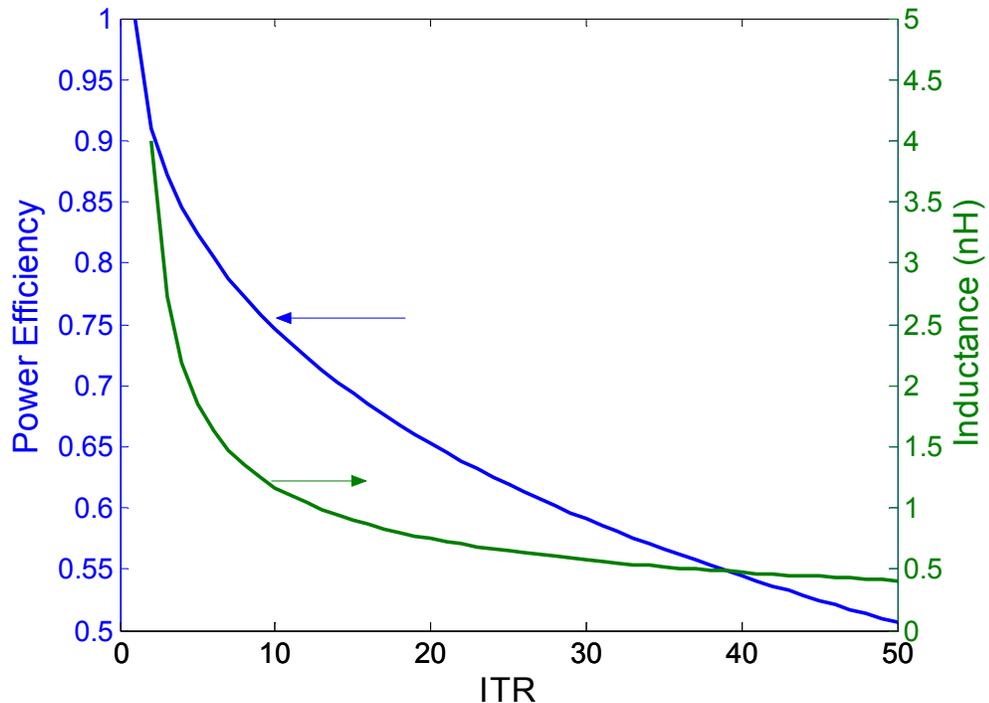


Figure 5.4: Power efficiency and required inductance of a single stage “L-match” network at 2-GHz with inductor  $Q_L = 10$ .

<sup>42</sup> Typical efficiency achieved with GaAs technologies is around 80~90%.

<sup>43</sup> Multi-stage network will occupy more area. And if ITR is small for a section, the required reactance is hard to be realized on-chip.

### 5.1.2 Transformer Matching Network

The flux coupled transformers are often used for impedance matching. On-chip transformers are implemented as coupled inductors. Therefore, non-idealities such as leakage flux, feed-through capacitance, and various losses cause real transformers (Figure 5.5) to deviate from ideal behaviors.

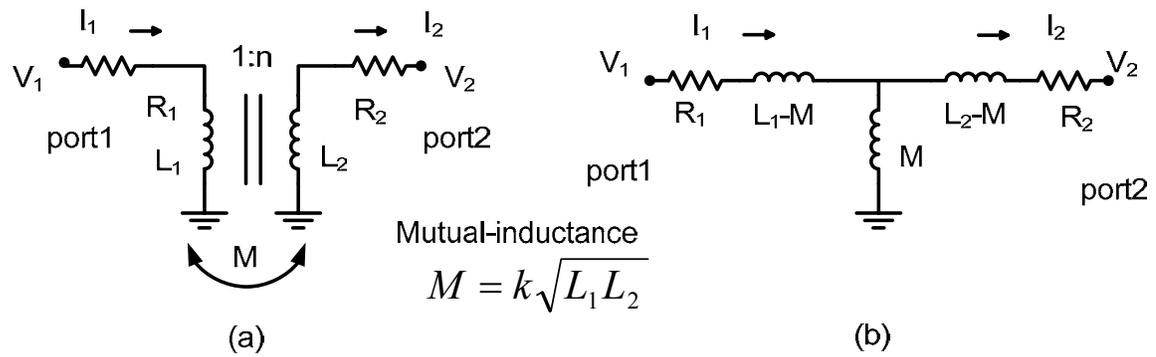


Figure 5.5: (a) Transformer model; (b) Transformer equivalent T-model

The losses of the primary and the secondary inductors are usually modeled with the resistors,  $R_1$  and  $R_2$ , as shown in Figure 5.5, where

$$R_1 = \frac{\omega L_1}{Q_1} \quad R_2 = \frac{\omega L_2}{Q_2}$$

Other than its isolation characteristics, the T-model is completely equivalent to the physical transformer model. The Z-parameter two-port equations for the transformer model are:

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} R_1 + j\omega L_1 & -j\omega M \\ j\omega M & -R_2 - j\omega L_2 \end{bmatrix} \cdot \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}^{44}$$

<sup>44</sup> Note that the flow direction of  $I_2$ .

The T-model can be modified so it is expressed in terms of leakage inductance and magnetizing inductance, which circuit designers are more familiar with than self-inductance and mutual-inductance (Figure 5.6). The magnetizing and leakage inductance are:

$$\begin{aligned} L_{m1} &= kL_1 & L_{L1} &= (1-k)L_1 \\ L_{m2} &= kL_2 & L_{L2} &= (1-k)L_2 \end{aligned}$$

Now, let's define the effective turn ratio,

$$\alpha = \sqrt{\frac{L_{m2}}{L_{m1}}} = \sqrt{\frac{L_{L2}}{L_{L1}}} = \sqrt{\frac{L_2}{L_1}} = k \cdot n$$

so the mutual inductance can be expressed as:

$$M = k\sqrt{L_1 L_2} = \sqrt{L_{m1} L_{m2}} = \alpha L_{m1} = \frac{1}{\alpha} L_{m2}$$

The Z-parameter two port equations become:

$$V_1 = (R_1 + j\omega L_{L1})I_1 + j\omega L_{m1}(I_1 - \alpha I_2)$$

$$V_2 = j\omega L_{m1}(I_1 - \alpha I_2)\alpha - (R_2 + j\omega L_{L2})I_2$$

Given a load connected to port 2 (Figure 5.7), the power efficiency of the transformer is:

$$\eta = \frac{R_{eq}}{(R_{eq} + R_2 / \alpha^2) + R_1 \frac{(R_2 / \alpha^2 + R_{eq})^2 + (k\omega L_1 + \omega(1-k)L_2 / \alpha^2 - 1/(\omega C_{eq}))^2}{(k\omega L_1)^2}}$$

where

$$C_{eq} = \frac{\alpha^2 [1 + (\omega R_L C_2)^2]}{\omega^2 R_L^2 C_2}$$

$$R_{eq} = \frac{R_L / \alpha^2}{1 + (\omega R_L C_2)^2}$$

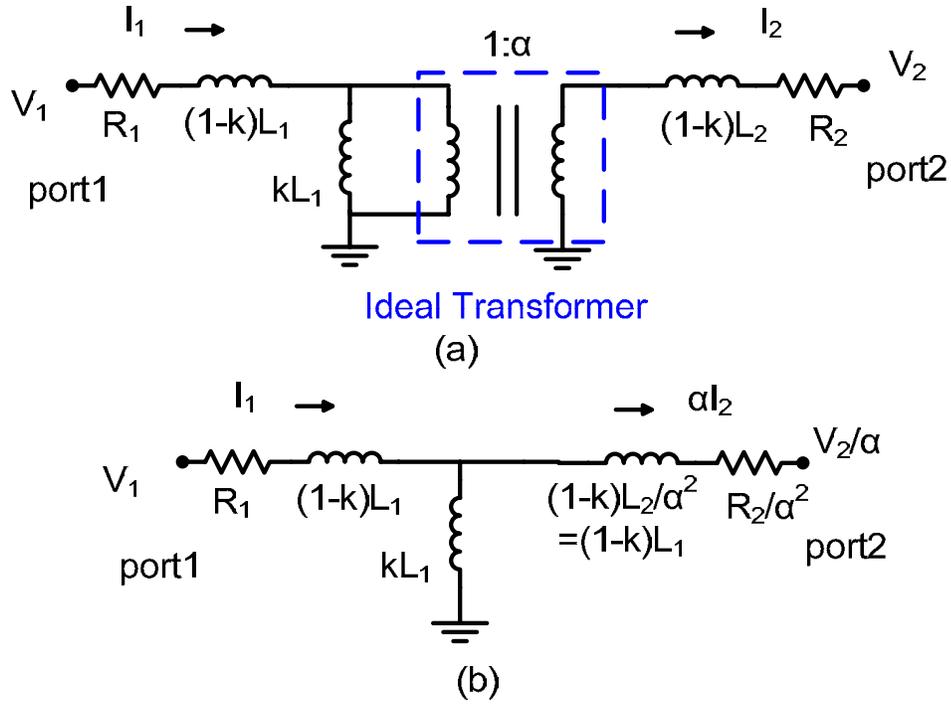


Figure 5.6: (a) Transformer model with leakage and magnetizing inductance; (b) Equivalent T-model

Apparently, to maximize the power efficiency, the inductance at the secondary should be tuned out by the capacitor at the secondary:

$$\frac{1}{\omega C_{eq}} = \omega L_2 / \alpha^2$$

And power efficiency becomes:

$$\eta = \frac{R_{eq}}{R_{eq} + \frac{\omega L_1}{Q_2} + \frac{\omega L_1}{Q_1} \left( \frac{1}{kQ_2} + \frac{R_{eq}}{k\omega L_1} \right)^2}$$

Taking the derivative with respect to  $\omega L_1$ , maximum efficiency is obtained<sup>45</sup>:

<sup>45</sup> In measurements, since the insertion loss of a transformer highly depends on the source and load impedance, it's convenient to find the minimum insertion loss at the frequency of interest under ideal

$$\eta_{\max} = \frac{1}{1 + \frac{2}{Q_1 Q_2 k^2} + 2 \sqrt{\frac{1}{Q_1 Q_2 k^2} \left(1 + \frac{1}{Q_1 Q_2 k^2}\right)}}$$

when

$$\omega L_1 = \frac{A}{1 + A^2} \cdot \frac{R_{load}}{\alpha^2} \quad \left( A = \frac{1}{\sqrt{\frac{1}{Q_2^2} + \frac{Q_1}{Q_2} k^2}} \right)$$

To complete the design,  $C_2$  need to be sized accordingly:

$$\frac{1}{\omega C_2} = \frac{R_L}{A}$$

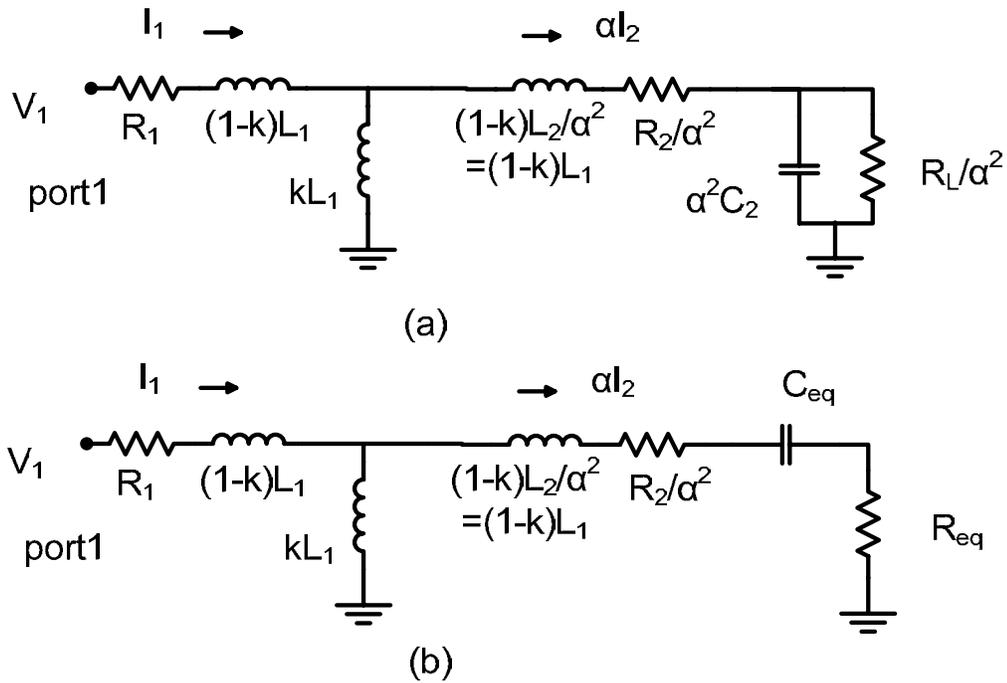


Figure 5.7: (a) Transformer equivalent T-model with a load resistor and tuning capacitor<sup>46</sup>; (b) Transformer T-model after parallel to series conversion at the load

conditions, a bi-conjugate source and load match, using s-parameters to get  $G_{\max}$ . Alternatively,  $G_P$  can be calculated based on S-parameters to derive insertion loss.

<sup>46</sup> The tuning capacitor could be placed in series with the load. However, in PA design, parallel placement is preferred since it will transform the load to a lower value.

Unlike LC resonant matching networks, the power efficiency of a transformer matching network does not depend on ITR. This is an inherent property of transformers, because the product of  $V \cdot I$  is constant on both sides of the transformer regardless of what ITR is. Figure 5.8 shows the power efficiency plot of a transformer. Note that there are two variables that determine the power efficiency. This should be kept in mind during transformer design, although some designs only paid attention to the quality factor of the coupled inductors or the coupling factor alone. It is also observed that after  $Q$  is higher than 15, the improvement in efficiency is marginal assuming the coupling factor is good.

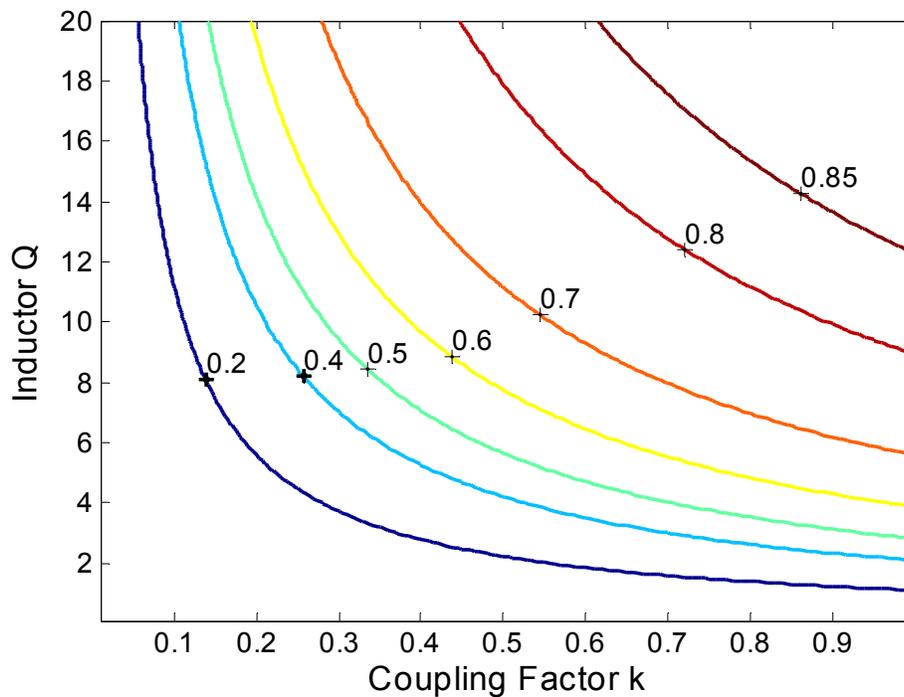


Figure 5.8: Power efficiency contour plot of a 1:n transformer, assuming  $Q_1 = Q_2$

It seems that the impedance matching problem is solved. When high ITR is needed, high turn ratio transformers could be used without sacrificing power efficiency.

However, in implementation, there are always non-idealities that inevitably degrade the power efficiency of high turn ratio transformers. This will be investigated in section 5.2.

Under the optimum power efficiency condition, the network Q is derived as:

$$Q_{network} = \frac{Q_1(1 + \frac{A}{Q_2})}{k^2 A Q_1 + (1 + \frac{A}{Q_2})}$$

which is only a function of inductor quality factors and coupling factor, the same as the power efficiency. When the inductor quality factor is not too low,  $Q_{network}$  is inversely proportion to k to the first order. As long as coupling is not too low ( $>0.6$ ), the bandwidth of a transformer is pretty wide ( $Q_{network} \approx 1.6$ ), which is certainly an advantage for designing the next generation wireless systems (Figure 5.9).

