

Milli-Volt Micro-Electro-Mechanical Relay Technology for Energy-Efficient Computing

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By

Benjamin O. Osoba

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requirements for the degree of

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Committee in charge:

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Professor Kristofer Pister

Professor Junqiao Wu

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By

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Abstract

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Professor Tsu-Jae King Liu

The proliferation of information and communication devices over the past few decades has been enabled by continual advancement of semiconductor manufacturing technology to steadily miniaturize semiconductor switching devices – most notably, metal-oxide-semiconductor field effect transistors (MOSFETs) – to increase the number of transistors in the most advanced integrated circuit (IC) products, at a pace set by Moore’s Law, for enhanced chip functionality and performance. In recent years, however, the incremental benefit of transistor scaling has diminished largely because the Boltzmann energy distribution of electrons in a semiconductor results in switching steepness (subthreshold swing) proportional to the thermal voltage ($\frac{kT}{q}$), which does not scale. As a result, conventional MOSFETs cannot switch ON/OFF more abruptly than 60 mV/decade at room temperature, which limits the extent to which the transistor threshold voltage (V_T) can be reduced for a given OFF-state leakage current specification (I_{OFF}). As the operating voltage (V_{DD}) of a digital IC is reduced with increasing transistor density to meet power density constraints (set by chip cooling limitations), then, the gate overdrive voltage ($V_{DD} - V_T$) is disproportionately reduced, limiting the transistor ON-state current and hence IC performance. With the advent of the Internet of Things, the need for more energy-efficient electronics has emerged; alternative switching devices that can be operated at much lower voltage than the MOSFET will be required. Micro-electro-mechanical (MEM) relays are promising candidate switching devices for low-voltage digital ICs, since they can achieve immeasurably low I_{OFF} and abrupt switching behavior across a wide range of operating temperatures. Since MEM relays exhibit hysteretic switching behavior (*i.e.*, the value of the control/gate voltage at which a relay switches ON is different than that at which it switches OFF) the hysteresis voltage sets a lower limit for their operating voltage.

This dissertation discusses approaches and challenges for realizing milli-Volt MEM relay technology for energy-efficient computing. First the application of self-assembled molecular (SAM) anti-stiction coatings to reduce contact adhesive force and thereby the hysteresis voltage is investigated, and stable sub-50 mV operation is demonstrated. Next the issue of variability in relay performance parameters over many switching cycles and from device to device is systematically studied, and SAM coating is found to improve stability. Then the effects of contacting electrode design and body-biased operation on relay ON-state resistance (R_{ON}) are investigated. The direct

source/drain contact design provides for lowest and least variable R_{ON} . Ultra-low-voltage relay operation facilitated by body-biasing results in lower contact velocity, which mitigates the need for a wear-resistant contacting electrode material while necessitating a contacting electrode material that is not susceptible to oxidation.

For my family,
past, present and future

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CHAPTER 1:

Introduction

1.1 BRIEF HISTORY OF INTEGRATED CIRCUIT (IC) COMPUTING DEVICES

Since the late 1950s, the electronics industry has rapidly advanced and proliferated throughout the world, bringing about the digital information age that has transformed various aspects of life in modern society. Examples include the Apollo Guidance Computer that facilitated the successful Apollo space program in the 1960s [1], and computer control of sound synthesizers via the Musical Instrument Digital Interface (MIDI) invented in 1982 [2] that revolutionized music performance, production and recording. The development of the integrated circuit (IC) [3] and steady advancement in planar semiconductor processing technology [4] to enable ever higher levels of component integration on an IC “chip” following Moore’s Law [5] has provided for continual reductions in cost per function and increases in computing performance (operations per second). Today, state-of-the-art ICs comprise billions of semiconductor devices known as transistors. The Metal Oxide Semiconductor Field Effect Transistor (MOSFET) is the predominant type of transistor used for computational ICs, and act as switches that either allow current to flow (in the ON state) or prevent current from flowing (in the OFF state) to implement digital logic functions [6][7].

1.2 CMOS TECHNOLOGY AND DIGITAL LOGIC

Schematic illustrations of n-channel (NMOS) and p-channel (PMOS) field-effect transistor structures are shown in **Fig. 1.1**. The ON/OFF state of a MOSFET is controlled via voltage applied to the Gate electrode (V_G) relative to the voltage applied to the heavily doped (electrically conductive) Source region (V_S). The Gate voltage is capacitively coupled to the electric potential of the semiconductor Channel region under the Gate electrode, and thereby controls the height of

the potential barrier between the heavily doped (electrically conductive) Source region and the Channel region. When a driving voltage (V_{DS}) is applied between the Source and Drain regions, the rate of thermionic emission of mobile charge carriers from the Source region into the Channel region (which is doped of opposite conductivity type as the Source and Drain regions) increases exponentially as the height of this source injection barrier is reduced linearly with increasing $V_{GS} \equiv V_G - V_S$. When $|V_{GS}|$ is increased beyond a certain threshold voltage (V_T), transistor current flow is no longer limited by thermionic emission; an inversion layer of mobile charge (“channel”) forms at the surface of the semiconductor under the Gate electrode, allowing electric current to easily flow between the Source region and the heavily doped Drain region if $V_{DS} \neq 0$, limited by carrier drift velocity. For NMOS devices, V_G must be higher than V_S by at least V_T (i.e., $V_{GS} > V_T$) in order for an inversion layer of electrons to form at the surface of the semiconductor so that electrons can flow from the n-type Source region through the channel to the n-type Drain region. For PMOS devices, V_G must be lower than V_S by at least V_T (i.e., $V_{GS} < -V_T$) in order for an inversion layer of positively charged holes to form at the surface of the semiconductor so that holes can flow from the p-type Source region through the channel to the p-type Drain region. NMOS and PMOS FET symbols used for circuit diagrams, and their switching requirements, are also shown in **Fig. 1.1**.

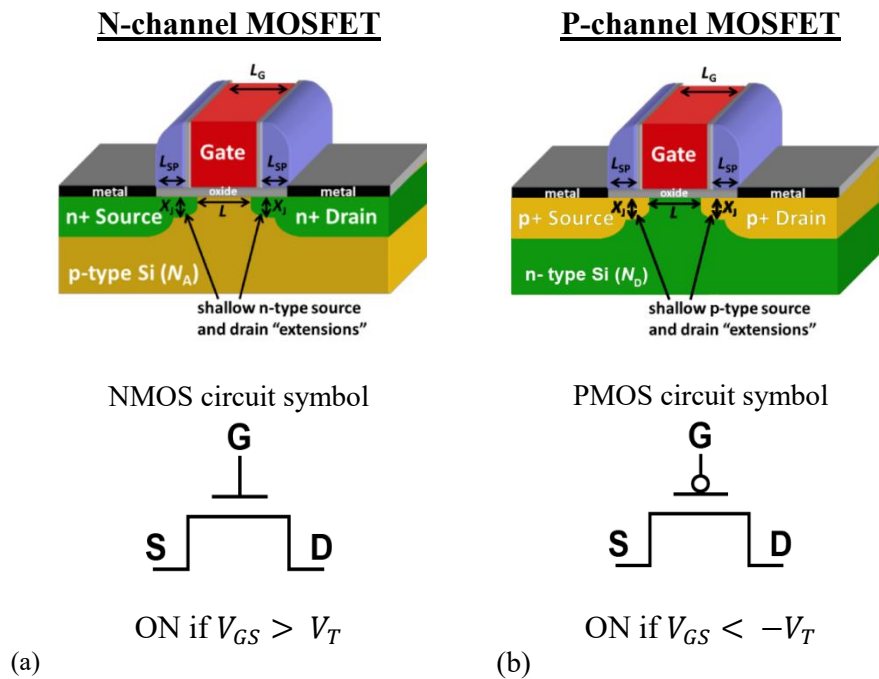


Fig. 1.1 Schematic illustrations of the structure, circuit symbol and ON state operation conditions of (a) NMOS and (b) PMOS field effect transistors. Critical dimensions are indicated: gate length (L_G), spacer length (L_{SP}), source/drain extension junction depth (X_1), and bulk dopant concentration (N_A , N_D).

NMOS and PMOS field-effect transistors are fabricated and electrically connected together to form ICs [4] that perform a variety of digital logic operations [6][7]. The simplest logic circuit is the inverter, illustrated in **Fig. 1.2**, comprising a pair of NMOS and PMOS transistors. As shown in **Fig. 1.2(a)**, the transistor Gate electrodes are connected together to form the input node, while the transistor Drain electrodes are connected together to form the output node; the NMOS Source is biased at the lowest voltage (ground, or 0 V) while the PMOS Source is biased at the highest

voltage (the power supply voltage, V_{DD}). The transistors operate in a complementary manner, *i.e.*, when one turns ON the other turns OFF, and *vice versa*: The NMOS transistor is ON when the input voltage is high (*e.g.*, V_{DD}), connecting the output node to ground; hence it is referred to as a “pull-down” device. The PMOS transistor is ON when the input voltage is low, connecting the output node to V_{DD} ; hence it is referred to as a “pull-up” device.

When the input node is charged so that the input voltage (V_{IN}) changes from 0 V to V_{DD} , the NMOS transistor turns ON while the PMOS transistor turns OFF, *i.e.*, the output node is discharged through the NMOS transistor so that the output voltage (V_{OUT}) is “pulled down” to 0 V, following the voltage transfer characteristic (**Fig. 1.2(b)**). The time required for this operation depends on the NMOS transistor ON-state “drive” current and the capacitance of the output node; the larger the drive current and/or the smaller the output node capacitance, the faster the output node discharges to ground. Similarly, the time required for V_{OUT} to transition from 0 V to V_{DD} after V_{IN} transitions from V_{DD} to 0 V depends on the PMOS transistor drive current and the capacitance of the output node.

Note that when the inverter is static (*i.e.*, not transitioning from one state to the other), one transistor is ON while the other is OFF. Moreover, the transistor that is OFF sustains a large voltage difference between the Source and Drain regions (V_{DS}), resulting in OFF-state leakage current (I_{OFF}) – which the other transistor readily allows to flow since it is ON. Therefore, power is continuously dissipated ($V_{DD} \times I_{OFF}$) when a CMOS logic circuit is static.

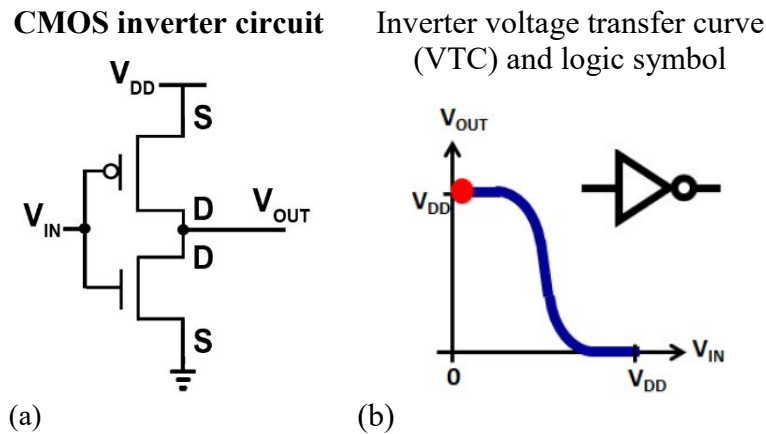
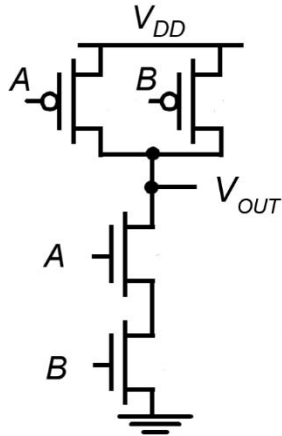


Fig. 1.2 CMOS inverter (a) circuit diagram (b) voltage transfer curve [7].

More complex logic functions are implemented with complementary pairs of NMOS and PMOS transistors that serve as pull-down and pull-up devices, respectively; hence the term “CMOS” logic technology. Examples include NAND (**Fig. 1.3(a)**) and NOR (**Fig. 1.3(b)**) digital logic gates. A static memory (SRAM) cell is implemented with two cross-coupled inverters and an additional two NMOS transistors used to pull-down their respective storage nodes during a write or read operation. A more compact but dynamic (*i.e.*, requiring periodic refreshing) memory (DRAM) cell comprises a single NMOS transistor and a capacitor to store charge (**Fig. 1.3(c-d)**) [8].

CMOS NAND gate

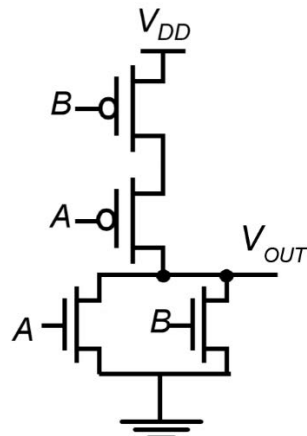


NAND Truth Table

A	B	V_{OUT}
0	0	1
0	1	1
1	0	1
1	1	0

(a)

CMOS NOR gate

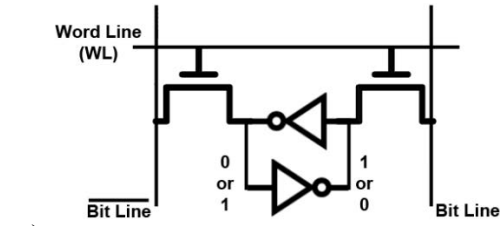


NOR Truth Table

A	B	V_{OUT}
0	0	1
0	1	0
1	0	0
1	1	0

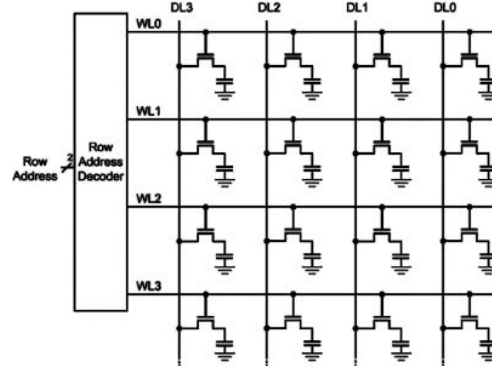
(b)

SRAM cell



(c)

DRAM cell



(d)

Fig. 1.3 CMOS logic and memory circuits (a) 2-input NAND gate (b) 2-input NOR gate and (c) Static Random Access Memory (SRAM) cell and (d) Dynamic Random Access Memory (DRAM) cell array [8]. Logic ‘1’ corresponds to high voltage; logic ‘0’ corresponds to low voltage.

1.3 CMOS ENERGY EFFICIENCY LIMIT

Traditionally, transistor miniaturization (*i.e.*, dimensional scaling) was accompanied by commensurate reduction in operating voltage (V_{DD}) to maintain a constant peak electric field (desirable for ensuring long-term reliability of transistor operation), a trend known as “Dennard Scaling” [9]. This scaling methodology provided for improved circuit operating speed at a constant chip power density. Since the 2000s, however, voltage scaling slowed down even as transistor scaling continued, because the V_T of a MOSFET cannot be scaled too close to 0 V because I_{OFF} increases exponentially (**Fig. 1.4(a)**) and hence the static power dissipation of a CMOS circuit increases exponentially with decreasing V_T . The operating speed of a CMOS circuit is dependent on transistor on-state drive current (I_{ON}), which in turn is dependent on the gate overdrive voltage ($V_{DD} - V_T$); a reduction in V_{DD} would result in smaller I_{ON} and hence slower circuit operation, if V_T cannot also be reduced.

The emergence of the “Internet of Things” in recent years has led to the need for more energy-efficient computing devices. Any CMOS-based digital logic circuit has a fundamental energy efficiency limit, however, due to non-zero transistor leakage current. This can be understood by considering the dynamic component (due to capacitive charging/discharging, proportional to the square of V_{DD}) and static component (due to transistor OFF-state leakage, proportional to V_{DD} and

also to t_{delay}) of energy consumed per operation by a generic combinational logic circuit comprising a cascade of logic gates [10]:

$$E_{\text{total}} = \alpha L_d f C V_{\text{DD}}^2 + L_d f I_{\text{OFF}} V_{\text{DD}} t_{\text{delay}} \quad (1.1)$$

$$t_{\text{delay}} = L_d f C V_{\text{DD}} / (2I_{\text{ON}}) \quad (1.2)$$

where α is the activity factor, L_d is logic depth, f is fanout, C is capacitance per logic stage, and t_{delay} is the time required to complete the logic operation.

As the time required to complete the digital operation increases (or, equivalently, circuit operating speed decreases), the energy that is wasted due to I_{OFF} increases, eventually to the point of making further reduction in V_{DD} counterproductive in terms of energy efficiency. This point corresponds to $V_{\text{DD}} = V_{\text{T}}$.

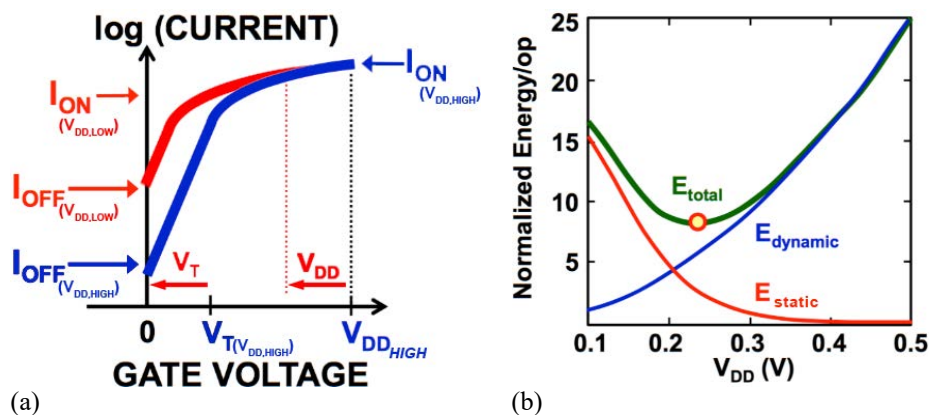


Fig. 1.4 Conceptual illustrations of (a) MOSFET transfer characteristic (for different values of V_{DD} with V_{T} adjusted to achieve the same ON-state drive current, I_{ON}) and (b) normalized energy per digital CMOS operation, showing how the total energy consumed per operation has a minimum due to transistor leakage current (I_{OFF}) [10].