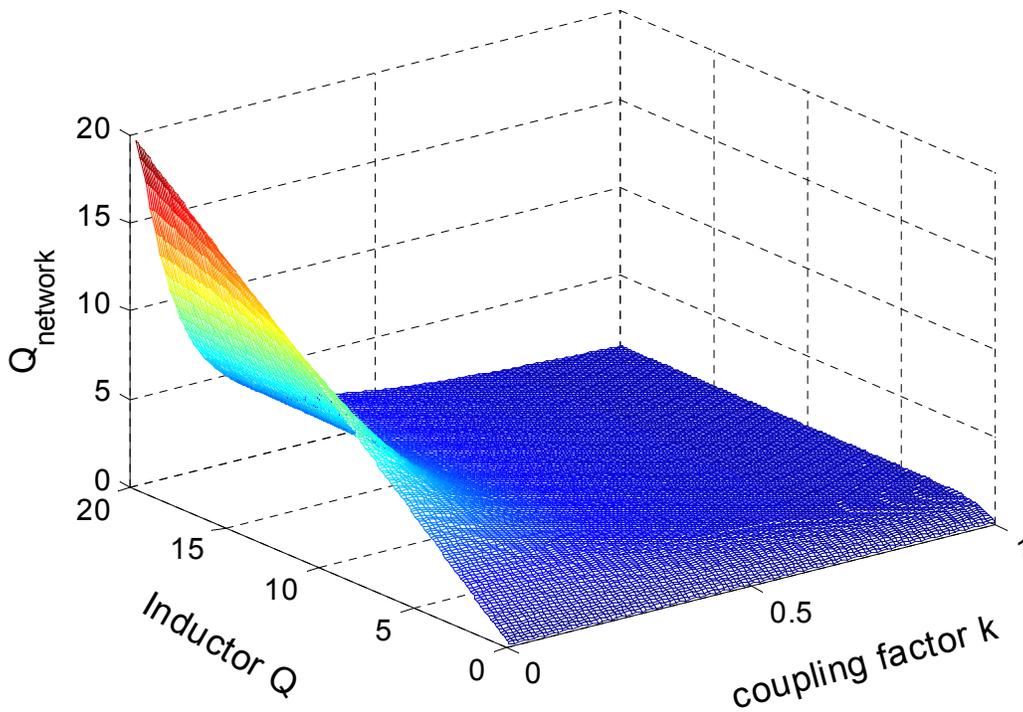


Figure 5.9:  $Q_{network}$  of a 1:n transformer vs. coupling factor and  $Q_{ind}$ , assuming  $Q_1 = Q_2$

## 5.2 Design Considerations of Transformers for Power Amplifiers

Although transformers are attractive when high ITR is required, some practical issues need to be addressed. Figure 5.10 illustrates the desired primary inductance for optimum power efficiency with 50- $\Omega$  load as ITR varies. When ITR is equal to 36, corresponding to turn ratio of 6, the primary side inductance should be around 52-pH in order to achieve the optimum power efficiency.

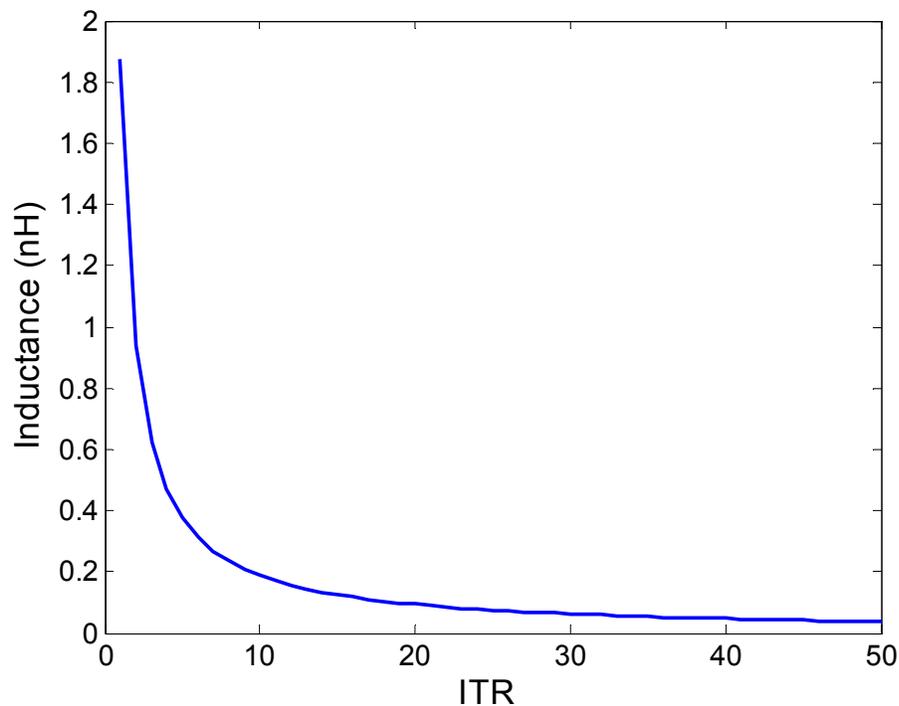


Figure 5.10: The required primary inductance for maximum efficiency vs. ITR (when  $\omega = 2$ -GHz,  $Q_1 = Q_2 = 10$ ,  $k = 0.7$ ,  $R_L = 50$ - $\Omega$ )

There are two issues with this approach. The first issue is how to implement low impedance inductor for the primary of the transformer. The fact is that it is not practical at all to implement, considering even a few hundreds of micron metal interconnects might

have the same inductance. The secondary issue has to do with the high turn ratio. For on-chip transformers, high turn ratio is realized by putting higher number of turns for the secondary (Figure 5.11). However, the power efficiency of this structure deteriorates because of increased loss and reduced coupling factor. A slightly better approach is to keep the turns of the primary and the secondary equal and connect the primary turns in shunt using underpass (Figure 5.12) [5.5]. This approach enhances the magnetic coupling between the primary and the secondary. Nonetheless, the insertion loss is still high for power amplifiers.

Clearly, high turn ratio transformers in practice suffer from high insertion loss, the same situation as high ITR LC resonant matching network. On the other hand, low turn ratio transformers are more practical and have the potential to achieve high power efficiency. Together with power combining topology, high impedance transformation with high power efficiency, therefore, becomes possible.

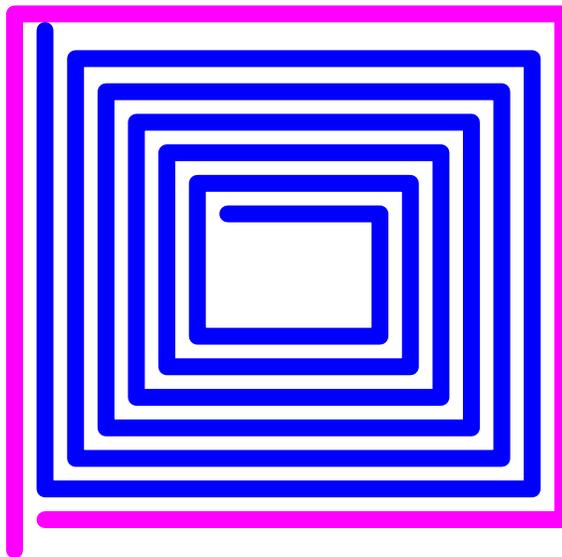


Figure 5.11: An on-chip transformer with high turn ratio formed by coupled inductors

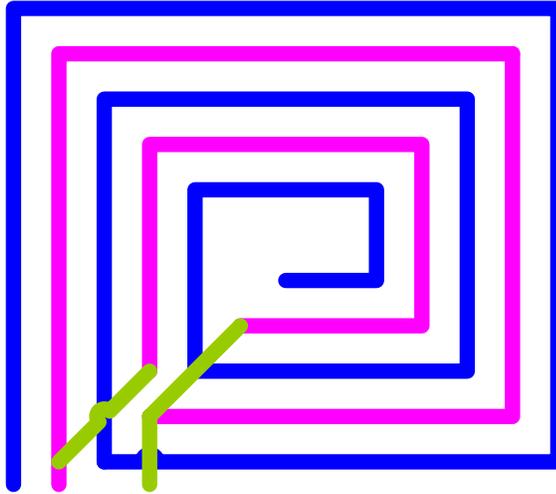


Figure 5.12: An on-chip high turn ratio transformer with shunted primary

### 5.2.1 Low Impedance Inductor Design

It is clear that low turn ratio transformer is preferred for high power efficiency. Yet it still remains unanswered how to implement low impedance inductors which compose such a transformer. Although the quality factor and inductance of coupled inductors will be different from those of a standalone inductor, the difference is not dramatic. Therefore it is still revealing to look at the design of inductors first. Three basic types of inductors can be chosen to design coupled inductor transformers, multi-turn inductors, micro-strip line inductors, and single-turn inductors.

For a multi-turn spiral inductor<sup>47</sup>, as number of turns increases, the spacing between opposite sides shrinks, causing a drop of inductance because of increasing negative magnetic coupling. Moreover similar currents flow in the conductors on the same side, the current within conductors will be constrained to smaller regions, resulting

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<sup>47</sup> The main point of using multi-turn spiral inductor is to conserve chip area

current crowding known as proximity effect. The combination of the two mechanisms significantly reduces the quality factor of an inductor, therefore reduce power efficiency of a transformer formed by multi-turn inductors.

To avoid negative magnetic coupling from opposite sides and the proximity effect, inductors can be built with a one-port short-circuited transmission line, often referred as micro-strip line inductor (Figure 5.13). The input impedance seen is:

$$Z_{in} = jZ_o \tanh(\gamma \cdot l)$$

where  $\gamma$  is the complex propagation constant and  $Z_o$  is the characteristic impedance. Because there is no negative magnetic coupling from the opposite side of the spiral, the total metal length will be shorter than a spiral inductor to obtain the same inductance. Therefore, it effectively reduces the series resistive loss of the metal. And the metal strip could be laid out with wider width comparing to a spiral inductor, because of less layout constraints. Although this approach demonstrates its potential to implement high-Q inductors, especially for high Q, low impedance inductors, it does have a serious drawback. Because two ports of such an inductor are not in close vicinity, it creates difficulties during implementations. A solution to this problem was demonstrated in [5.6], with a proposed double-differential architecture.

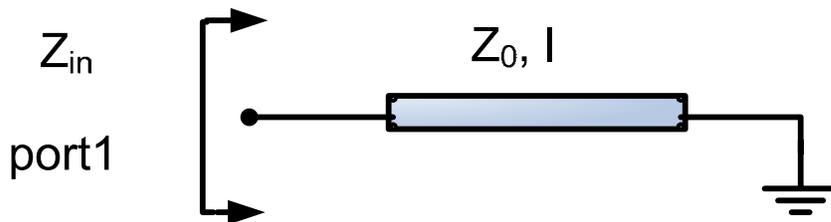


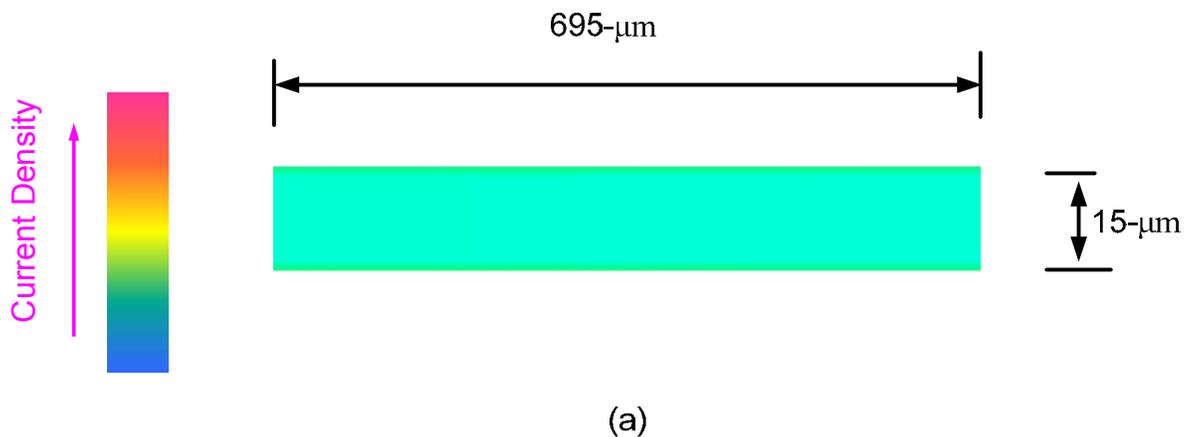
Figure 5.13: A transmission line with one port short-circuited to ground

A compromise between a multi-turn inductor and a micro-strip line inductor is a single-turn inductor, sometime referred as “hairpin” inductor. In a single-turn inductor, if the distance between opposite sides is large, negative magnetic coupling is negligible. The inductance is primarily limited by back plane mirror current. Moreover, the proximity effect in a single-turn inductor has little impact while the skin effect dominates the high frequency loss. Hence, it behaves very much like a micro-strip line inductor of the same total length. Unlike a micro-strip line inductor, the two ports are close by rather than far away from each other, so that it is relatively straightforward to lay it out.

Figure 5.14 shows the three inductors implemented in the same technology but with different style, micro-strip line, single-turn and multi-turn respectively. The metal width of three inductors is kept same. The dimensions of the inductors are designed to make them have roughly equal inductance. The inductance of three inductors are about the same ( $0.6\text{-nH} \pm 1\%$ ), simulated at 2-GHz with Momentum in Agilent ADS. The quality factors of three inductors are 17, 11 and 7.9 respectively. We see that the micro-strip line inductor has used the cross section area most efficiently, with current evenly distributed, while in the multi-turn inductor, the current crowding is quite obvious, especially in the inner turns where the magnetic field is large. However, the single-turn inductor did not have expected performance. Its quality factor is lower than the micro-strip line inductor. Depending on the distance between opposite sides, losses caused by proximity effect and negative mutual coupling still have some impact on a single-turn inductor and degrade its performance. Besides, two additional mechanisms degrade the quality factor. First, the two ports of a single turn inductor are physically close to each other, therefore part of the signal will leak through substrate and induce extra loss,

especially at high frequency. For micro-strip line inductors, two ports are away from each other, the path through substrate is, therefore, a high impedance path. Very little signal will take this path which effectively eliminates this loss. It should be noted this loss could be significantly reduced in a single-turn or multi-turn inductor using a patterned metal shield as ground plane. The other is due to the geometry of the single-turn inductor. Circular geometry can improve the quality factor by 10~20% comparing to octagonal geometry [5.7]. After changing the geometry to circular shape, the Q of the single-turn inductor increased from 11 to 12 (Figure 5.15).

As mentioned before, micro-strip line inductors have superior quality factor, nonetheless they impose much more constraints in implementation and will occupy more area. In single-turn or multi-turn spiral inductors, current crowding degrades Q factors, however, they usually occupy much less area comparing to micro-strip line inductors and are easy to be laid out. Single-turn inductors are particularly of interest for low impedance inductors. Quality factors of single-turn inductors or multi-turn inductors can be further improved using interleave structure and/or other measures.



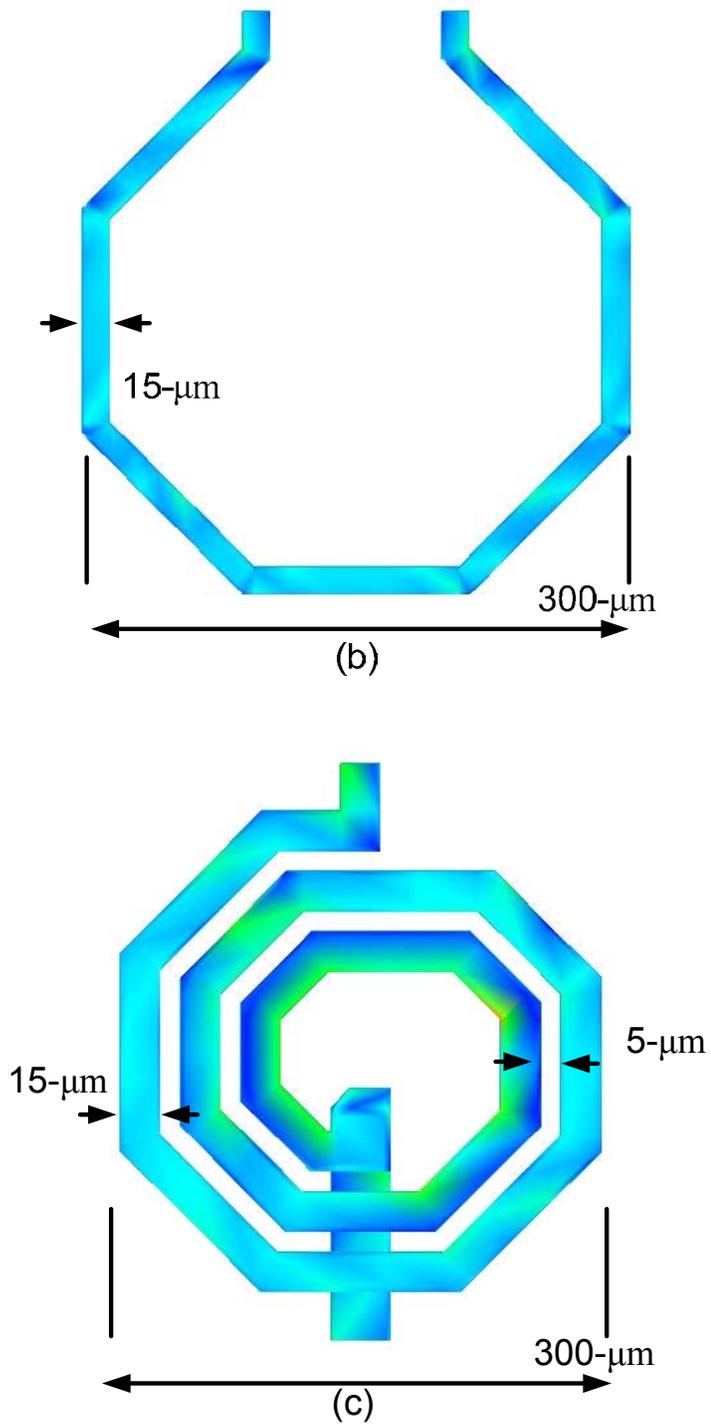


Figure 5.14: Current densities of three inductors implemented in the same technology with equal width: (a) Top view of the micro-strip line inductor; (b) Top view of the single-turn inductor; (c) Top view of the multi-turn inductor

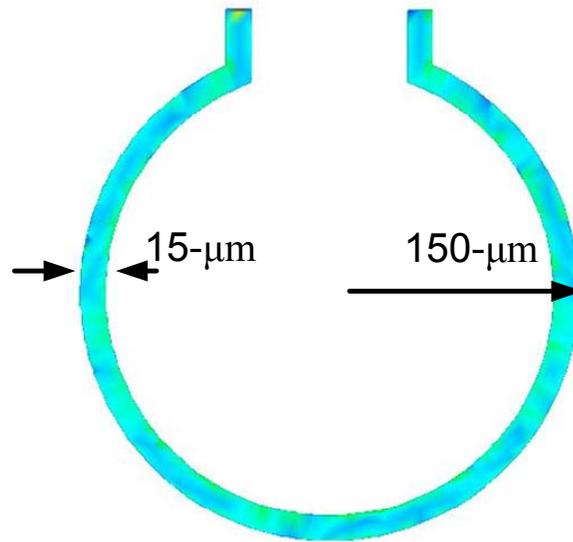


Figure 5.15: Current density of a circular single-turn inductor (top view)

### 5.2.2 Low Turn Ratio Transformer Design

A desired transformer in a power combining amplifier should have the following properties: high Q inductors forming the primary and secondary, high magnetic coupling, and very little capacitive coupling. The importance of the first two properties has been emphasized. The impact of capacitive coupling is studied here.