In order to reduce the minimum energy per operation (*i.e.*, to improve energy efficiency), V_{T} must be reduced without increasing I_{OFF} . This means that the steepness of the transistor transfer characteristic (**Fig. 1.4(a)**) in the region where the gate voltage is smaller than the threshold voltage, *i.e.*, the “subthreshold swing” (SS) must be steeper. SS for a MOSFET is fundamentally limited to be no smaller than $\left(\frac{kT}{q}\right)(\ln 10)$, which is approximately 60 mV/decade at room temperature, due to the Boltzmann energy distribution of electrons in the Source region of the transistor [7]. For this reason, alternative solid-state switching devices have been investigated [11]. Although alternative transistor designs such as the tunnel field-effect transistor (TFET) [12] and negative capacitance FET (NC-FET) [13] can achieve steeper switching characteristics than the MOSFET, they also can be more sensitive to process-induced variations and device operating conditions, which practically limits their benefit. For example, switching abruptness can be degraded by trap-assisted tunneling due to interfacial defects in a TFET [14] and by polarization screening in a NC-FET [15].

Micro-electro-mechanical (MEM) switches (relays) can achieve immeasurably low I_{OFF} and abrupt switching behavior across a wide range of temperatures [16]; in principle, they can be operated with much lower voltage than can any type of transistor. (Although they switch more slowly than do transistors, circuit design optimization to minimize the number of mechanical switching delays per function can compensate for this [17].) Thus, MEM switches are of keen interest for digital IC applications for which energy efficiency is paramount. In this dissertation, challenges for achieving reliable millivolt relay operation are investigated. While piezoelectric MEM relays have also been studied for millivolt switching [18], this dissertation focuses on electrostatically actuated relay designs because they can be fabricated with a simpler process flow. Nevertheless, insights for achieving reliable millivolt operation of electrostatic relays should also apply for piezoelectric relays.

1.4 MEM RELAY STRUCTURE AND OPERATION

Fig. 1.5(a) shows a plan-view scanning electron microscope (SEM) image of a 6-terminal (6-T) relay developed for digital logic IC applications [19]. This device comprises a movable gate electrode suspended by four folded-flexure beams (nominal length $L = 12 \mu\text{m}$) over a fixed body electrode. As shown in the schematic cross-section of the relay in **Fig. 1.5(b)**, with nominal as-fabricated actuation air gap (g_0) of 220 nm and nominal as-fabricated contact air gap (g_d) of 60 nm in the OFF state, narrow strips of W (50 nm thick) are attached to the underside of the gate insulating layer (50 nm thick). These “channels” serve to bridge their respective S/D electrodes when the relay is in the ON state, allowing current (I_{DS}) to flow in response to a source-drain voltage difference, as also illustrated in **Fig. 1.5(b)**.

To switch ON the relay, a voltage (V_{GB}) is applied between the gate and the body, inducing electrostatic force (F_{elec}) that actuates the gate downward (**Fig. 1.6(a)**). Simultaneously, as the structure’s displacement from its equilibrium position increases, the spring restoring force F_{spring} of the deformed suspension beams increases linearly (in the opposite direction). Balancing these opposing forces, one can see that the displacement g of the structure rapidly increases with increasing V_{GB} :

$$g = g_0 - \frac{\epsilon_0 A V_{\text{GB}}^2}{2k_{\text{eff}} g^2} \quad (1.3)$$

where g_0 is the initial (as-fabricated) actuation gap, k_{eff} is the effective spring constant of the suspension beams, ϵ_0 is the vacuum permittivity, and A is the effective actuation area. If g is reduced by $\frac{1}{3}g_0$, the inherent positive feedback within this system causes the structure to become unstable and collapse downward – a phenomenon known as pull-in [20].

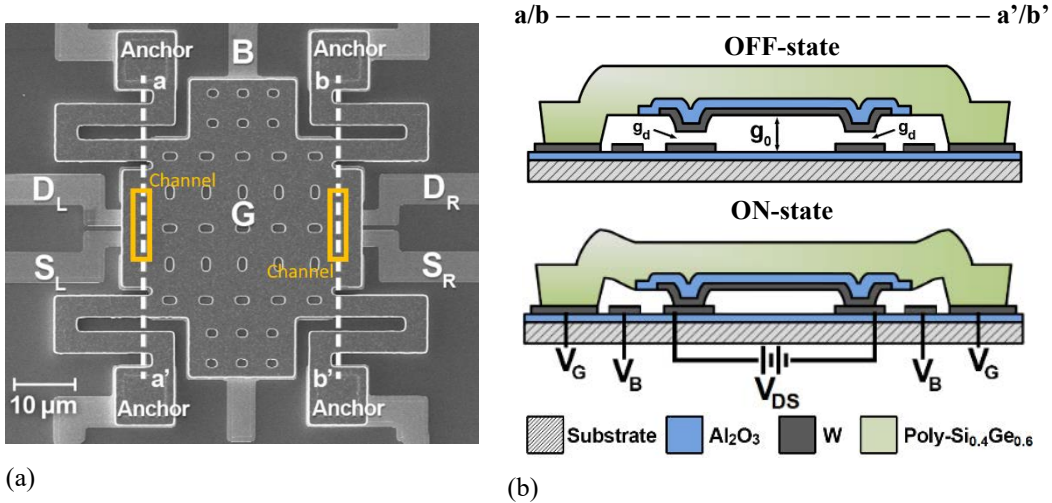


Fig. 1.5 (a) Plan-view scanning electron micrograph (SEM) image of a fabricated 6-terminal MEM relay [26] and (b) Schematic cross-section A-A' in the OFF-state and ON-state. In the ON-state, surface adhesive force exists, resulting in hysteretic switching behavior.

When the magnitude of V_{GB} is increased to be equal to or greater than that of the pull-in voltage (V_{PI}), the channels come into physical contact with their respective S/D electrodes, allowing an abrupt increase in current conduction. Subsequently when $|V_{GB}|$ is reduced below the magnitude of the release voltage (V_{RL}), the spring restoring force (F_{spring}) of the suspension beams is sufficient to overcome F_{elec} and the contact adhesive force (F_A) so that the channels are separated from their respective S/D electrodes and the relay turns off. As explained in [21], high device manufacturing yield can be achieved by designing relays to have relatively stiff structures and large air gaps as fabricated; subsequently they can be made to operate with a small gate voltage (V_G) swing by applying a body bias voltage (V_B) (**Fig. 1.6(b)**).

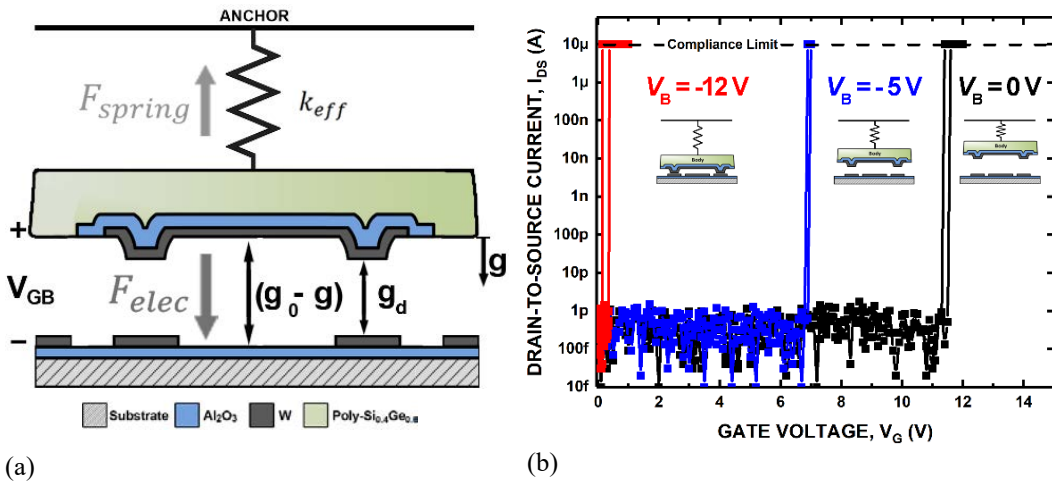


Fig. 1.6 (a) Illustration of electrostatic actuation and spring restoring forces in the MEM relay and (b) measured I - V characteristics for a relay operated with $V_{DS} = 1$ V and various body bias voltages V_B . The current is limited to be 10 μ A to avoid contact welding due to Joule heating.

It should be noted that relays can be designed to be normally off (*i.e.*, actuated into the ON state via V_{GB}) or to be normally on (*i.e.*, actuated into the OFF state via V_{GB}). Furthermore, a normally-off relay can be designed to avoid the pull-in phenomenon by making the as-fabricated contact gap smaller than $\frac{1}{3}g_0$, *i.e.*, $g_0 > 3g_d$. While previous energy-delay analyses [21-23] indicate that it is energetically favorable for relays to operate in non-pull-in mode, practical challenges (*e.g.*, variations in the fabrication process, non-zero strain gradient in the structural material) make this difficult to achieve in practice [24-26]. As such, the relays utilized in this study were designed for pull-in mode operation. Based on the aforementioned electrostatic and mechanical force-balancing with respect to V_{GB} , the formulae for V_{PI} and V_{RL} of a pull-in mode relay are as follows:

$$V_{PI} = \sqrt{\frac{8k_{eff}g_0^3}{27\epsilon_0 A}} \quad (1.4)$$

$$V_{RL} = \sqrt{\frac{2(k_{eff}g_d - F_A)(g_0 - g_d)^2}{\epsilon_0 A}} \quad (1.5)$$

where F_A is the contact surface adhesive force. Adhesive force is due primarily to van der Waals forces in the contact dimple regions in the ON state [27].

1.5 RELAY FABRICATION PROCESS

Details of the MEM relay fabrication process flow are provided in [19]. For the relays studied in this dissertation, the two sets of conducting source and drain (S/D) electrodes are coplanar with the body electrode, formed from the same layer of 50 nm-thick tungsten (W) deposited by sputter deposition (**Fig. 1.7(b)**) over the insulating substrate (**Fig. 1.7(a)**). LPCVD SiO₂ (**Fig. 1.7(c)**) was used as the sacrificial material so that the relays could be released using vapor-phase hydrofluoric acid (HF). Al₂O₃ deposited by atomic layer deposition (ALD) is used as the body (**Fig. 1.7(e)**) and substrate (**Fig. 1.7(a)**) insulator material because of its resistance to vapor-HF treatment. The structural (gate and suspension beams) material is 1.75 μm -thick *in-situ* boron doped polycrystalline silicon-germanium (poly-Si_{0.4}Ge_{0.6}) deposited by low-pressure chemical vapor deposition (LPCVD) (**Fig. 1.7(f)**). The aforementioned relay dimensions are summarized in Table 1.1.

TABLE 1.1
Nominal design parameter values for relays used in this study

Design Parameter	Value
Poly-Si _{0.4} Ge _{0.6} Thickness, t	1.75 μm
Beam Width, W	2 μm
Beam Length, L	{8, 12} μm
Actuation Area, A	1236 μm^2
Actuation Gap, g_0	220 nm
Contact Dimple Gap, g_d	60 nm
Contact Area, A_{CONT}	1 μm^2

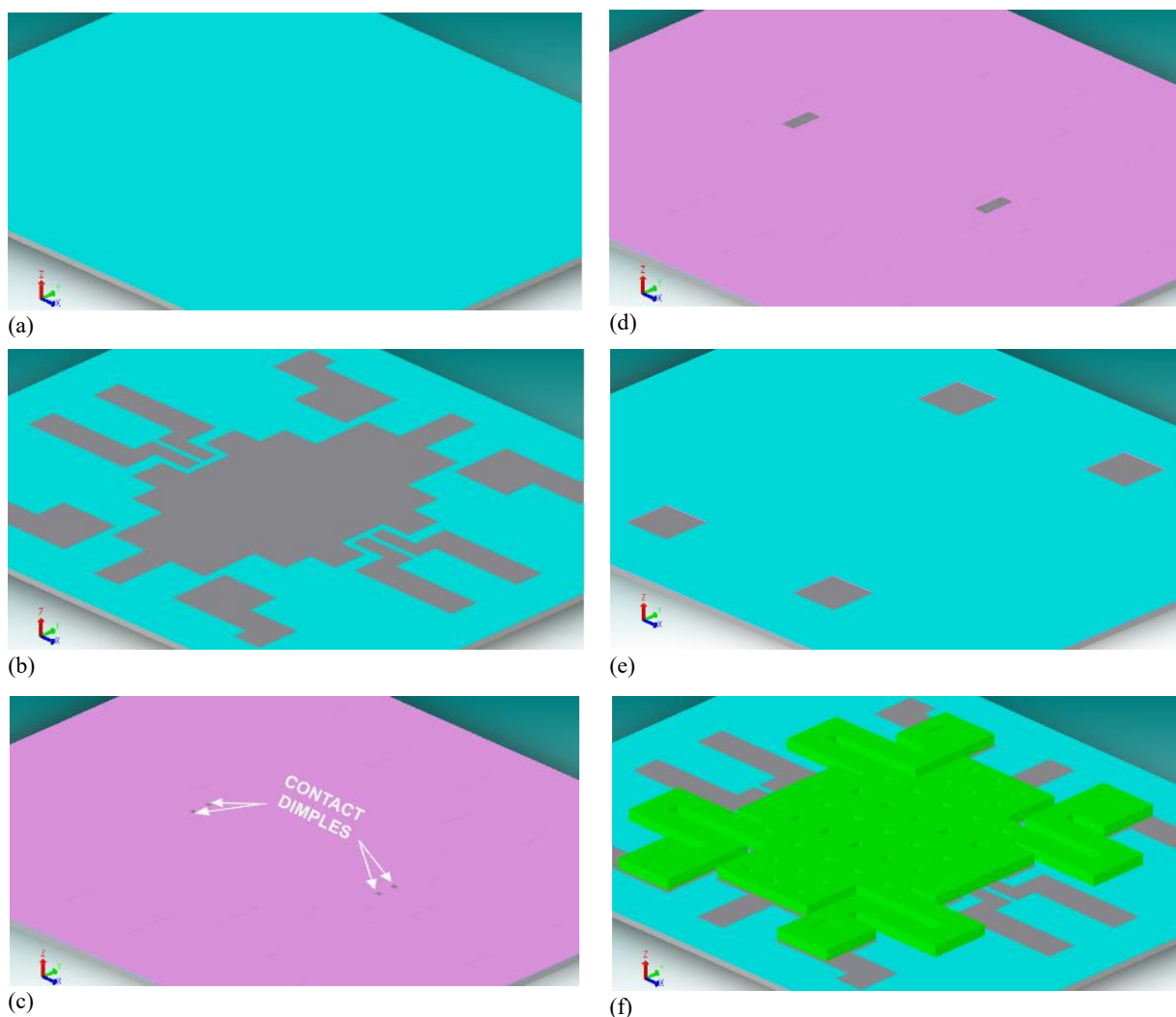


Fig. 1.7 CoventorWare MEMS+ simulated relay fabrication, showing deposition and patterning of (a) Al₂O₃ substrate dielectric, (b) W body/source/drain fixed electrodes, (c) sacrificial low temperature oxide and contact dimples, (d) W channel, (e) gate dielectric and structural anchor regions, and (f) Poly-Si_{0.4}Ge_{0.6} structure (after HF vapor release). [19]

The relays in this work were released using a uEtch Primaxx anhydrous HF vapor process, in order to avoid catastrophic pull-in and stiction due to capillary forces. The release recipe, noted in Table 1.2, consists of 15-17 cycles of stabilization, etching, and pumping; the respective durations (per cycle) of each of these steps is also shown in Table 1.2. Further information regarding this tool and etch process are available in the Marvell Nanofabrication Laboratory equipment manual [28].

TABLE 1.2.
Primaxx HF Vapor release recipe utilized in this study

	N2 (sccm)	EtOH (sccm)	HF (sccm)	Time (min)
Stabilize	1250	350	0	2
Etch	1250	350	310	5
Pump	0	0	0	0.5

In this work, MEM relays were electrically characterized using a Lakeshore TTPX cryogenic vacuum probe station at ~ 1.5 μTorr . Prior to collecting data, a native-oxide breakdown process was performed by applying 100 voltage pulses (~ 5 V, $f = 10$ kHz) between the source and drain electrodes with the relay in the ON-state, to achieve a reasonably low (less than 1 k Ω) initial ON-state resistance [10].

1.6 DISSERTATION OBJECTIVES

This dissertation discusses approaches and challenges for realizing reliable millivolt MEM relay operation for energy-efficient computing. The hysteresis voltage caused by surface adhesive force at the contact dimples during operation is the primary bottleneck for V_{DD} scaling for relay-based ICs, therefore possible methods to resolving this issue are investigated.

In chapter 2, post-fabrication treatment of the contacting electrode surfaces with a self-assembled molecular (SAM) anti-stiction coating is demonstrated to effectively reduce surface adhesive force F_A . This process is shown to enable stable sub-50 mV operation.

In chapter 3, the issue of variability in relay performance parameters over many switching cycles and from device to device is systematically studied with respect to operating conditions and contact treatment. SAM coating is found to improve switching stability for a single device and to reduce variation in hysteresis voltage from device to device.

In chapter 4, the effects of contacting electrode design and body-biased operation on relay ON-state resistance (R_{ON}) are investigated. A direct source/drain contact design provides for lowest and least variable R_{ON} . Ultra-low-voltage relay operation facilitated by body-biasing results in lower contact velocity, which mitigates the need for a wear-resistant contacting electrode material while necessitating a contacting electrode material that is not susceptible to oxidation.