The impacts of  $C_c$  on the performance of a power combining transformer are in two aspects. First, it limits the operation frequency of a transformer. At a certain frequency,  $C_c$  resonates with coupled inductors. The transformer degenerates into another structure and cannot be called a transformer anymore. The second impact is more subtle. For the power combining amplifier enabled by the power combining transformer, the ac voltages add up at the secondary. Therefore, capacitive coupling of

different amplifiers through  $C_c$  will not be the same due to the different voltage swing at the secondary (Figure 5.16). Parallel driven primaries now work in different environment in terms of voltage stress, and some will break down earlier than others<sup>48</sup>.

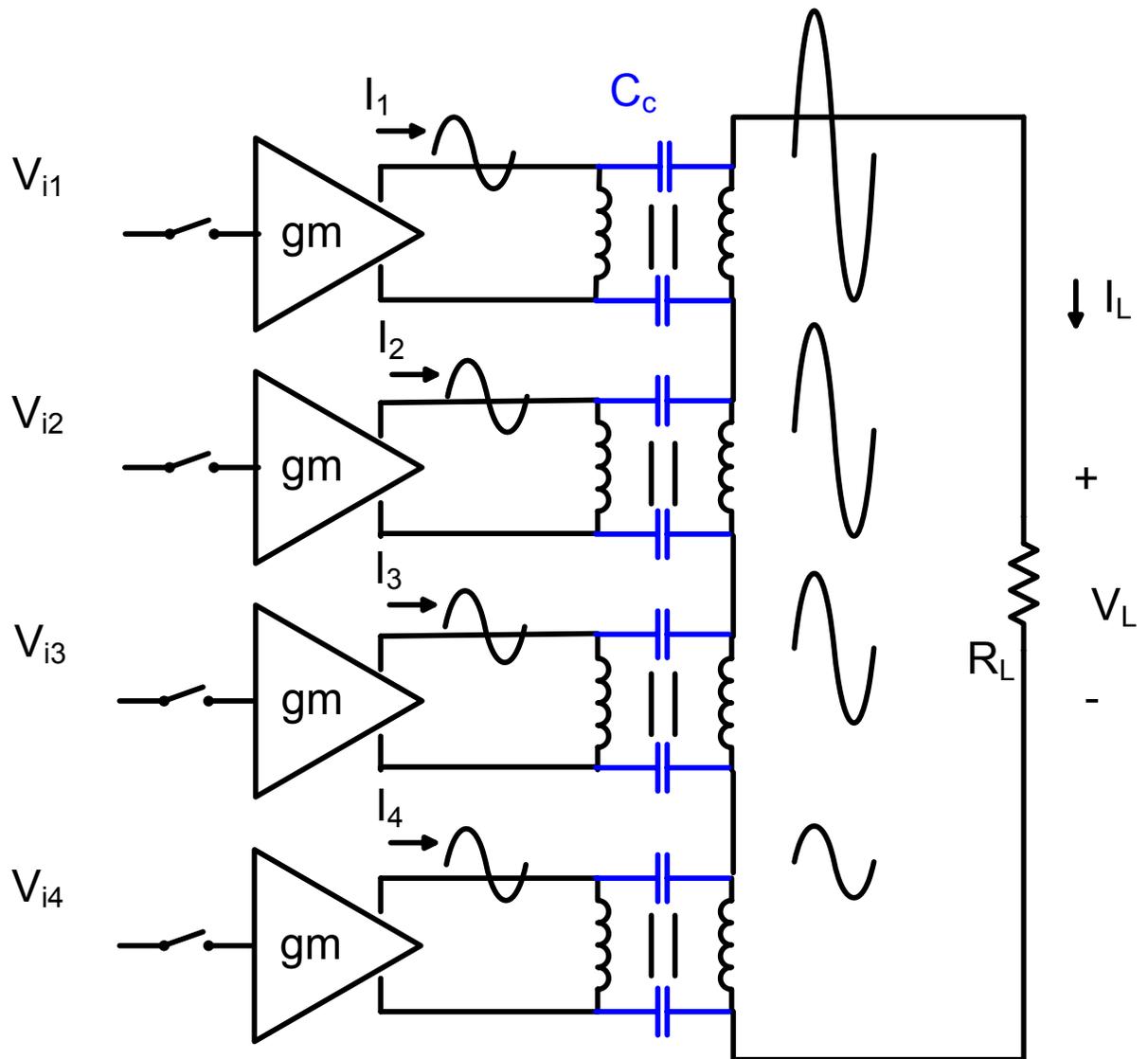


Figure 5.16: Capacitive coupling of the power combining transformer will cause some amplifiers break down earlier than others.

<sup>48</sup> Some techniques can reduce or eliminate this impact, which will be discussed later.

It is interesting to look at quality factors of inductors in a coupled inductor transformer composed of micro-strip line inductors and single-turn inductors respectively. The quality factor of an inductor will definitely change due to current redistribution. Many layout styles have been used to build transformers. Each layout style has its advantages and disadvantages. The choice of layout style is tightly correlated with the technology features which the transformer is to be implemented with. For now, an overlay structure is adopted for comparison, where primary and secondary are implemented with the top two “analog” metal layers. The dimensions of coupled inductors are kept the same as individual inductors studied in section 5.2.1. Table 5.1 summarizes the simulated results.

Inductor style	Inductance of a stand alone inductor (nH)	Q of a stand alone inductor	Inductance of such an inductor in a transformer (nH)	Q of such an inductor in a transformer
Micro-strip line	0.608	17	0.605	15
Single-turn (round)	0.593	12	0.583	11.2
Single-turn (octagonal)	0.604	11	0.604	9.6

Table 5.1: Q of a stand alone inductor and of such an inductor in a transformer

### 5.3 Design and Implementation of the Proposed Transformer

The power amplifier implemented in this work requires an eight-way power combining amplifier, to transmit 24-dBm linear power with 1.2-V supply voltage. Since pseudo-differential topology is adopted to implement the amplifiers, four pseudo-differential amplifiers and four 1:1 transformers are needed to construct an eight-way power combining amplifier. Assuming that the achievable quality factors of both primary and secondary inductors are 12.5 and coupling factor is 0.7, the optimal inductance is around 460-pH at 2-GHz. The power efficiency of the transformer is 0.796 (IL= 0.99-dB) with proper tuning. Although the inductance cannot be predicted precisely due to process variation, the power efficiency is relatively insensitive to the inductance, a benefit from wide-band characteristic of transformers (Figure 5.17).

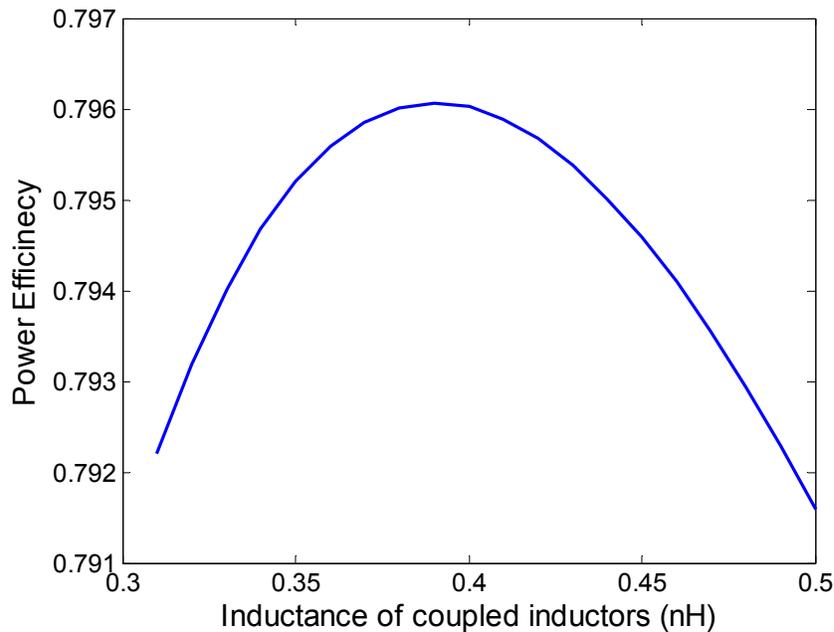


Figure 5.17: The variation of power efficiency vs. inductance of coupled inductors in the designed transformer

Because the chosen process offers two thick top metal layers, overlay structure is used to implement the power combining transformer. This structure can provide good magnetic coupling without excessive capacitive coupling. The primaries are implemented with lower level top metal and the secondary is implemented with the upper top metal. In this way, primaries act as good electric shield to prevent the displacement current flowing from the high voltage swing secondary to the substrate as well as electrical coupling to the other part of the circuits. Patterned ground shield with M1 provides further isolation. Inductors are implemented with single-turn style for both primaries and the secondary. Ideally, a circular shape would be favored to obtain high quality factor, however, it is prohibited by the design rules of the process.

A simple transformer layout is shown in Figure 5.18. In this approach, the adjacent windings have current flowing in opposite direction, and thus do not contribute as much flux and coupling to the secondary. Hence, power efficiency will be hurt. Moreover, since primaries will have different magnetic coupling to the secondary, a different load will be seen at each primary which causes severely degraded performance.

Several measures can be taken to minimize coupling of the adjacent windings. One of them is to leverage the fact that orthogonal lines have negligible magnetic coupling as shown in Figure 5.19. This approach still has one flaw, which is the degradation of quality factors from those 90° corners. A compromise is made as shown in Figure 5.20. Now the primary inductors look like an oval. And windings are kept apart with some distance to minimize internal flux cancellation.

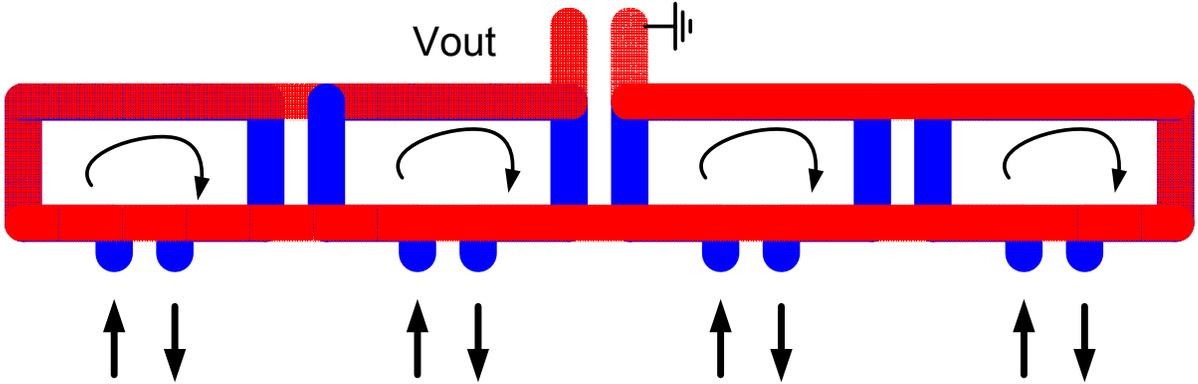


Figure 5.18: A simple power combining transformer. Some parts of primaries are not overlapped with the secondary which reduces coupling factor. Opposite currents flow in those parts of adjacent primaries. It reduces inductance and degrades Q.

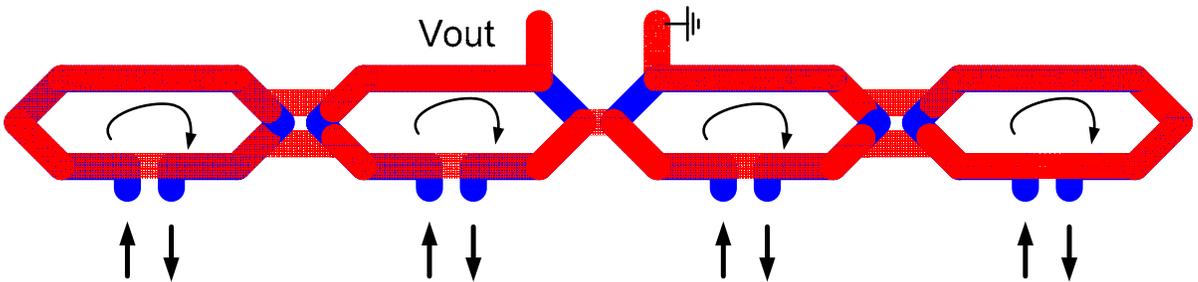


Figure 5.19: A power combining transformer with reduced magnetic coupling between adjacent windings.

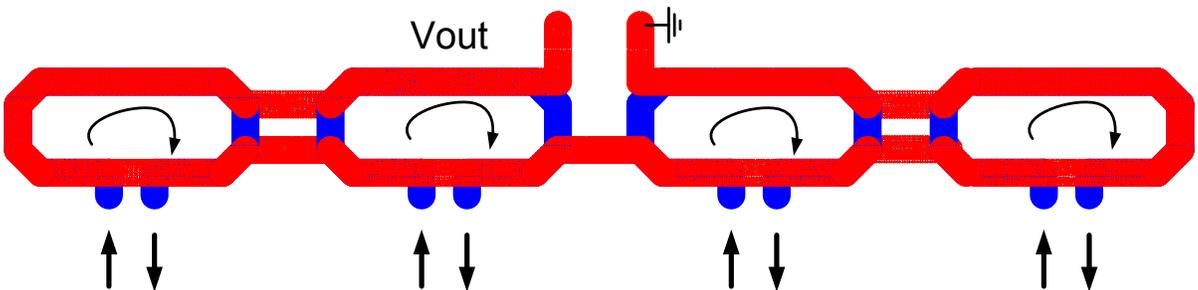


Figure 5.20: A power combining transformer with oval-like high-Q inductors

The structure in Figure 5.20 was imported into Momentum, a 2.5D EM simulator. Top analog metals were modeled as thick conductors instead of sheet conductors to accurately model the inductance, Q and coupling factor. Extra leads necessary for connecting transistors with the transformer, bypass network, and M1 patterned ground are included in the simulation. The simulated s-parameter table was then imported into Cadence circuit simulator. With proper tuning at the secondary to resonate out the secondary inductance, the power efficiency is more than 79%. Figure 5.21 shows the variation of power efficiency with the capacitance of the tuning capacitor at the secondary. Figure 5.22 shows the change of power efficiency as a function frequency. The transformer maintains more than 70% efficiency from 1.45-GHz to 3.0-GHz. In other words, presuming the quality factors of the passives and the coupling factors are insensitive to process variation, the power efficiency of the transformer is very tolerant to components variation.