Chapter 5 discusses key findings of this work and suggests possible directions of future research.

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CHAPTER 2:

Sub-50 milli-volt NEM Relay Operation Enabled by Self-Assembled Molecular Coating

2.1 INTRODUCTION

Due to the aforementioned limitations of conventional semiconductor transistors – particularly the Boltzmann distribution of electrons that is exponentially dependent on the thermal voltage $\frac{kT}{q}$, which limits the subthreshold swing (SS) of transistors to be no steeper than approximately 60 mV/dec at room temperature – nanometer-scale electro-mechanical (NEM) switches (relays) are of keen interest for ultra-low-power digital logic integrated circuit (IC) applications [1]. This is because a mechanical switch can achieve the ideal property of zero OFF-state leakage current, in turn providing for zero static power consumption [1][2]. To minimize active power consumption, the operating voltage (V_{DD}) of a digital IC should be minimized.

V_{DD} scaling for a NEM relay is limited by the switching hysteresis voltage that is caused by contact stiction [3]. When a relay is in the ON-state, surface adhesive force exists in the contact dimple regions, so that the electrostatic force required to maintain the relay in the ON-state is smaller than the electrostatic force required to actuate the relay into the ON-state. Thus, the turn-off voltage is smaller than the turn-on voltage, resulting in the aforementioned hysteresis voltage. For this reason, it is of paramount importance to investigate how to mitigate – and ultimately eliminate – surface adhesion in the relay contact regions. In this chapter, reduction in contact adhesive force via the application of an anti-stiction molecular coating is investigated.

2.2 BODY BIAS EFFECT FOR VERSATILE PASS GATE LOGIC

The 6T relays [4] in this work were tested at room temperature using a vacuum probe station (1.5 μ Torr) to minimize oxidation of the W electrode surfaces which is undesirable because WOx is electrically insulating, resulting in high ON-state resistance [5]. Measured current-vs.-voltage (I - V) characteristics for forward and reverse sweeps of the gate voltage (V_G) are shown in **Fig. 2.1(a)**. By applying a negative body voltage (V_B), the positive value of V_G that is required to turn ON the relay (V_{DD}) can be decreased to $V_{PI} - |V_B|$. The maximum value of $|V_B|$ that can be applied (while ensuring that the relay is OFF at $V_G = 0$ V) is V_{RL} , so that the minimum V_{DD} is the hysteresis voltage $V_H \equiv V_{PI} - V_{RL}$. Sub-200 mV operation with negative body biasing is demonstrated in **Fig. 2.1(b)**. In a digital logic circuit, the switching devices are used not only to pass low voltage (0 V) as in a “pull-down” device but also to pass high voltage (V_{DD}) as in a “pull-up” device. For a relay to operate as a pull-up device, it must switch ON with *decreasing* V_G . In this case, to achieve ultra-low-voltage operation, a positive body bias should be used as demonstrated in **Fig. 2.1(c)**.

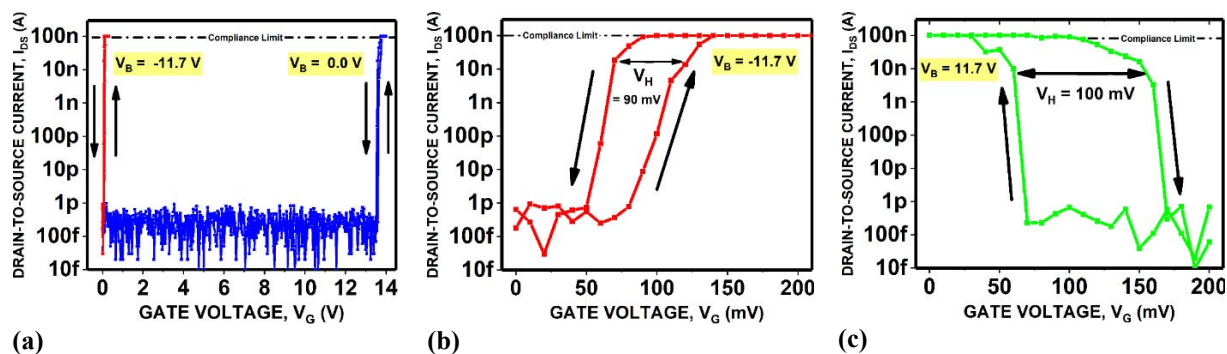


Fig. 2.1 (a) Measured relay I - V characteristics showing the effect of body-biasing, which is utilized to achieve low-voltage operation for (b) pull-down (N-relay) operation and (c) pull-up (P-relay) operation. I_{DS} is artificially limited to 100 nA in order to prevent Joule heating and subsequent W welding at the relay contacts.

Fig. 2.2(a) illustrates an inverter circuit in which the body-biased relay is used as a pull-down device, and **Fig. 2.2(b)** shows measured input and output voltage waveforms for this circuit.

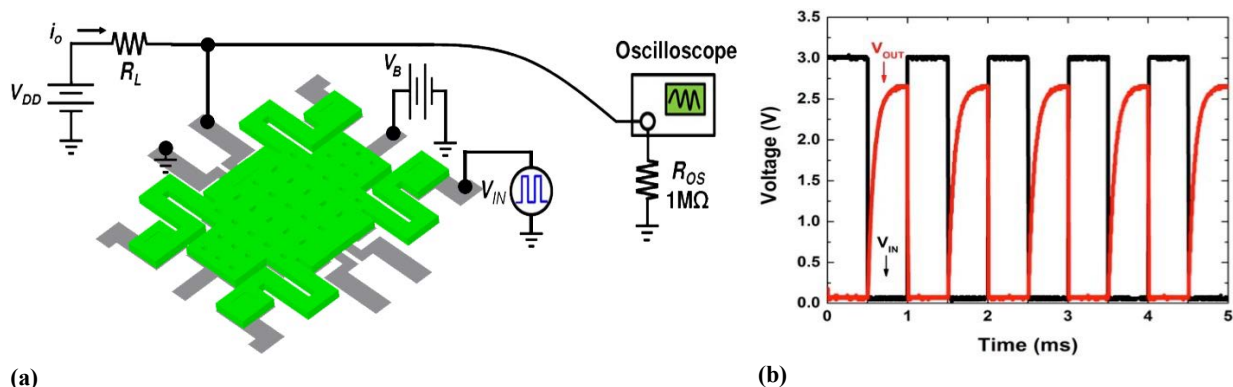


Fig. 2.2. (a) Relay inverter circuit and (b) measured voltage waveforms for inverter circuit in which a non-coated relay is configured as a pull-down device. $R_L = 123$ k Ω , $V_{DD} = V_{IN,max} = 3$ V, $V_B = -11.75$ V, and $f = 1$ kHz. (v_{OUT} does not reach V_{DD} due to oscilloscope internal resistance $R_{osc} = 1$ M Ω .)

This inverter circuit is used to extract the value of relay ON-state resistance (R_{ON}) via the voltage divider formula:

$$V_{OUT} \cong \left(\frac{R_{ON}}{R_{ON} + R_L} \right) V_{DD} \quad (2.1)$$

$$R_{ON} \cong \left(\frac{V_{OUT}}{V_{DD} - V_{OUT}} \right) R_L \quad (2.2)$$

Because the oscilloscope internal resistance ($R_{osc} = 1 \text{ M}\Omega$) is relatively large in comparison to R_{ON} , it can be considered negligible in the voltage division estimation. However, the load resistance R_L is significant compared to R_{osc} so that it cannot be ignored:

$$V_{OUT} = \begin{cases} \left(\frac{R_{osc}}{R_L + R_{osc}} \right) V_{DD} & , \text{ for } V_{IN} = 0 \text{ V} \\ \left[\frac{R_{ON} R_{osc}}{R_{ON} R_{osc} + (R_{ON} + R_{osc}) R_L} \right] V_{DD} & , \text{ for } V_{IN} = V_{DD} \end{cases} \quad (2.3)$$

$$(2.4)$$

The value of R_L affects the current flowing through the relay contacts. As such, this parameter can be tuned in order to obtain optimal circuit performance. A low value of R_L facilitates *in situ* electrical breakdown of native oxide formed on the surfaces of the contacting asperities during ON-state conduction, and reduces the effect of R_{osc} when the relay is in the OFF state. However if R_L is too low, excessive Joule heating could result in micro-welding, causing the relay to be stuck in the ON state. $R_L = 123 \text{ k}\Omega$ was chosen for the tests conducted in this chapter.

2.3 SELF-ASSEMBLED MONOLAYER (SAM) MOLECULAR COATING

Hydrophobic 1H,1H,2H,2H-Perfluorodecyltriethoxysilane (PFDTES, **Fig. 2.3(a)**) was selected as the relay coating material in this work. The silane functional group of this molecule allows its assembly onto oxidized surfaces [14] and hence facilitates self-assembly onto native WO_x on the contact surfaces (**Fig. 2.3(b)**) while the fluorinated backbone lowers the surface energy and reduces adhesive force [17-19] as shown quantitatively in **Fig. 2.7(c)**.