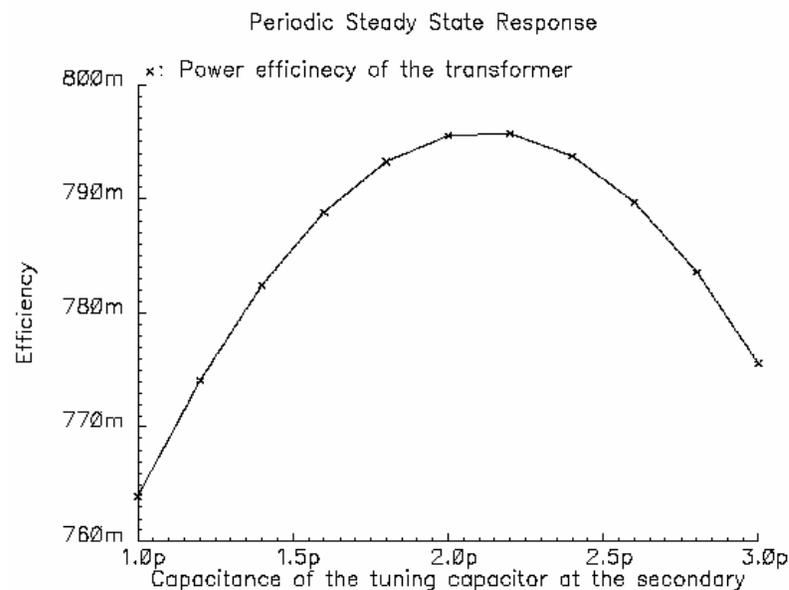


Figure 5.21: Power efficiency vs. the secondary tuning capacitance at 2-GHz

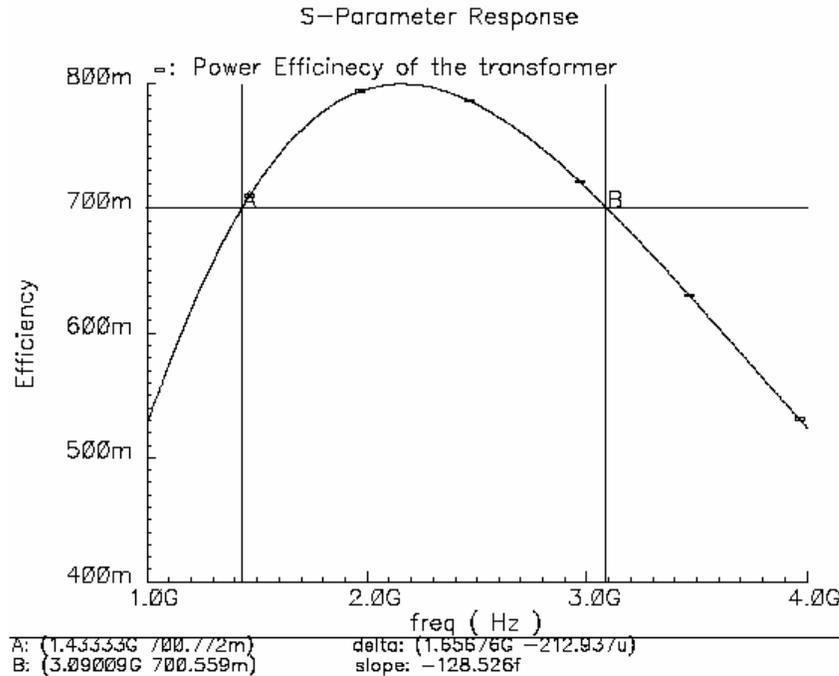


Figure 5.22: Power efficiency vs. frequency for a transformer designed at 2-GHz

The high efficiency achieved by this transformer undoubtedly benefited from double thick “analog” metals (~3- $\mu\text{m}$ ) available in the process. In a typical digital CMOS process, however, only one thick top metal is available. Obviously, a different style is needed.

## 5.4 Discussions and Summary

In a typical digital CMOS process, only one thick metal is provided. Therefore, lateral coupling structure has to be used which could potentially degrade power efficiency from two aspects. First, the magnetic coupling will not be as good as an overlay structure. Second, the inner conductor will suffer from current crowding which results from the

proximity effect, just like in a multi-turn inductor. Consequently, the resistance of the structure increases and Q decreases.

A new “figure 8” style layout which is compatible with “vanilla” CMOS processes (Figure 5.23) has been proposed to address those issues [5.8]. An interleaved structure is used for the primary windings, to reduce losses and enhance magnetic coupling. An important additional benefit comes from the alternating direction of the secondary winding. The secondary winding is immune to common mode disturbance from a distant source, because the incoming magnetic flux induces currents of opposite directions across each “figure 8” section. For this reason, an even number of sections is favored. The simulation of this structure shows an efficiency of 0.752 (IL = 1.35-dB) at 5-GHz, with only one thick top metal in a 90-nm digital CMOS process.

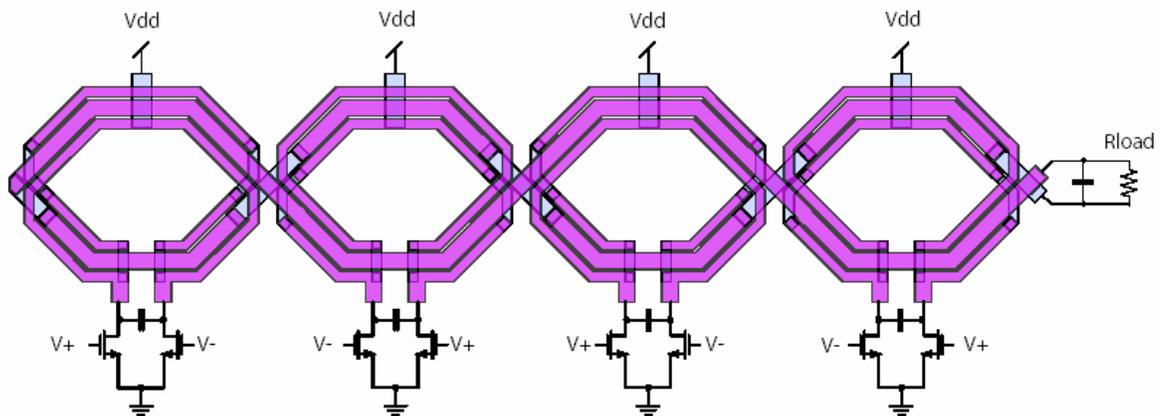


Figure 5.23: A power amplifier with “figure 8” transformer power combiner [5.8]

In Table 5.2, the performance of several power combining transformers are compared. Transformers composed of single-turn inductors demonstrate high power efficiency, comparable to transformers composed of micro-strip line inductors. The ease

of implementation, the compatibility with CMOS processes and the ability of accessing individual amplifiers to improve average efficiency make this type of transformers very appealing.

Process	Type	Freq (GHz)	Efficiency	Area (mm <sup>2</sup> )	Ref.
GaAs	micro- strip line	2	0.877	1.2*1.2	[5.9]
0.35- $\mu$ m BiCMOS	micro- strip line	2.4	0.7	0.8*0.8	[5.4]
0.20- $\mu$ m SiGe	micro- strip line	21-26	0.776	0.4*0.2	[5.10]
0.18- $\mu$ m RF CMOS	micro- strip line	2.4	0.83	0.8*0.5	[5.11]
0.13- $\mu$ m RF CMOS	single- turn	2.4	0.8	1.8*0.25	[5.8]
90-nm CMOS	single- turn	5.35	0.75	0.65*0.15	[5.12]

Table 5.2: Comparisons among state-of-the-art power combining networks

## 5.5 References

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# Chapter 6. A Fully Integrated CMOS Power Amplifier with Average Efficiency Enhancement

6.1 Design of the prototype

6.2 Layout considerations

6.3 The CMOS prototype

6.4 Experimental Results

6.5 Summary

6.6 References

A prototype was implemented in a 0.13- $\mu\text{m}$  CMOS process to prove the concept of the power control and efficiency enhancement technique proposed in this work. The prototype is based on a power combining transformer described in Section 4.3 centered around 2.4-GHz, with the ability to transmit 24-dBm at the  $P_{-1\text{dB}}$  compression point under 1.2-V supply. The average efficiency should be good as well as the instantaneous efficiency at the peak output power. In this chapter, the design process will be highlighted, with some discussion of practical issues. The design methodology took a top-down approach, with several iterations in some critical steps. This methodology proved to be very effective. Although the prototype was not designed for any particular standards, it was tested with both continuous wave (CW) signals and modulated signals.

## **6.1 Design of the Prototype**

### **6.1.1 Features of the CMOS Process**

A 0.13- $\mu\text{m}$  RF CMOS process was used to implement the prototype. This process offers two thick analog top metal layers for high-Q inductors, MIM capacitors, 1.2-V core transistors, 3.3-V I/O transistors and other devices. It should be noted that only thick top metals and MIM capacitors are Analog/RF options. All other features are also standard in a digital CMOS process. As discussed in Chapter 3, the use of I/O transistors has several drawbacks. Furthermore, I/O transistors will scale as well as process scaling continues. Based on those considerations, only thin-oxide core transistors were employed to implement the prototype. This implies a low supply voltage for the power amplifier.

### **6.1.2 PA Architecture**

At the beginning of the design, one of the most important decisions to make was to choose the class of operation for the power amplifier. The class-AB mode was chosen for good reasons. It is a classical compromise, offering higher efficiency than “linear” class-A mode, with some increased nonlinear effects which can be tolerated. No linearization scheme was employed around the amplifier. The purpose is to determine the intrinsic linearity of CMOS power amplifiers with deeply scaled devices.

A power amplifier can be divided into three major blocks, an input matching network, active devices and an output matching network. Input matching is certainly critical because it plays an important role in determining the power amplifier gain.

Hence it will affect the power added efficiency (PAE). Nonetheless, good drain efficiency usually implies good PAE in class-AB transconductance power amplifiers, because the gain of each stage is usually around 10~12-dB. Furthermore, it should be noted that the major challenge of fully integrated CMOS power amplifier designs lies in the integration of the output matching network. In the implemented prototype, the output matching network of the power amplifier was emphasized, while input matching was not implemented.

### 6.1.3 Power Combining

The targeted linear power of this work is 24-dBm at P<sub>-1dB</sub>. The supply voltage is predetermined to be 1.2-V, the same as the supply voltage for the baseband circuitry in the same technology. To determine how many individual amplifiers are needed for power combining for the peak output power, some assumptions have to be made at the design stage. Assuming that saturation voltage V<sub>dsat</sub> is 0.1-V and the efficiency of the overall amplifier is between 25% and 35%, the total output power of the N-way transformer power combining amplifier is:

$$P_{out} = \eta \cdot \frac{1}{2} \frac{(V_{DD} - V_{dsat})^2}{R_L / N} \cdot N$$

so N is derived as:

$$N = \sqrt{\frac{2 \cdot P_{out} \cdot R_L}{\eta \cdot (V_{DD} - V_{dsat})^2}}$$

Plugging in numbers,  $N$  is approximately 8 for 50- $\Omega$  load. Therefore, an 8-way transformer power combining amplifier is needed for the peak output power<sup>49</sup>.

#### 6.1.4 Pseudo-Differential Pair

The differential topology prevails in integrated circuits design for good reasons. It is ideally immune to common mode signals and interference, which is very crucial to integrated circuits design. However, in power amplifier designs, the true-differential pair is not appropriate because it limits the linearity performance under large input signal drive. An alternative is to use pseudo-differential pair as shown in Figure 6.1, where each device has its source grounded.

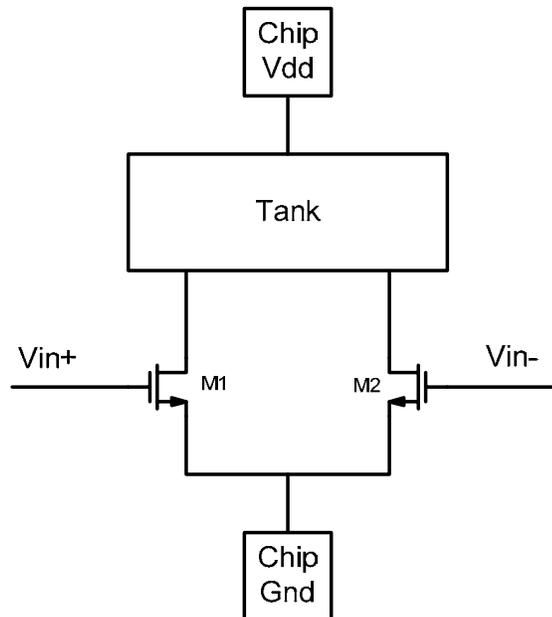


Figure 6.1: A pseudo-differential pair in power amplifier designs

<sup>49</sup> Here, the calculation was based on a class-A amplifier, which gives some margin.

Several key benefits of pseudo-differential pair are very important to integrated power amplifier designs. The fundamental frequency components of the two device currents will be equal in amplitude and opposite in phase. In fact, this applies to all other odd-order harmonics. Therefore, this creates a low-loss on-chip AC-ground at the common source node and  $V_{DD}$  supply node, which significantly minimizes the impact of package parasitics on power amplifier performance. Under typical conditions, the output is taken differentially so that even-order harmonics are suppressed at the output. Hence, this relaxes the filtering requirements at the output to meet stringent spurious tone emission specifications. In addition, signals injected into the substrate are even order harmonics. Therefore, the impact on the performance of other circuit blocks that are on the same chip is substantially reduced. The most important benefit, in the context of power amplifier designs, is doubling the voltage swing at the output. In fact, a pseudo-differential amplifier is equivalent to a 2-way power combined amplifier. Therefore, in the prototype, four pseudo-differential amplifiers are needed to form an 8-way transformer power combining amplifier.

### **6.1.5 Transconductor Design**

Although RF performance of CMOS devices has been greatly improved in parallel with the rapid technology evolution, it can be severely compromised by parasitics. This is especially true for power transistors. The gate-width of a power transistor is usually very large and can reach several millimeters to achieve desired gain and output power. For instance, let's calculate the poly gate resistance of a transistor with dimensions of  $2000\text{-}\mu\text{m}/0.13\text{-}\mu\text{m}$ , assuming the sheet resistance  $R_{\text{sheet}}$  is  $10\text{-}\Omega/\text{square}$ :

$$R_G = R_{sheet} \cdot \frac{W}{L} = 153K\Omega$$

Recall that in Chapter 3:

$$f_{max} = \frac{f_T}{2} \sqrt{\frac{1}{g_{DS}(R_G + R_S) + 2\pi f_T R_G C_{GD}}}$$

With more than 100-k $\Omega$  in series with gate, the  $f_{max}$  of the device is certainly not acceptable. Hence, a multi-finger structure with small finger gate width is necessary to reduce gate resistance in order to operate power transistor in RF frequencies. However, as number of fingers (NF) increases, the layout of the power transistor becomes cumbersome. Gradually, extrinsic layout parasitics will dominate over intrinsic parasitics to degrade the RF performance. Figure 6.2 shows a power transistor with some parasitic elements. The source parasitic components cause RF voltage feedback and reduce the gain. The gate and drain parasitic elements induce some non-negligible delay along the signal path, so that output of each individual transistor cannot be added up in phase perfectly.

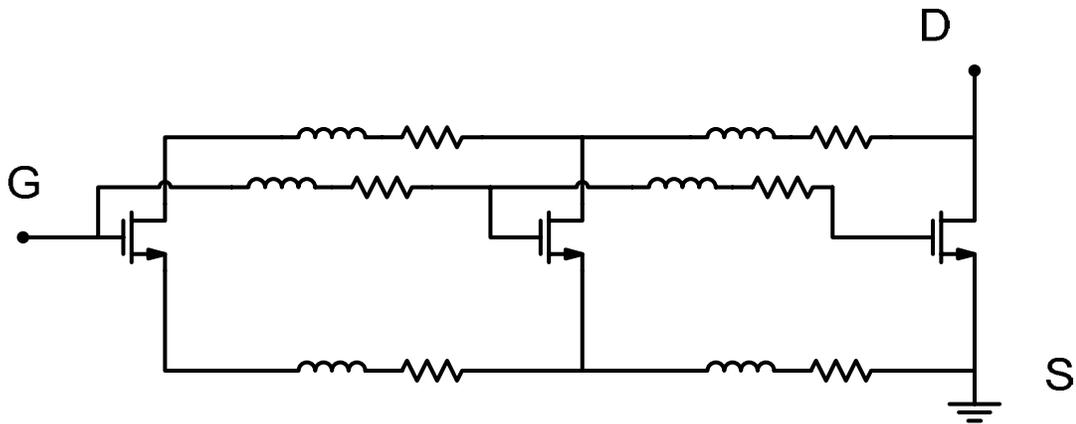


Figure 6.2: A transistor model for power transistors including inductive and resistive parasitic elements

Yet another design trade-off to make is about the substrate resistance. Figure 6.3 illustrates a model of a NMOS device in common-source configuration with a simple substrate network. If  $R_{\text{sub}}$  is large, the transistor performance at RF frequency will be compromised. This could be explained in the following manner. An input signal applied at the gate of the common-source transistor will generate an out-of-phase voltage at the drain. At high frequencies, the large voltage swing at the drain will induce a voltage swing at the back gate (body node). The input signal at the gate and the induced signal at the back gate are out of phase, leading to transconductance degradation at high frequencies<sup>50</sup>. The output impedance degradation at high frequencies can also be explained in a similar way. Besides, this parasitic resistance consumes signal power. Therefore,  $R_{\text{sub}}$  of the transconductor should be properly minimized. The substrate resistance  $R_{\text{sub}}$  is determined by the distance from substrate contacts to the actual transistor.  $R_{\text{sub}}$  is reduced by placing substrate contacts close to the transistor.