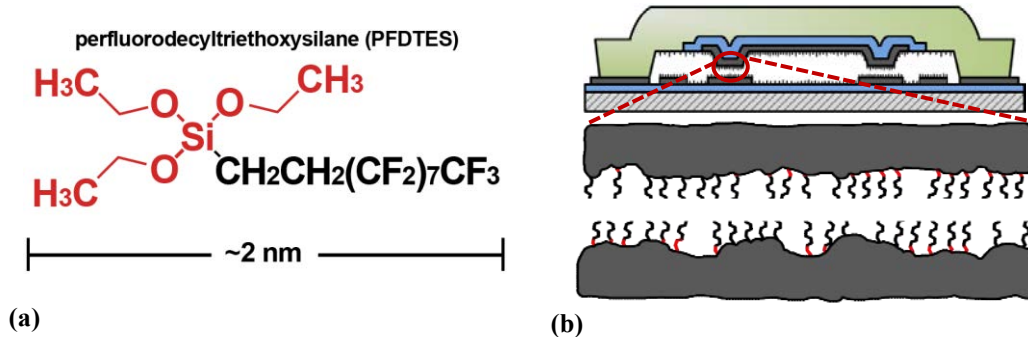


Fig. 2.3 (a) Molecular structure of PFDTES and (b) qualitative illustration of PFDTES coating, which adheres well to W surfaces due to its silane end-group.

Utilizing Atomic Force Microscopy (AFM) and the Derjaguin, Muller and Toporov (DMT) model for an adhesive contact [14, 15, 19]

$$F_{ADH} = W_{ADH} \cdot 2\pi R_{tip} \quad (2.5)$$

where W_{ADH} is the measured work of adhesion with respect to the normal plane and R_{tip} is the radius of the AFM tip, the effect of PFDTES coating was first characterized.

In this work, PFDTES was deposited using a vapor-phase process as shown in **Fig. 2.4**. A few drops of the liquid-phase molecules were placed in close proximity to the samples to be coated, inside a vacuum desiccator where the pressure was reduced to vaporize the molecules. The samples were left in this environment for ~24 hours to ensure full coverage.

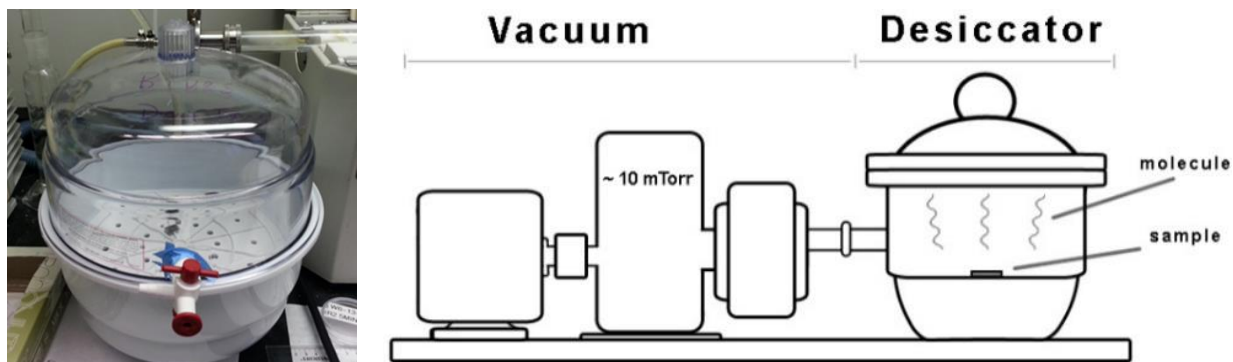


Fig. 2.4 (a) photograph and (b) qualitative illustration of the vapor phase molecular coating process, during which the molecules self-assemble onto the sample surfaces.

Contact angle measurements were conducted on samples before and after in order to confirm that the silane functional group assembled effectively. Because fluorinated molecules are hydrophobic, a drop of water on a coated surface results in a higher contact angle than a non-coated surface, as shown in **Fig. 2.5**. As such, self-assembly of PFDTES on W electrode material was confirmed.

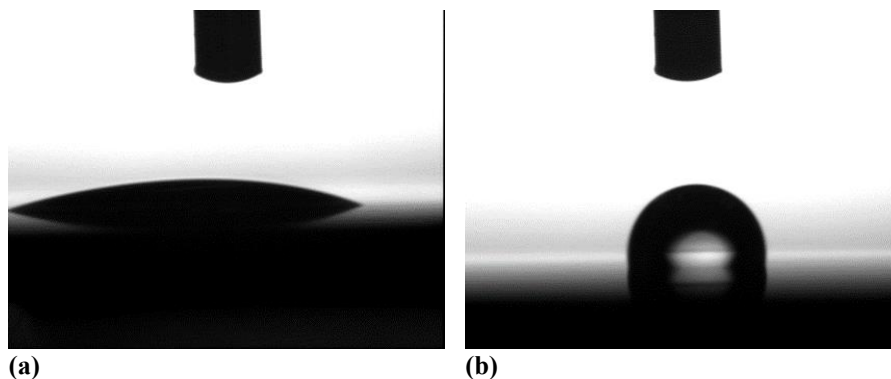


Fig. 2.5 Contact-angle measurements (a) 30° pre-coating and (b) 97° post-coating indicate successful deposition of the fluorinated molecule.

In addition, X-ray Photoelectron Spectroscopy (XPS) measurements confirm successful coating of W with PFDTES, as indicated in **Fig. 2.6**.

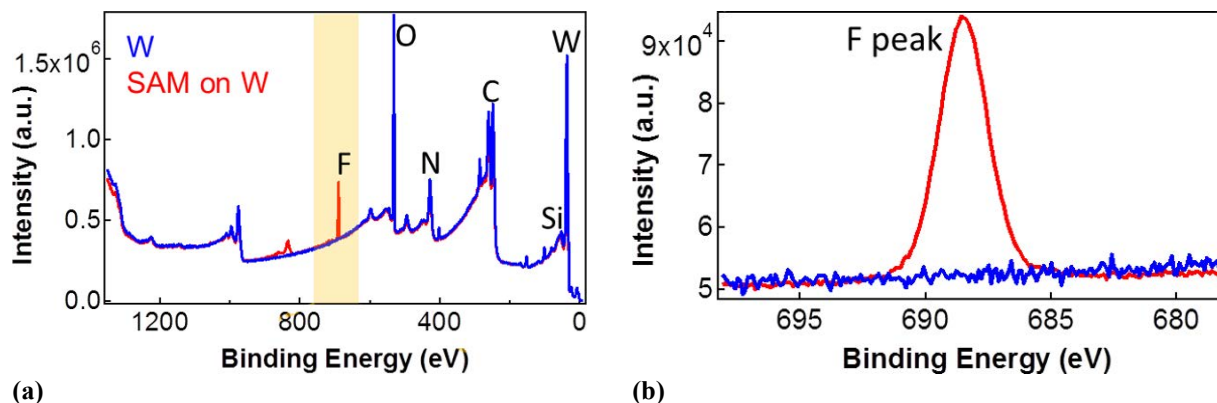


Fig. 2.6 (a) Characteristic peaks from XPS measurements and (b) the fluorine peak, indicating the successful self-assembly of PFDTES onto the W surface.

To provide reference data, a silicon-dioxide AFM tip (**Fig. 2.7(a)**) was brought into and out of contact with the surface of an oxidized silicon wafer, 10 times at each of 5 different locations on the surface for a total of 50 measurements of adhesive force [14 - 16]. This test was then conducted for a PFDTES-coated AFM tip to PFDTES-coated wafer (**Fig. 2.7(b)**). The results of these tests as shown in **Fig. 2.7(c)** indicate that PFDTES effectively decreases surface adhesive force.

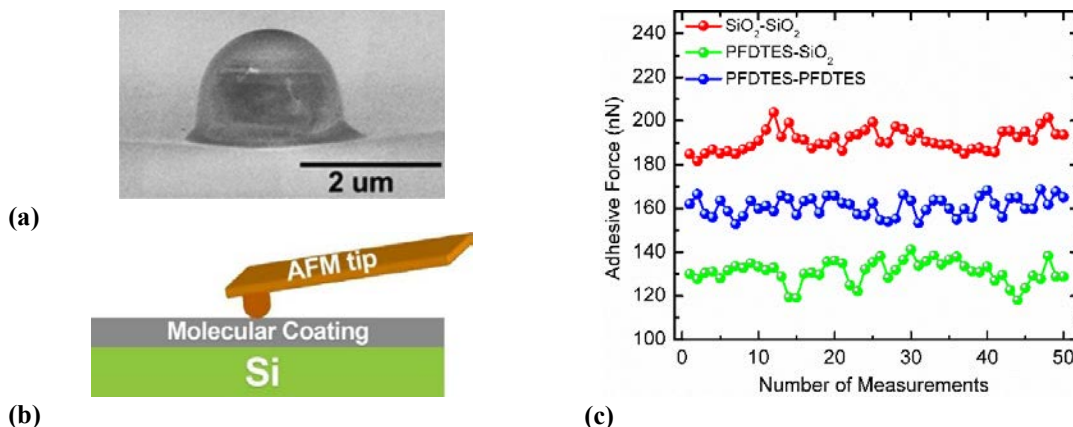


Fig. 2.7 (a) SEM image of SiO₂ AFM tip, (b) illustration of Atomic Force Microscope (AFM) adhesion force measurement and (c) empirical measurements indicating that surface adhesion is decreased with PFDTES coating.

2.4 EFFECTS OF MOLECULAR COATING ON RELAY SWITCHING CHARACTERISTICS

After initial testing, relays were coated with PFDTES using the vapor-phase growth process and then retested. For 6 relays of identical design, I_{DS} - V_G characteristics were measured multiple times (*i.e.* with multiple forward and reverse V_G sweeps) to obtain the average value of V_H . The results shown in **Fig. 2.8(a)** indicate that the PFDTES coating significantly reduces V_H , by 41% on average both for zero body bias and non-zero body bias. It also reduces V_H variation from one

device to another, from 8.3 mill-volt to 7.4 milli-volt (standard deviation) for body-biased relays. From **Fig. 2.8(b)** it is evident that relays operated with body biasing generally have lower V_H and variability due to lower contact velocity; molecular coating is as effective for reducing V_H in this case.

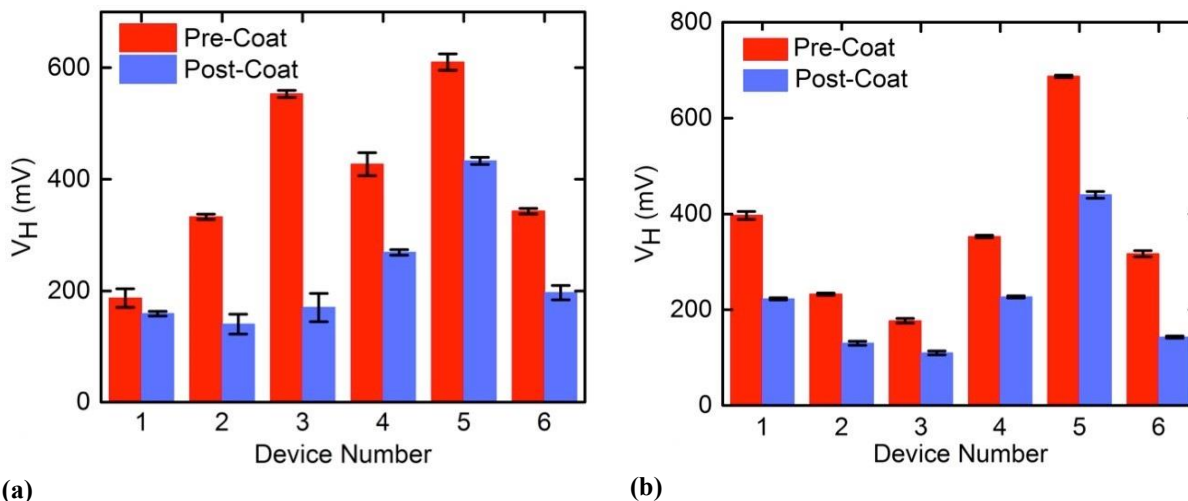


Fig. 2.8 Summary of measured data, pre- and post-PFDTES coating, showing decrease in switching hysteresis voltage V_H for (a) zero body bias, (b) $V_B = -9$ V.

Fig. 2.9 shows that the PFDTES does not substantially change the relay ON-state resistance (R_{ON}). This is likely because any PFDTES at the small number of contacting asperities (cf. Fig. 2.3(b)) is electrically broken down or ablated due to local Joule heating.

Fig. 2.10(a) shows measured I_{DS} - V_G characteristics for a coated relay with body biasing. Note that although V_H (measured at a current level of 10 nA) is reduced by the PFDTES coating, the transitions between OFF and ON states are less abrupt, *i.e.* the subthreshold swing is increased to ~ 15 mV/dec. Therefore, a larger gate voltage swing is needed to fully switch the relay ON. However, if a smaller ON/OFF current ratio (*e.g.* 10^4) is sufficient, then the coated relay can be operated

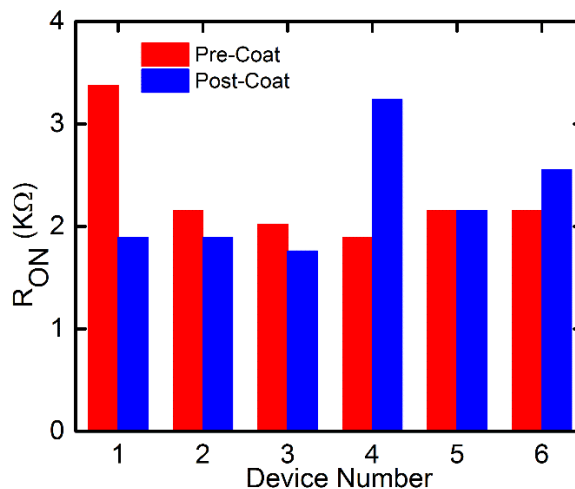


Fig. 2.9 Measured R_{ON} data for $L = 15$ μm relays operated at $V_B = -9$ V and $V_{IN} = V_{DD} = 3$ V. These data show no significant increase in relay ON-state resistance with PFDTES coating. Notably, the V_{IN} value was chosen to account for process-induced variation in V_{PI} for the given set of relays.

with a smaller gate voltage swing. This is in contrast to an abruptly switching relay, which cannot be operated with a gate voltage swing that is smaller than V_H . By applying a body bias to bring the molecular coatings on the S/D and channel electrodes into contact, a metal-molecule-metal “squitch” [17][18] is effectively achieved. The molecular material can be engineered for more abrupt switching behavior, through chemical synthesis techniques, to modify the functional end

group and/or the spacer backbone. For example, a lower Young's modulus molecular layer can be achieved by changing the spacer group.

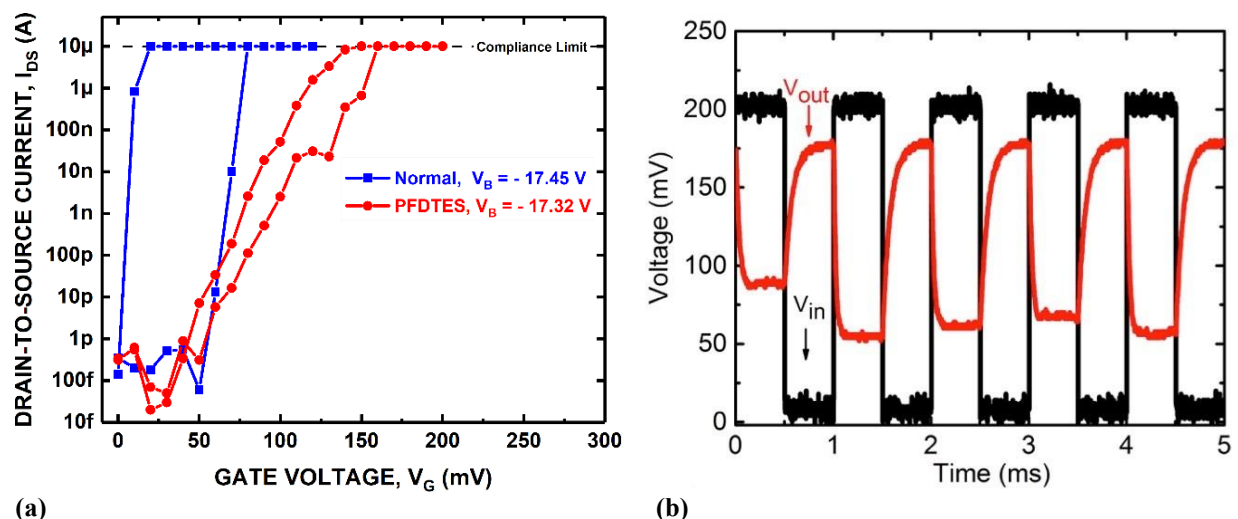


Fig. 2.10 (a) Measured $L = 8 \mu\text{m}$ relay I - V characteristics showing that PFDTES coating can provide for smaller V_H . (b) Measured voltage waveforms for inverter circuit in which a relay coated with PFDTES is configured as a pull-down device. $R_L = 123 \text{ k}\Omega$, $R_{\text{osc}} = 1 \text{ M}\Omega$, $V_{\text{DD}} = V_{\text{IN}} = 200 \text{ mV}$, $V_{\text{Bn}} = -12.34 \text{ V}$, and $f = 1 \text{ kHz}$.

Fig. 2.11 shows an example of shorter alkane molecule with Young's modulus in the GPa regime compared to longer chain poly(ethylene glycol) which exhibits a Young's modulus as low as a few MPa [17-19].