Proper biasing of the power transistor is important, because the operating point affects the intrinsic linearity directly. It is well known that the superposition of nonlinearities in the transfer characteristic can reduce/cancel some undesirable nonlinearities. This indeed is the fundamental of class-AB operation [6.1 – 6.3]<sup>51</sup>. In the prototype, the  $g_m$  of the transconductor is one of the major sources of nonlinearity. When MOS transistors are biased from weak inversion region to moderate and strong inversion region, the third-order term  $g_{m,3}$  changes its sign from positive to negative. By biasing the transistor in the weak inversion region (slightly above threshold voltage), the effective average  $g_{m,3}$  can be reduced to zero, hence improving the linearity. At RF

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<sup>50</sup> This is quite obvious from small-signal model.

<sup>51</sup> It should be noted, it only considers AM-AM nonlinearity. In some applications, such as multi-carrier system, AM-PM is more important.

frequencies, the effectiveness of this method can be compromised, because even-order distortion products will feed back through lead inductance, interact with fundamental signals and generate IM products falling into the interested band. In fact, the second-order term  $g_{m,2}$  peaks at the biasing point corresponding to minimum  $g_{m,3}$ . Therefore, even-order terms need to be properly terminated in order to obtain good linearity. This can be done by placing a second order harmonic “trap”, an LC tank, at the drain and the source [6.4], or by placing a large bypass capacitor to reduce voltage swing generated by even-order harmonics as used in this work.

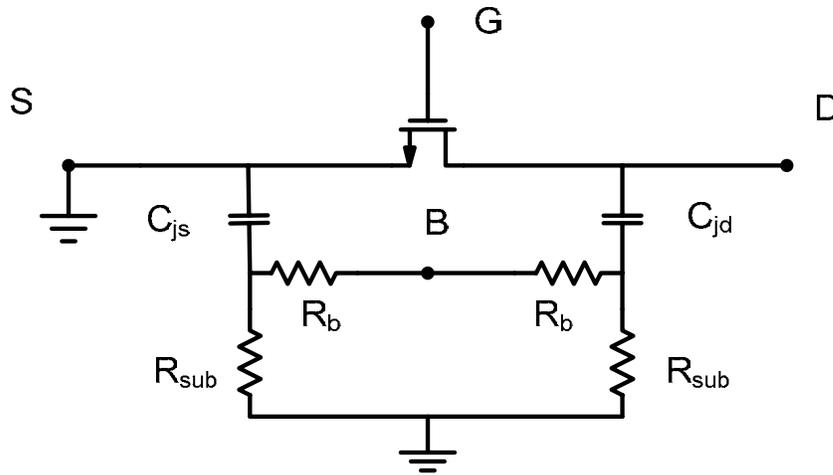


Figure 6.3: A device model of a common-source NMOS transistor with a simple substrate network.  $C_{js}$  and  $C_{jd}$  are junction capacitance of source and drain respectively.  $R_b$  is the effective body resistance.  $R_{sub}$  represents substrate resistance.

### 6.1.6 Cascode Transistor Design

The cascode configuration was employed to ensure reliable operations with 1.2-V supply voltage. Furthermore, it offers several other benefits such as higher gain and

reduced Miller feedback. However, the cascode topology does pose some risks on the stability of the PA.

A simplified model is shown in Figure 6.4(b). Looking into the gate of the cascode device m2, the input impedance is:

$$Z_{in} = \frac{1}{sC_{gs}} + \frac{1}{sC_{par}} + \frac{g_{m2}}{s^2 C_{gs} C_{par}}$$

The real part is:

$$\text{Re}(Z_{in}) = \frac{g_{m2}}{s^2 C_{gs} C_{par}}$$

Obviously it is negative. This definitely poses concerns on the stability of the circuit. There should not be any surprise, since the circuit in Figure 6.4(b) looks like a Colpitts oscillator. Careful design and layout is required to suppress this potential oscillation.

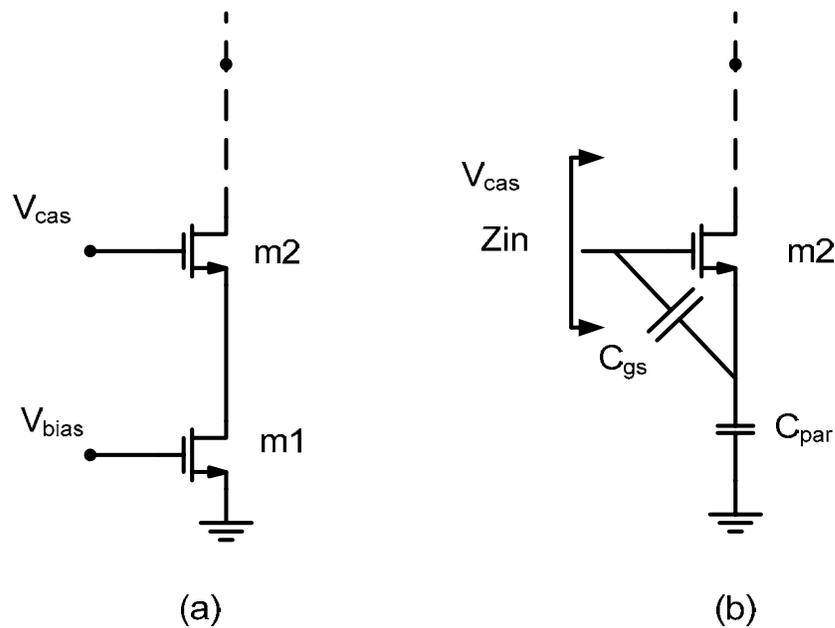


Figure 6.4: (a) A simplified cascode configuration, where m1 is the transconductor device and m2 is the cascode device; (b) An equivalent model for stability analysis.

For convenience, usually the cascode transistor is connected with the supply, although this is neither the only nor the best choice. The size of the cascode transistor is determined after considering several trade-offs. As discussed in Chapter 4, the size and the bias of the cascode transistor will affect the gain, output power and efficiency. Another consideration on the cascode transistor design is AM-PM compensation. The cascode configuration consists of a common-source transistor and a common-gate transistor. Due to the fact that the common-source transistor delivers the output power out-of-phase while the common-gate transistor delivers the output power in phase, their AM-PM conversion at near saturation region are expected to have opposite behaviors [6.5].

The cascode common-gate transistor design is as important as the common-source transconductor design. The design process is rather interactive with the transconductor design, therefore, the design needs several iterations in order to obtain optimum performance.

### **6.1.7 Output Matching Network – Transformer Power Combiner**

The output matching network was designed based on the transformer power combiner described in Chapter 5. It plays two important roles. First, it acts as an impedance transformation network, and combines power from each individual amplifier. Second, it converts a differential signal into a single-ended signal so it can be connected to an antenna directly<sup>52</sup>. High efficiency of the transformer is the prerequisite in order to

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<sup>52</sup> Although differential circuits prevail in transceiver and baseband circuits, almost all the power amplifiers in the market today are single-ended. If the differential topology is employed, a balun is required to convert a differential signal to a single-ended signal. Typical loss of a balun at RF frequencies is around 1-

achieve high efficiency of the entire PA. High component Q and tight magnetic coupling are crucial to reduce the loss in the transformer. One-turn “hair pin” style inductors are implemented to construct the primary and the secondary coils of the transformer. To improve the magnetic coupling, an overlay structure is adopted wherein the secondary coil is placed directly on top of the primary coils. The magnetic coupling factor  $k$  is  $\sim 0.7$  with this structure. A metal shield (M1) is used to reduce capacitive coupling to the conductive substrate. The efficiency of the on-chip transformer is approximately 80%, simulated with ADS Momentum and HFSS.

At power back-off, some amplifiers are turned off, the matching network need be reconfigured to maintain reasonable efficiency. The reconfiguration is necessary due to two reasons. First, the transformer is a passive device, which means it is bilateral. Figure 6.5 shows an equivalent model for a power combining amplifier. Although two amplifiers are turned off, signals on the secondary of the transformer will still be transformed to the primaries and some power is dissipated due to the inductor loss. Therefore, as the amplifier is turned off, the corresponding primary side of the transformer should be reconfigured to minimize this loss.

Second, the impedance seen by the amplifiers remaining on will vary as other amplifiers turned off. To maintain optimum output impedance seen by the amplifiers remaining on, the corresponding primary sides of the transformer also need to be reconfigured to obtain optimum performance<sup>53</sup>. The detailed hand analysis is very complicated, and the result is highly depended on the transformer style itself. In practice,

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dB. And such a balun is costly and occupies lots of board space. Hence, a differential PA is very hard to sell in the market. In this work, a balun is not needed in the design which offers a great advantage.

<sup>53</sup> The secondary will have large swing, and it is better to leave intact.

simulations should be employed to help designers to complete the design of the output matching network.

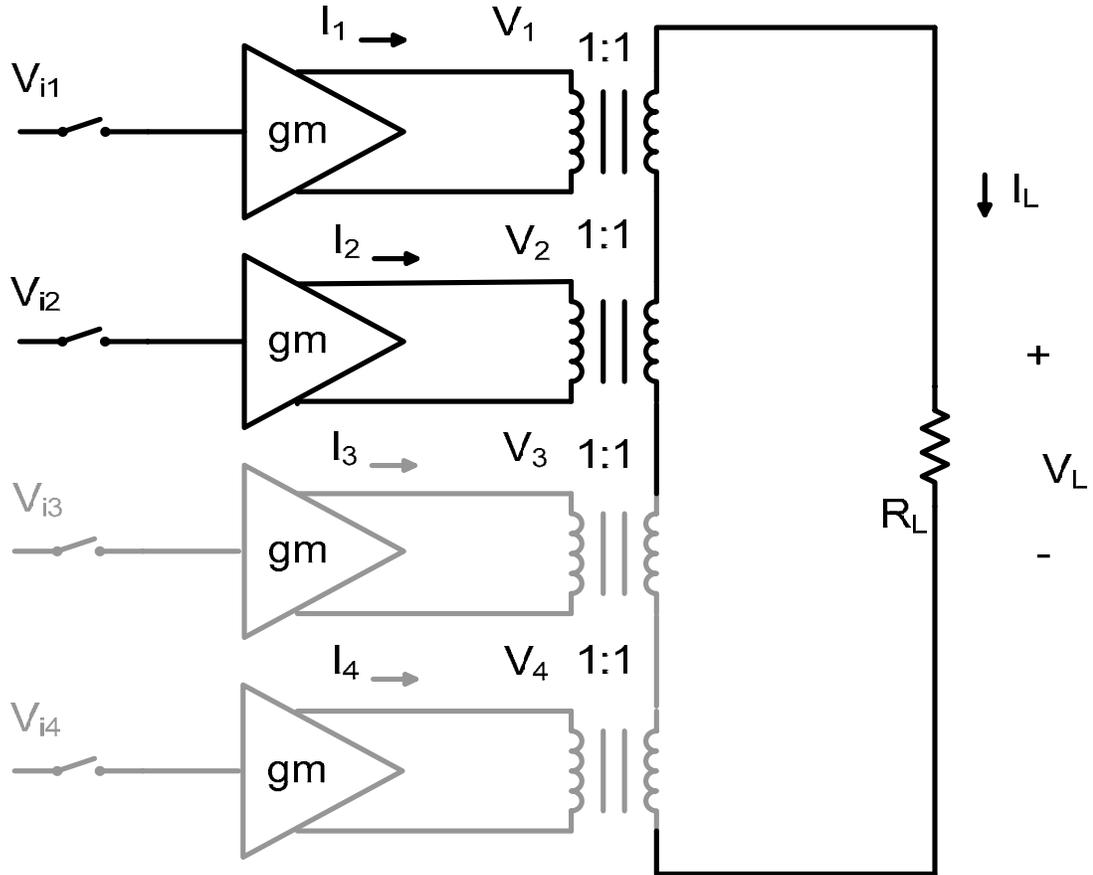


Figure 6.5: An equivalent model of a power combining amplifier. Two amplifiers are turned off, while the other two remain on.

The reconfiguration of the transformer is achieved by switching capacitors in and out. It must be carefully designed to ensure it has enough range to compensate process variation and has low loss (Figure 6.6).

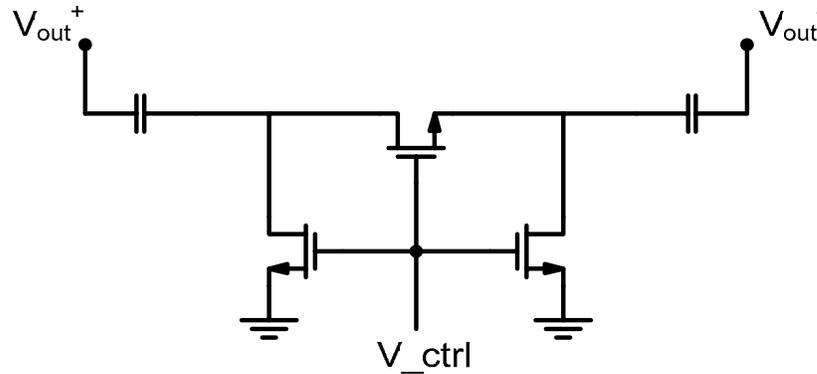


Figure 6.6: A switched capacitor array. This configuration takes advantage of differential operation to minimize switch losses without the need for large size switches.

### 6.1.8 Stability

Almost every PA design is susceptible to unwanted and potentially destructive oscillations in power amplifiers. Extra attention paid during the design stage should eliminate this risk, or at least make it less likely. Stability analysis available in circuit simulators assumes the entire circuit is linear, although power amplifiers are very nonlinear. To get around this issue, stability analysis is performed while sweeping the operating point in order to gain insights into the stability of the power amplifier under large signal operation. Of course, transient analysis is always needed as the final check<sup>54</sup>.

For the proposed power combining amplifier, the inputs of each individual amplifier are connected with interconnects. Because the dimensions of the layout are rather large, those interconnects behave like transmission lines. This, in turn, gives a potential oscillation problem, odd mode oscillation, which is a common problem in

<sup>54</sup> It was found that small-signal stability analysis across swept operating points is a very good indicator of the stability under large signal operation.

power amplifiers using cluster matching [6.6]. Figure 6.7 illustrates a 2-way power combined amplifiers oscillating in the odd mode.

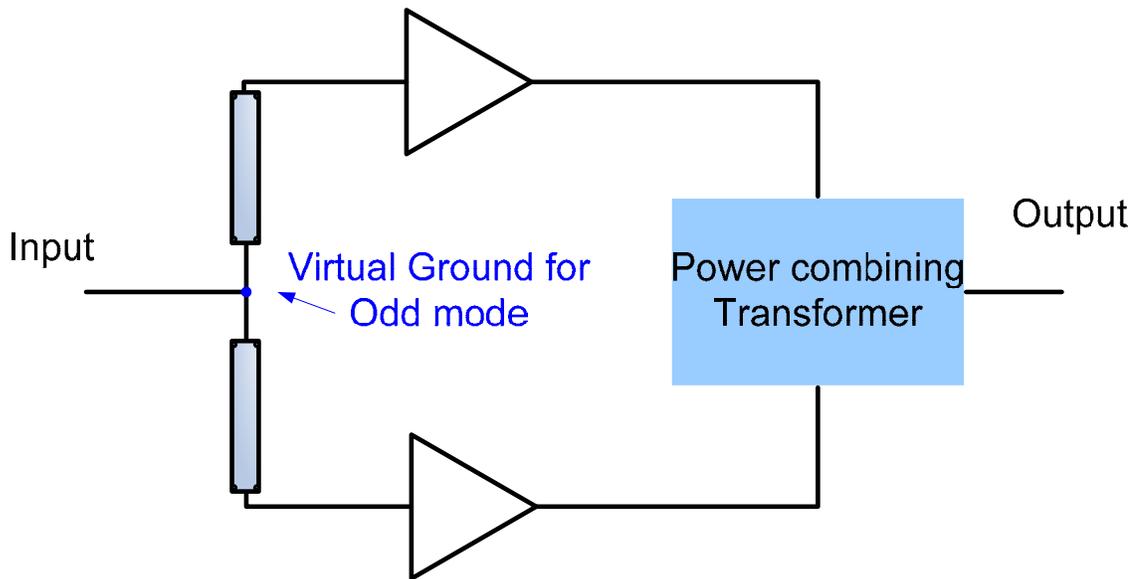


Figure 6.7: A two-way power combined amplifier. Notice the virtual ground of odd mode oscillation.

To suppress oscillations, a resistor is connected in series with the gate to reduce the loop gain. The amount of resistance should be designed in conjunction with the transconductor design. Some other de-Q'ing resistors are placed in the bypass network and bias network to ensure a stable power amplifier. The detailed stability analysis is beyond the scope of this work, though there is further study needed to investigate the stability of power combined amplifiers. There are some preliminary research results on this issue. Interested readers are encouraged to consult those resources, such as [6.7].

## 6.2 Layout Considerations

The importance of layout in power amplifier designs needs no introduction. In this section, several practical considerations are presented. However, it should be noted that there are many ways to layout one structure. Trade-offs have to be made based on different considerations of each individual case.

### 6.2.1 Transconductor Layout

Based on the considerations discussed previously, a large power transistor can be obtained by connecting unit cells in parallel. The dimension of the unit cell is determined by trade-offs discussed before. The distance between unit cells is another factor under consideration by the designer during layout. Decreasing of this distance is of course the advantage from integration density perspective. However, this results in higher chip temperature due to heat flow degradation. If the distance is too large, parasitic elements will degrade the RF performance. In order to minimize the source resistance, which degrades the gain, output power and efficiency, the source electrode is contacted on both sides of the transistor.

Assembling smaller unit transistors into a much larger power transistor entails a trade-off between the chip size and the delay equalization. Transistors are typically laid out in grid fashion without considering the delay along the signal path to each transistor (Figure 6.8). This approach will not cause any problem when the transistor is small. However, for power transistors, it will degrade the performance greatly, since signals from each unit transistor will not sum up in phase. Furthermore, some unit transistors experience excessive voltage drops comparing to others, and current is not evenly

distributed in the device. A different approach, referred as “tree” layout, guarantees equal delay<sup>55</sup>. The signal will reach each unit transistor simultaneously, and the output from each unit transistor will arrive at the summing point simultaneously (Figure 6.9). As the reader might expect, this is obtained at the expense of large area and high parasitics. A desirable layout should be compact and delay-equalized as shown in Figure 6.10. If the delay of the input signal is made equal to the delay of the output signal, then a delay-equalized structure is obtained. Meanwhile interconnects should be laid out to minimize uneven current distribution and excessive voltage drops.

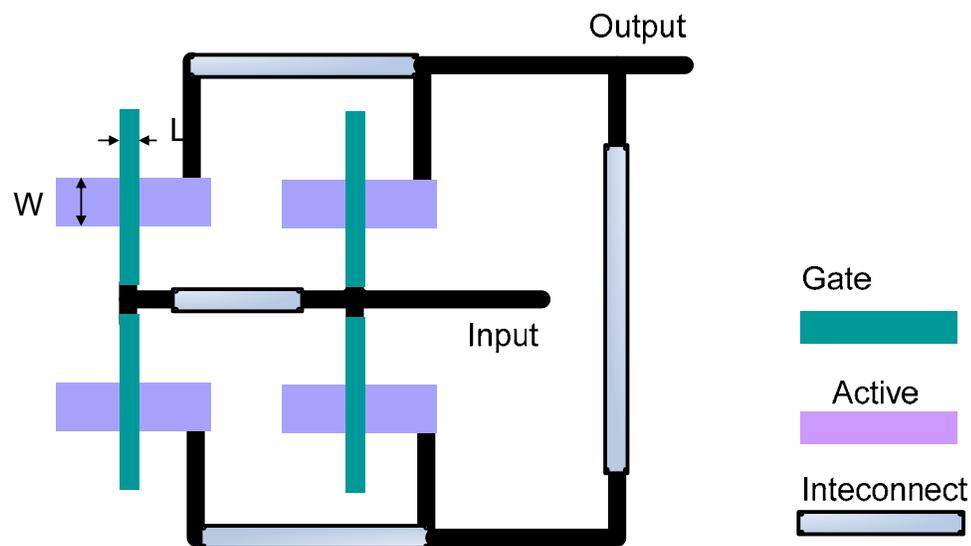


Figure 6.8: A conventional transistor layout. Note that the unequal delay among unit transistors leads to performance degradation.

<sup>55</sup> It is often seen in clock distribution in digital circuits.

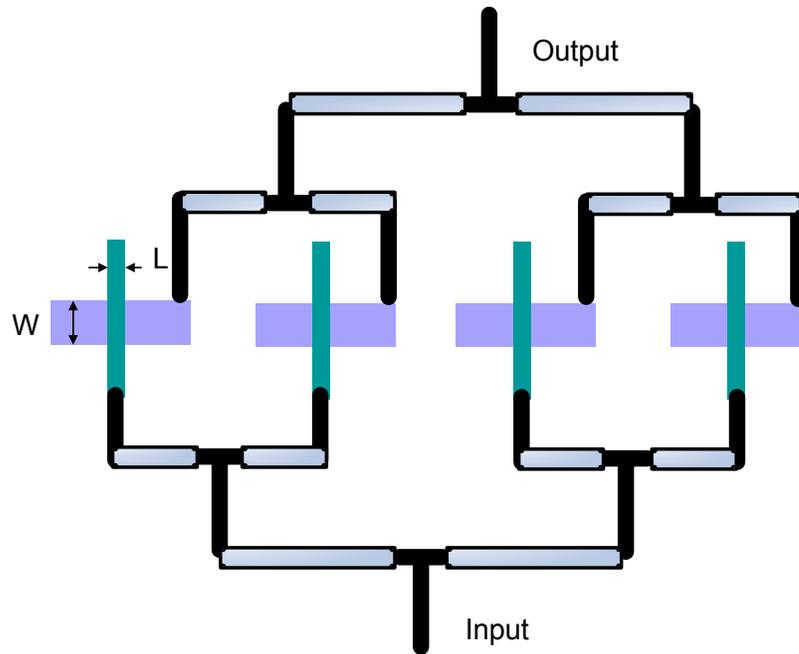


Figure 6.9: A power transistor laid out in "tree" layout.

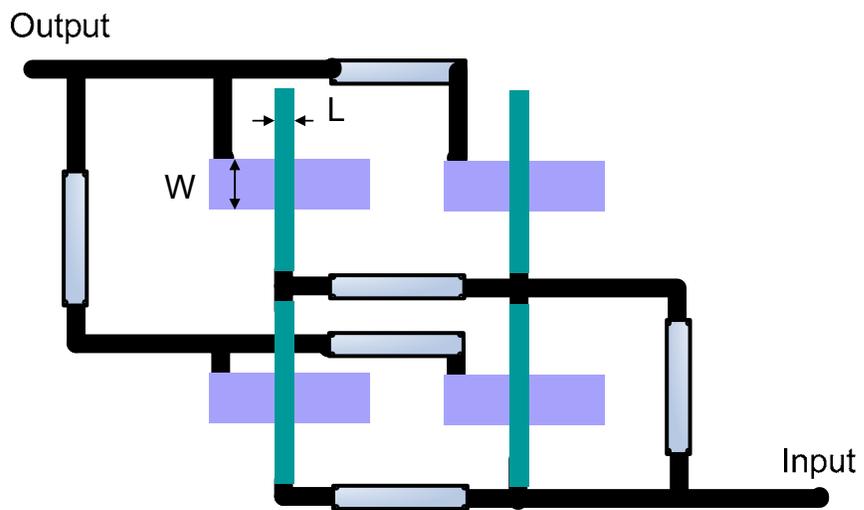


Figure 6.10: A delay-equalized compact layout of a power transistor.

## 6.2.2 Cascode Transistor Layout

The layout of a cascode circuit can be simplified if the input device m1 and the cascode device m2 have equal sizes<sup>56</sup>. As shown in Figure 6.11(a), the drain of m1 and the source of m2 can share the same junction. More importantly, the size of this junction can be made much smaller than a regular junction, if it does not need to be accessible. Consequently, the parasitic capacitance at that node is reduced substantially, improve high frequency performance. For power amplifiers, this helps to improve power efficiency.

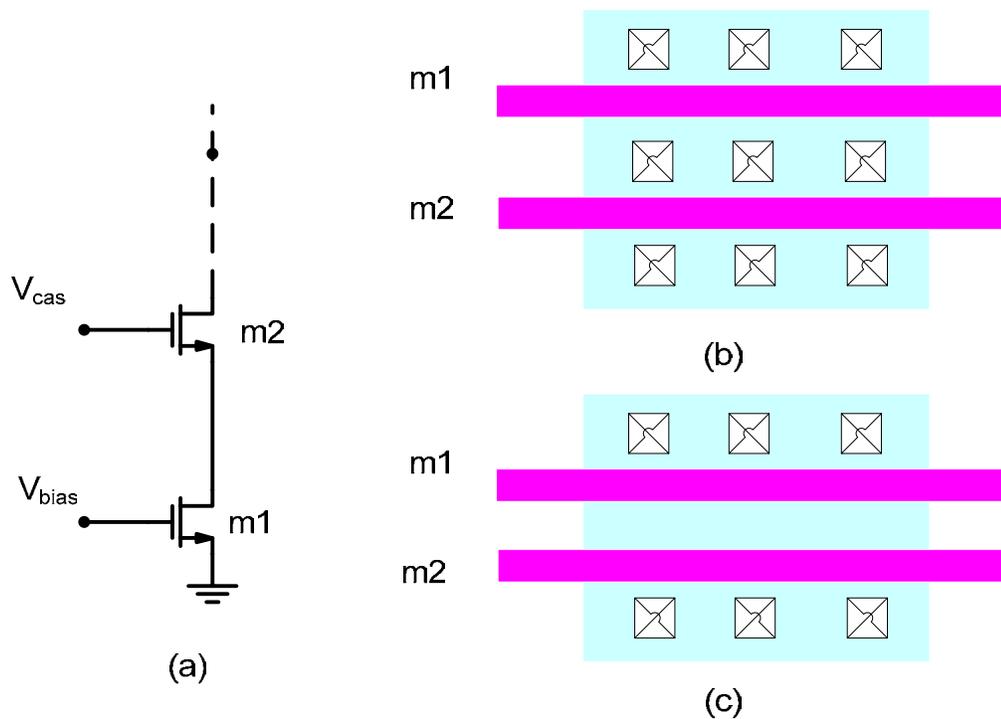


Figure 6.11: (a) The schematic of a cascode circuit; (b) The conventional layout of a cascode circuit, in which cascode devices have the same width; (c) The improved layout of a cascode circuit, with reduced parasitic capacitance at the shared junction.

<sup>56</sup> In fact, they only need to have equal width.

### 6.3 The CMOS Prototype

Using the approach describe above, with iterations in some critical steps, the prototype was designed and implemented in a 0.13- $\mu\text{m}$  CMOS process.

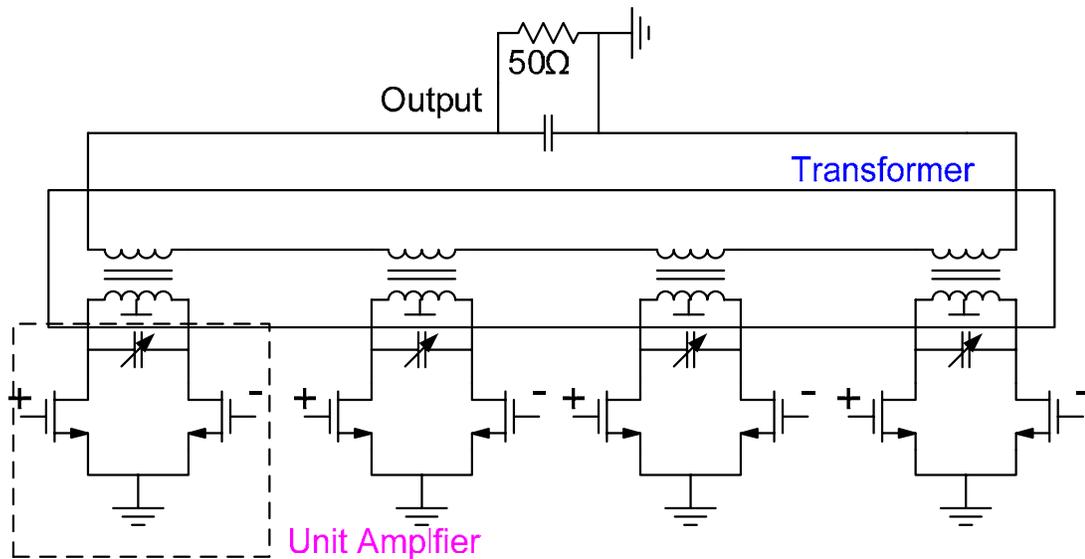


Figure 6.12: The simplified schematic of the prototype.

Figure 6.12 illustrates the simplified schematic of the prototype, an 8-way power combined amplifier. Figure 6.13 shows the dimensions of the power combining transformer used to combine power from each individual amplifier. Figure 6.14 illustrates the simplified schematic of each unit amplifier. The cascode device has the same sizes as the transconductor transistor for layout simplicity. None minimum channel length thin-oxide devices were employed to ensure reliable operations. Figure 6.15 shows the micrograph of the prototype. The chip area is measured as 2-mm x 1-mm, including pads. The prototype takes differential RF input signal and transmits single-

ended output. Simulation results of the prototype are shown in Figure 6.16, Figure 6.17 and Figure 6.18.<sup>57</sup>

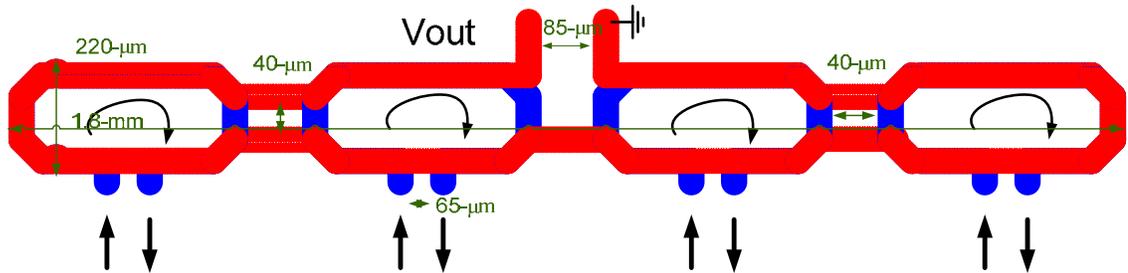


Figure 6.13: The power combining transformer in the prototype

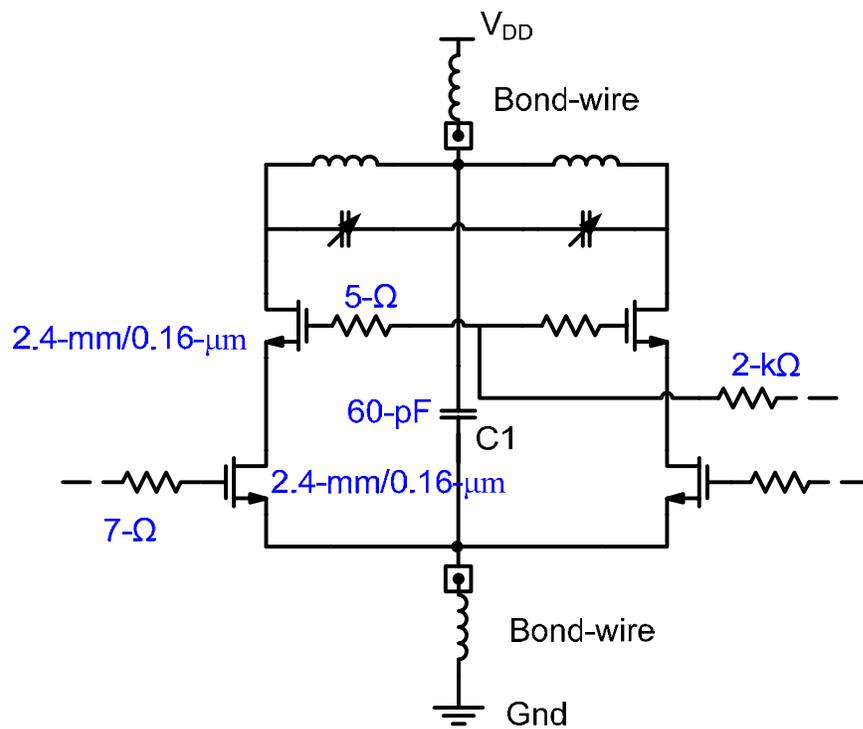


Figure 6.14: The simplified schematic of each unit amplifier.

<sup>57</sup> Simulations were performed with SpectreRF.

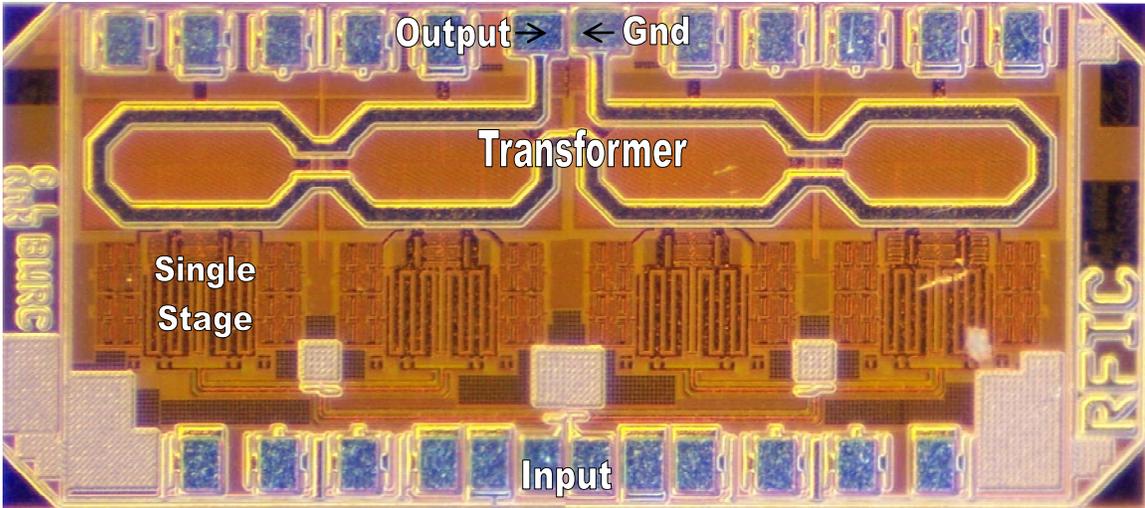


Figure 6.15: Die Microphotograph of the Prototype

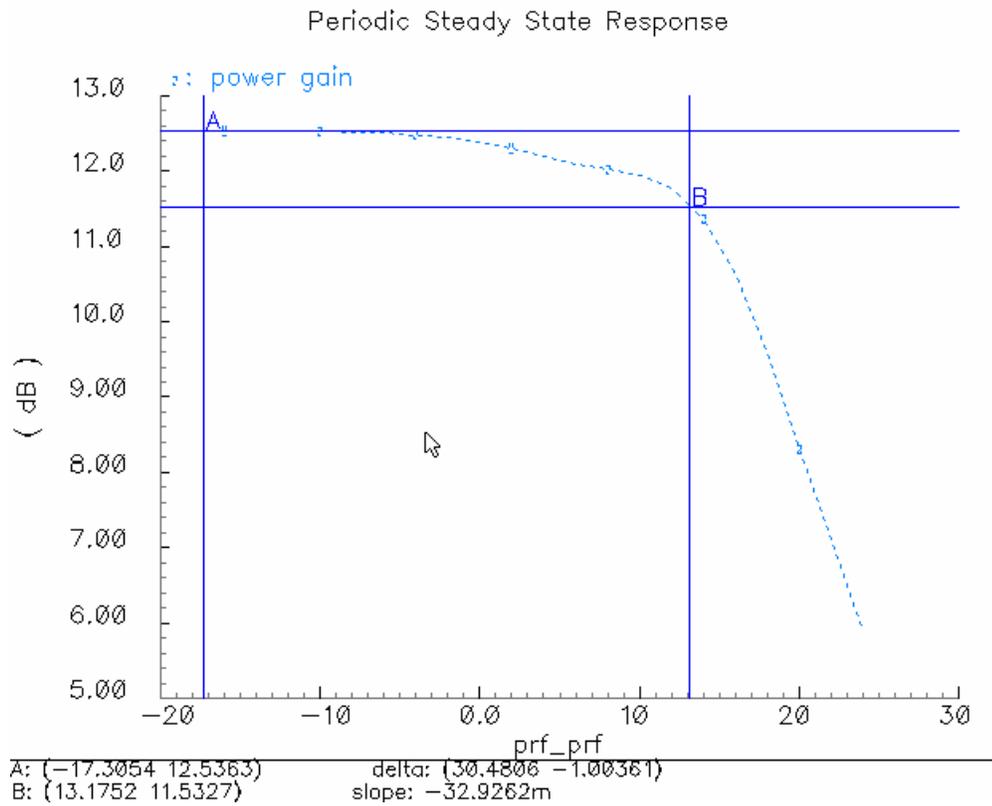


Figure 6.16: The power gain of the prototype when all unit amplifiers are on.

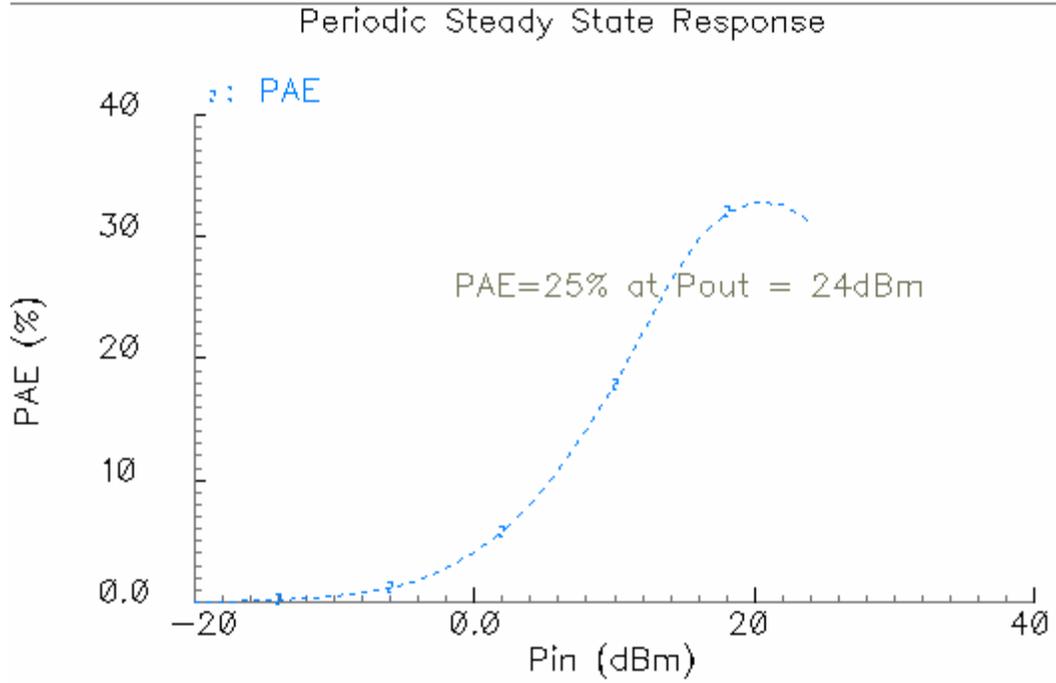
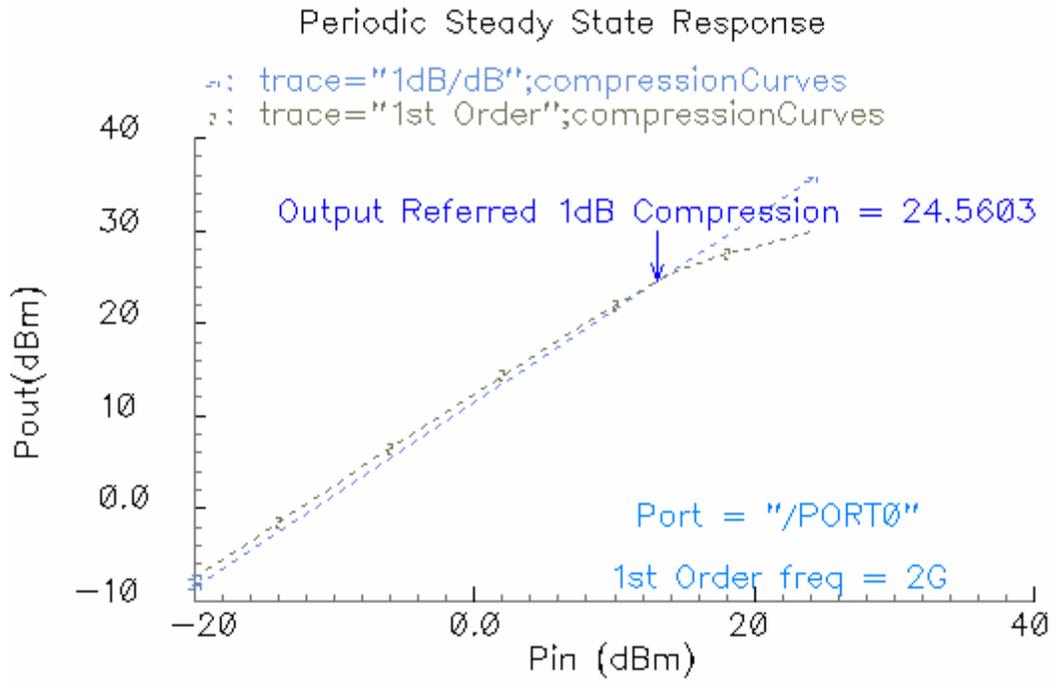


Figure 6.17: One tone simulation results when all unit amplifiers are on.

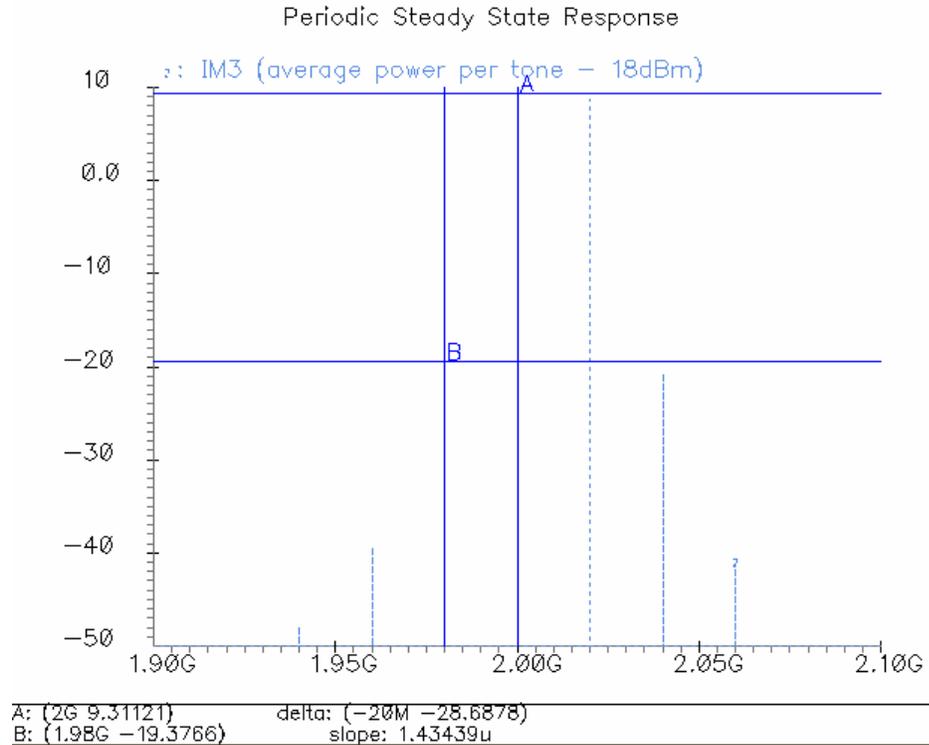


Figure 6.18: Two tone simulation results when all unit amplifiers are on. The simulation is performed when output power per tone is 18dBm (around 9dBv with 50 ohm reference). Note that the imbalance is mainly because input matching is not designed.

## 6.4 Experimental Results

During measurements, the chip was directly glued to the printed circuit board using conductive adhesives. All the pads, including input and output pads, were wire bonded on the board. Each pad was bonded to the test board with only one bond-wire, although multi bond-wires can be employed to minimized lead inductance. No off-chip impedance matching elements are needed or used in this design. The input is driven by a commercial driver amplifier through an off-chip balun. Since the input is not matched, power gain is not known exactly. According to simulation, the power gain is 10 dB. The

amplifier was tested with a 1.2V power supply. The cascode node was tied to the power supply. It drew 114mA DC current without RF signals applied.

### 6.4.1 CW Signal Test

The output was directly connected to a power meter with two 6-dB attenuators for power measurements. All system losses were calibrated out, while the measured results included losses on the board and bond wire losses. Output power and drain efficiency versus input power (read from the signal generator) for a single-tone test is shown in Figure 6.19. The PA transmits up to 24-dBm linear power with 25% drain efficiency, centered at 2.4-GHz. When driven into saturation, it delivers 27-dBm power with 32% drain efficiency.

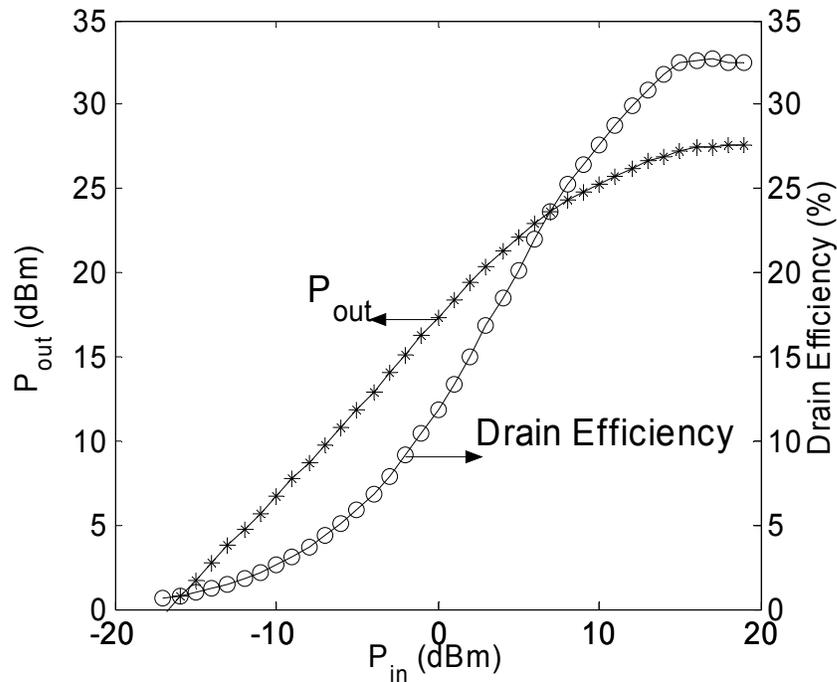


Figure 6.19: Measured output power and drain efficiency from single-tone test.

Under the same bias conditions, a two-tone test was performed at 2.4-GHz with 1-kHz tone spacing. Little asymmetry was observed during testing. The results are shown in Figure 6.20. When the average output power per tone is 18-dBm, measured IM3, IM5 and IM7 are -29dBc, -36dBc and -42dBc respectively.

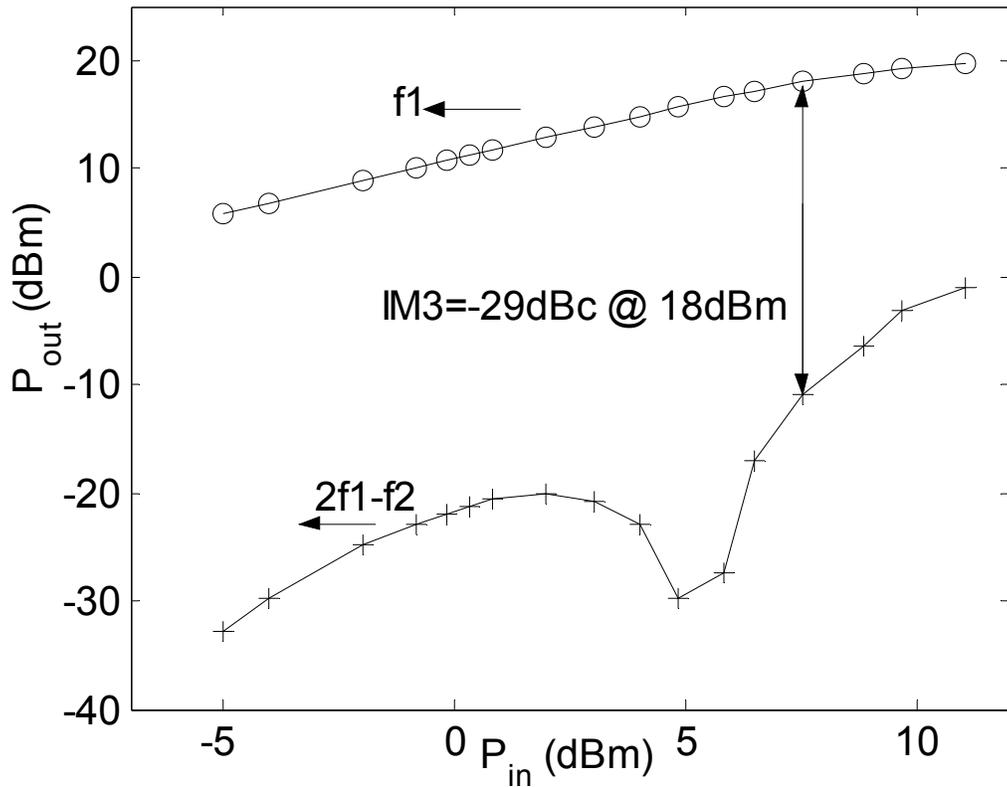


Figure 6.20: Measured output power and IM3 from a two-tone test (1-kHz tone spacing)

Figure 6.21 shows the measured results which matches simulated results<sup>58</sup>. With 1.2-V power supply, a peak power of 27-dBm is measured with 32% drain efficiency, when all of four amplifiers are on. When output power is at 2.5-dB back-off from peak

<sup>58</sup> At high power region, the measured result differs from the simulated result because of the rise of chip temperature. All simulations are done with 25°C temperature setting.

power, in the PA employing average efficiency enhancement circuitry, one amplifier is turned off and the other three remain on. The drain efficiency is measured as 31.5% at 24.5dBm, very close to the drain efficiency at peak output power. In contrast, drain efficiency is 5% lower in the conventional PA at 2.5-dB back-off. In fact, as shown in Figure 6.22, further enhancements of efficiency in the back-off region can be obtained by turning off the remaining amplifiers sequentially, when output power is at 6-dB and 12-dB back-off.

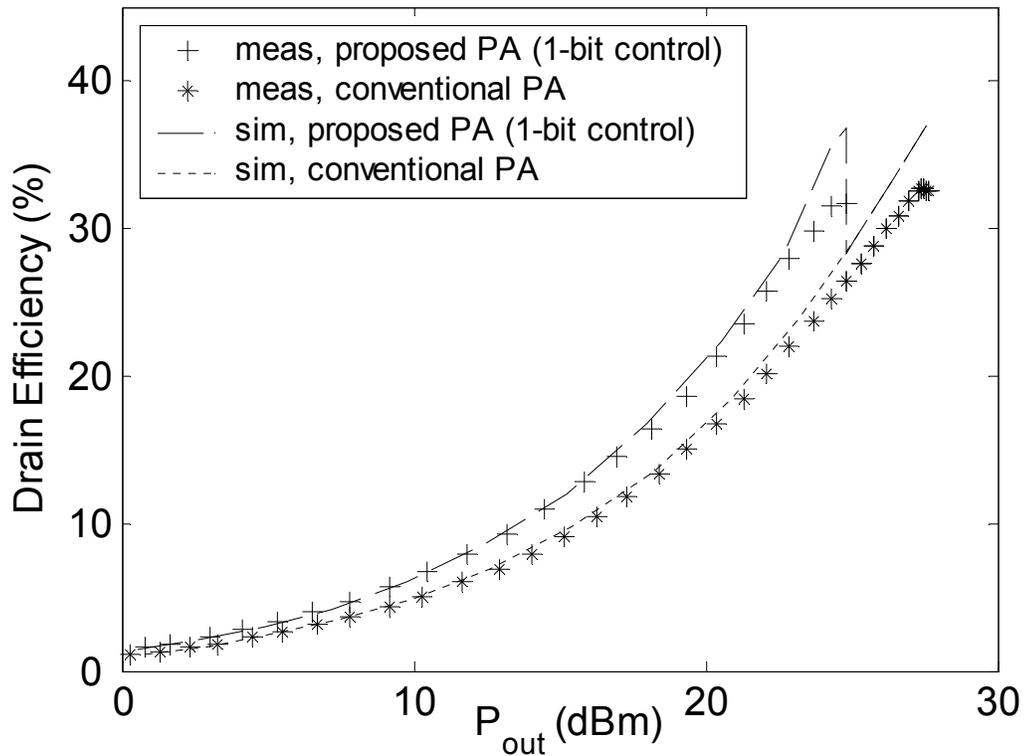


Figure 6.21: Simulated and measured drain efficiency of the proposed PA, in comparison with those for the conventional PA.

To verify the concept of the average efficiency enhancement technique, two PAs are compared. They use the same devices and the same power combining transformer, with the exception that one employs the efficiency enhancement circuitry.

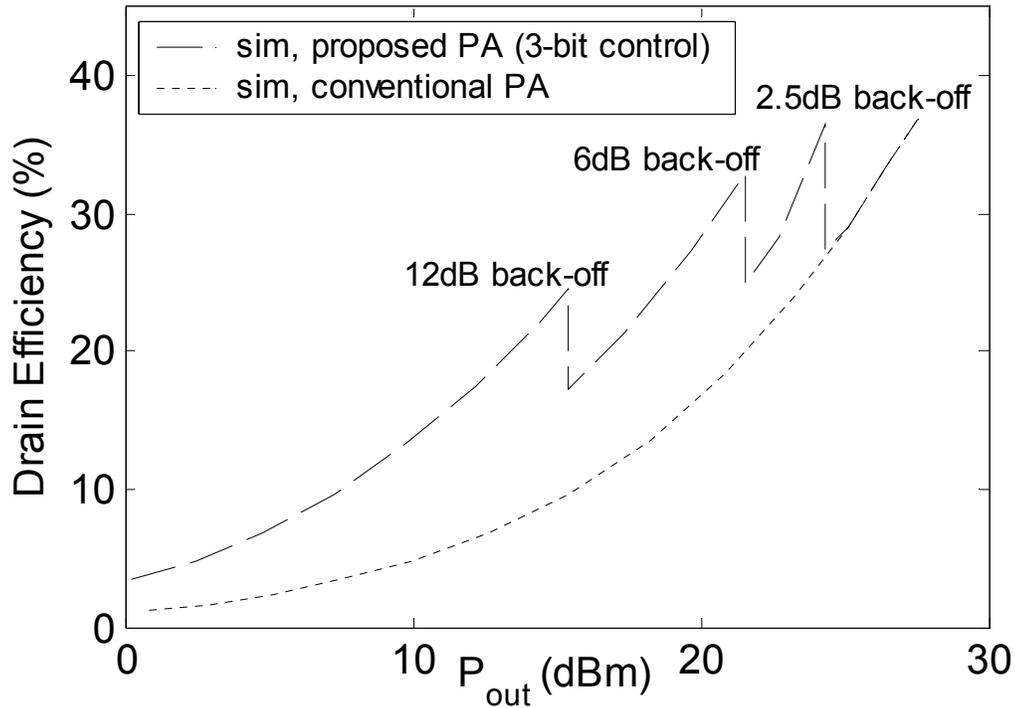


Figure 6.22: Simulated drain efficiency of the proposed PA with power back-off, in comparison with that for the conventional PA

#### 6.4.2 Modulated Signal Test

Although the prototype was not designed to meet any standards, it was tested with EDGE and 802.11g signals to see its linearity with modulated signals. Because automatic power control circuit was not implemented with the prototype, the improvement on average efficiency cannot be tested with modulated signals.

First, it was tested with GSM/EDGE signal, which provides high data rate over 200-kHz carrier bandwidth. In addition to Gaussian minimum shift keying (GMSK), EDGE uses 8 phase shift keying (8PSK) for the upper five of its nine modulation and coding schemes to achieve higher data rate than GSM. It has peak-to-average ratio of 3.2-dB, and peak-to-minimum ratio of 17-dB. The measured peak output power while still meeting the spectral mask is 21.75-dBm after calibrating out 1.25-dB cable loss (Figure 6.23)<sup>59</sup>. The drain efficiency is approximately 20%.

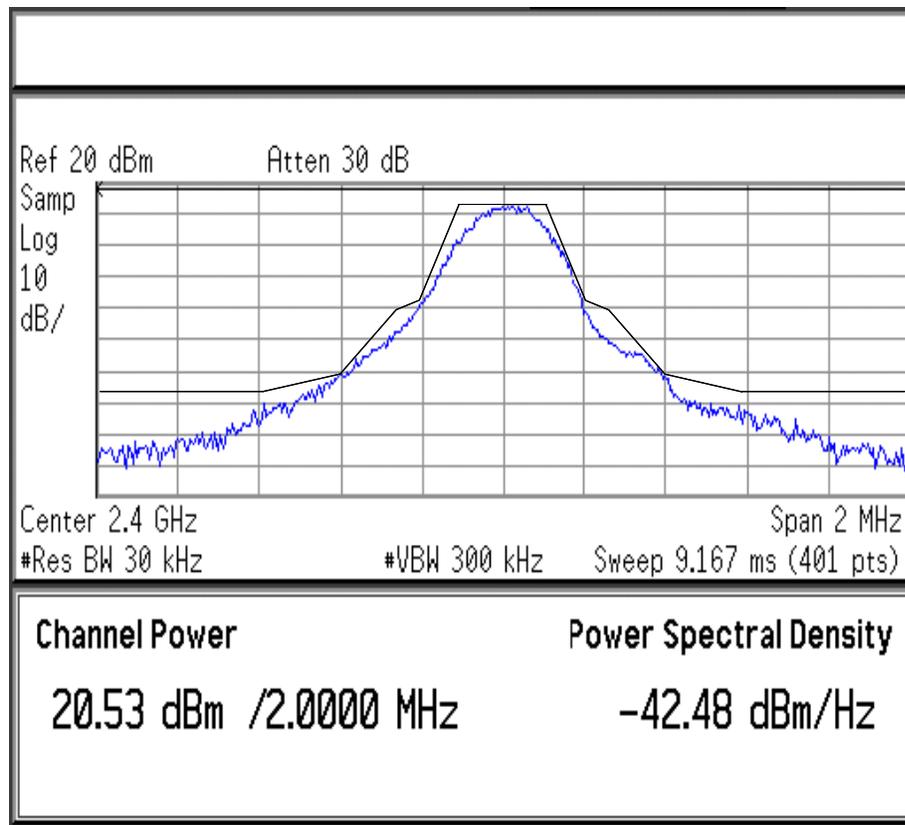


Figure 6.23: Output spectrum with GSM/EDGE signal. Measured PSD at offset frequencies are: at  $\pm 200$ -kHz, -30.75-dBc, -30.3-dBc (spec: -30-dBc); at  $\pm 400$ -kHz, -55.3-dBc, -55-dBc (spec: -54-dBc); at  $\pm 600$ -kHz, -64.4-dBc, -63.9-dBc (spec: -60-dBc)

<sup>59</sup> As mentioned in Chapter 2, narrow-band system is usually limited by spectral emissions. EVM requirements are easily achieved. This is in contrast to wide-band system, which is usually limited by EVM requirements.

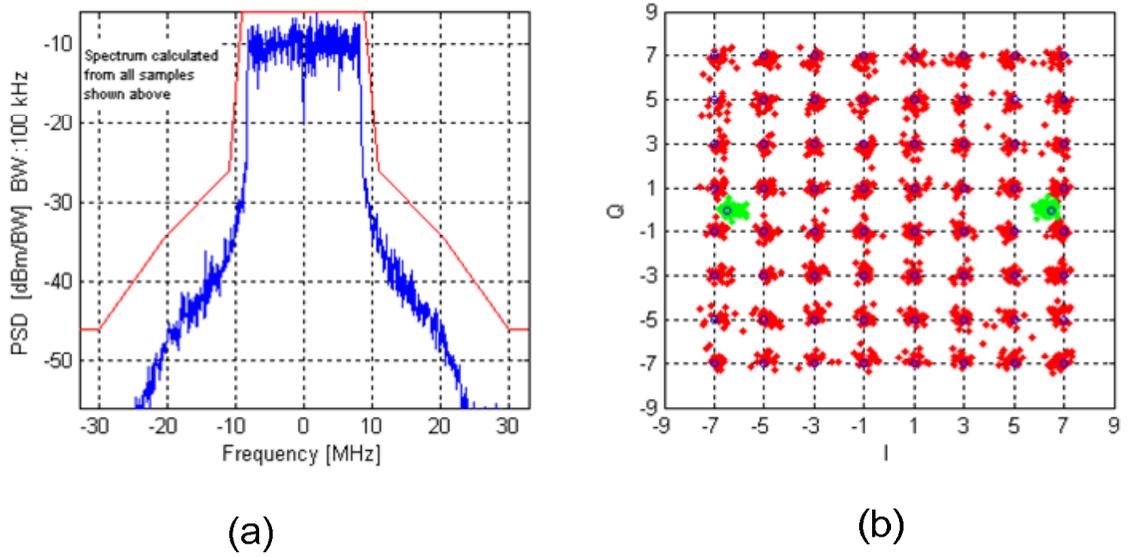


Figure 6.24: Measured at  $P_{\text{out}} = 14.5\text{-dBm}$  with 4.48% EVM. (a) Output spectrum; (b) Rectangular constellation diagram

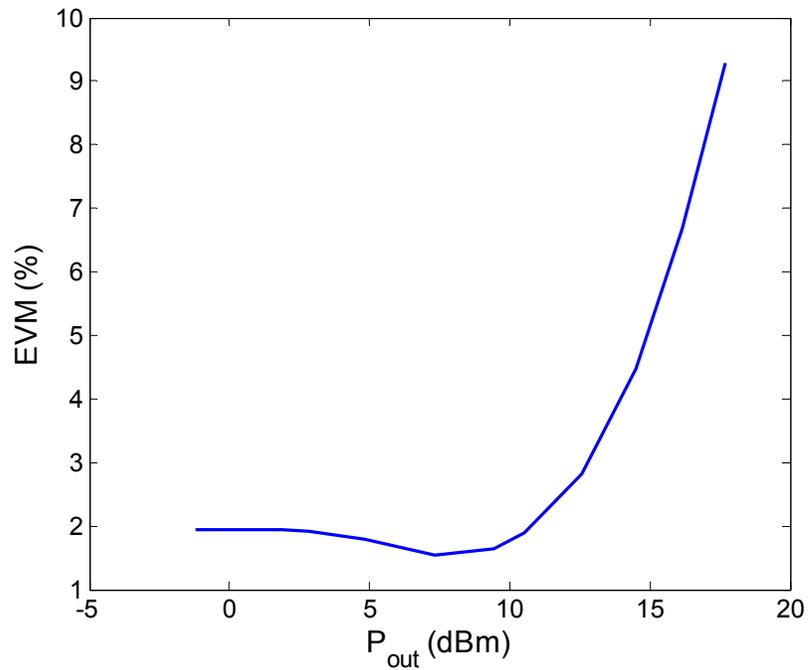


Figure 6.25: Measured EVM vs. output power

## 6.5 Summary

In this chapter, the design approach of the power amplifier with average efficiency enhancement is first described. The prototype was implemented using the design methodology in a 0.13- $\mu\text{m}$  CMOS process. The measurements prove the average efficiency enhancement technique, and the effectiveness of the design methodology. Tests with modulated signals show that this amplifier is linear to be used in state-of-the-art wireless communication systems.

## 6.6 References

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## Chapter 7. Conclusion

7.1 Thesis summary

7.2 Possible future directions

### 7.1 Thesis Summary

Explosive growth in wireless communication market has led to consumer demand for low-cost, small form factor, low power terminals. It has been proven in practice that high level of integration is the most effective way to provide such a solution. The VLSI capabilities of CMOS make itself a well-suited vehicle for high integration. Although it was certainly a non-trivial task to realize system-on-chip (SoC), engineers from industry together with researches from universities have figured out ways to integrate almost an entire system on a single chip. Yet there is still one piece missing on the integration chart, the power amplifiers.

Two major hurdles associated with the design of fully integrated CMOS power amplifiers are low transistor breakdown voltage/high threshold voltage, and high loss impedance transformation network consisting of lossy on-chip passives. To overcome those two hurdles, highly efficient power combining can be used to generate enough power with good overall efficiency.

Besides integration, there is another serious issue associated with PA design which is inherent to conventional PA. It is well known that a PA can only achieve maximum efficiency at peak output power. As output power decreases, efficiency drops rapidly. However, the need to conserve battery power and to mitigate interference to

other users necessitates the transmission of power levels well below the peak output power of the transmitter. Moreover, since spectrum is a scarce commodity, modern transmitters for wireless communications employ spectrally efficient digital modulations with high peak-to-average ratio. Because of these reasons, the PA transmits much lower than peak output power under typical operating conditions.

This thesis started with an overview of the developments in the field, examined several important characteristics of a power amplifier, and compared prevalent technologies for RF power amplifiers, especially CMOS technologies. In Chapter 4, after presenting various power combining approaches, a simple yet elegant power combining transformer was proposed as a means to enable CMOS integration and improve average efficiency simultaneously. The design of the proposed transformer was analyzed in Chapter 5. The CMOS prototype was implemented and tested to verify the concept. The design methodology and the experimental results were presented in Chapter 6. With 1.2V supply, it transmits linear power up to 24dBm with 25% drain efficiency. When driven into saturation, it transmits 27dBm peak power with 32% drain efficiency. As one of the four amplifiers is turned off for 2.5dB power back-off from 27dBm, drain efficiency is improved from 26.5% to 31.5%, very close to instantaneous drain efficiency at peak power. To test its linearity, GSM/EDGE and 802.11g OFDM signals were used as test signals. The measured results demonstrated that the prototype is linear enough to amplify high peak-to-average modulated signals linearly.

## 7.2 Possible Future Directions

Almost every research contributes something to the understanding of the specific subject. Meanwhile, it also opens the door to many other new topics. This work is no exception. While this work demonstrated average efficiency enhancement technique at power back-off, the automatic power control circuitry was not designed due to time constraints at the time of tape-out. A natural extension of this work is to include that in the prototype and verify its effectiveness with high peak-to-average ratio signals. It should be noted that AM-PM behavior should be carefully studied as individual amplifiers are turned on/off. For modulated signals with high peak-to-average ratio, the probability of signals with large envelope is very small, so does the probability to switch capacitors. Therefore, switched capacitor arrays work at low frequency. Nonetheless, quantization noise from switching actions needs to be carefully investigated.

A better approach to handle modulation schemes with high peak-to-average ratio is presented in Chapter 4, the transformer coupled outphasing amplifier. It is another interesting case to study. Given the fact that DSP is getting more powerful and the cost overhead is diminishing, outphasing amplifiers is certainly worth investigation. In this approach, nonlinear amplifiers could be used to achieve linear amplification, which certainly presents many advantages. With the proposed power combining transformer, the load is automatically modulated at the power back-off by varying phase modulation. Therefore, average efficiency is improved.

It was noted that AM-PM becomes more important in modern modulation schemes which employ multi-carrier for spectral efficiency and robustness. In practice, it was found that AM-AM characteristic is correlated with odd order terms in a power

series expression, while AM-PM characteristic is correlated with even order terms. This fact will certainly have impacts on the biasing point of a linear power amplifier. More in-depth study is very necessary to fully understand this point.