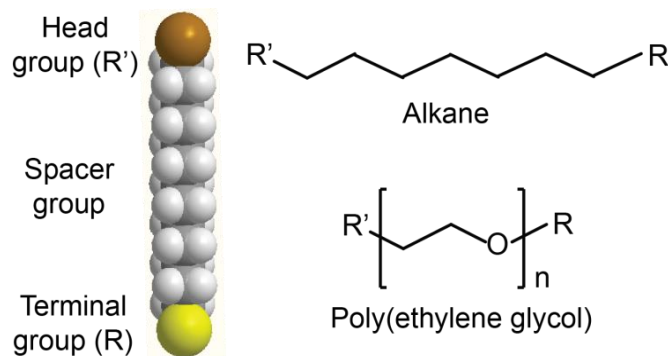


Fig. 2.11 Through chemical synthesis, molecules can be designed with particular head, terminal and spacer groups to exhibit desired surface selectivity for device functionalization, surface adhesive properties, and electromechanical performance. Here, an alkane molecule with Young's modulus in the GPa regime and poly(ethylene glycol) with Young's modulus in the MPa regime are shown as examples.

Fig. 2.12(b) shows measured voltage waveforms for an inverter circuit in which the body-biased coated relay is used as a pull-down device (cf. **Fig. 2.2(a)**). As the input voltage (V_{IN}) amplitude decreases, the relay ON state current is reduced so that it cannot fully discharge the output node

and hence the minimum output voltage ($V_{OUT,MIN}$) rises. **Fig. 2.12** shows voltage waveforms for relay-based inverter circuits, demonstrating sub-50 milli-volt operation ($V_{IN} = V_{DD}$).

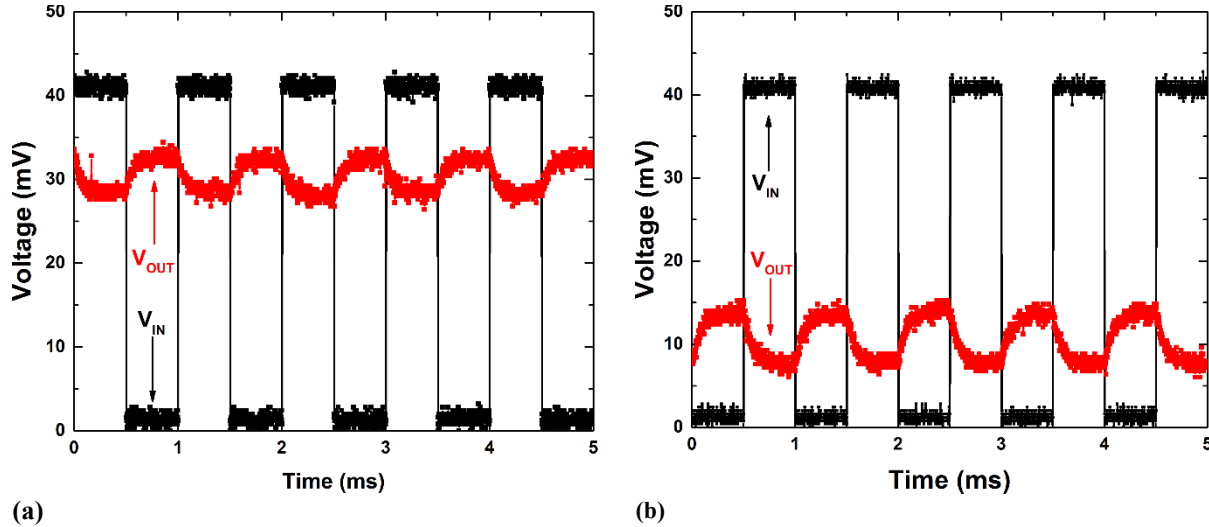


Fig. 2.12 Measured voltage waveforms demonstrating sub-50 mV relay-based inverter circuit operation: (a) N-relay configuration with $V_{Bn} = -14.96$ V, and (b) P-relay configuration with $V_{Bp} = 14.1$ V. $R_L = 123$ k Ω , $R_{osc} = 1$ M Ω , $V_{DD} = V_{IN} = 40$ mV, and $f = 1$ kHz.

2.5 DISCUSSION

The experimental results show that PFOTES is effective for reducing surface adhesion and hence V_H , thereby enabling reliable sub-50 milli-volt relay operation for both pull-up and pull-down operation (cf. **Fig. 2.12**). This comes at the tradeoff of reduced switching abruptness, however, resulting in degraded ON/OFF ratio for the same (small) gate-voltage swing. Effectively, R_{ON} for low- V_{DD} operation is increased, resulting in significantly degraded output voltage swing. This issue is exacerbated by the softer contacting force for body-biased operation [6-8]. For $V_{DD} = V_{IN} = 40$ mV, the pull-down and pull-up relays have effective $R_{ON_{N-relay}} \approx 369$ k Ω and $R_{ON_{P-relay}} \approx 205$ k Ω , respectively.

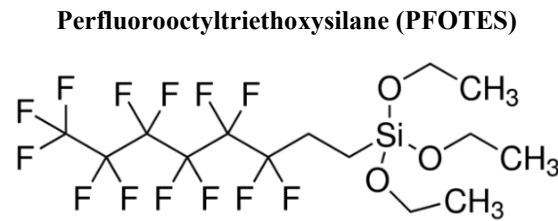


Fig. 2.13 Molecular structure of PFOTES

Alternative fluorinated molecules, such as perfluorooctyltriethoxysilane (PFOTES, **Fig. 2.13**), could be used as anti-stiction coating material [11]. The quantity n of difluoromethane (CF_2) within

the larger fluorinated chain affects the overall length of the molecule. Measurements of PFOTES-coated relays indicate that the shorter molecule ($n = 5$) results in lower surface adhesive force (Fig. 2.14 (a)) and smaller V_H (Fig. 2.14 (b)) in comparison with PFDTES.

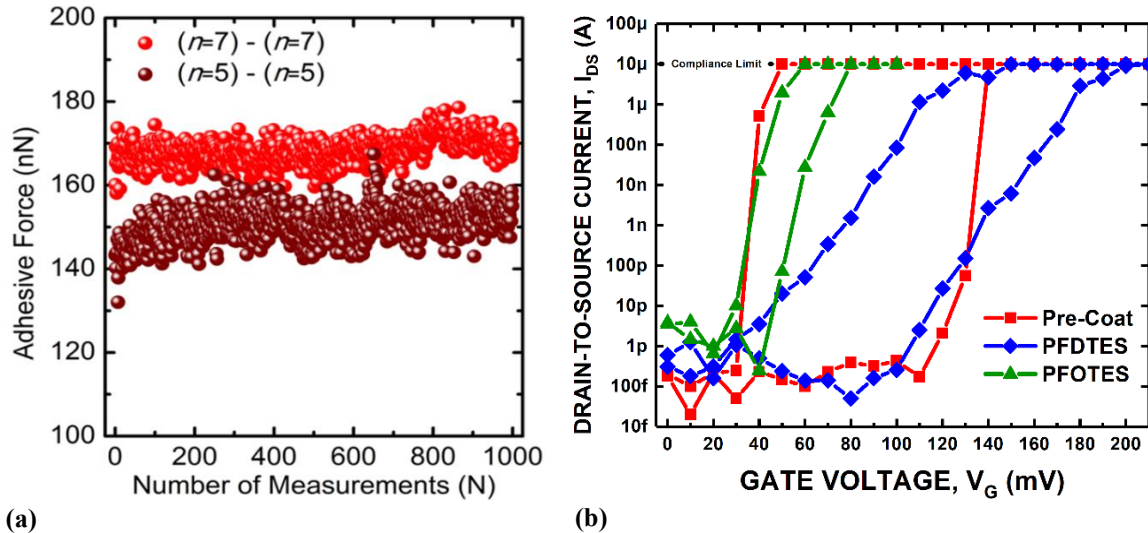


Fig. 2.14 (a) AFM-based measurements of coated contact adhesive force and (b) measured relay I - V characteristics, comparing the effects of PFOTES and PFDTES anti-stiction coatings.

2.6 SUMMARY

Reduction of the hysteresis voltage V_H is key to minimizing the gate voltage swing of a relay and thereby the active power consumption of relay-based digital ICs. Self-assembled monolayer PFDTES coating is found to be effective for reducing V_H (by more than 41%) without significantly affecting ON-state resistance, enabling lower voltage operation. Further work is needed to optimize the molecular coating material to achieve more abrupt switching behavior, to fully realize the benefit of lower V_H for lower the operating voltage and hence for improving MEM relay operating energy efficiency.

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CHAPTER 3:

Variability Study for Low-Voltage Micro-Electro-Mechanical Relay Operation

3.1 INTRODUCTION

In order to overcome the inherent switching energy efficiency limitation of conventional transistors [1], there have been many efforts to develop alternative solid-state switch designs that can achieve more ideal (*i.e.*, abrupt) switching characteristics [2-6]. Micro/nano-electro-mechanical (M/NEM) switches are a promising alternative to conventional transistors for applications in which energy efficiency is paramount, primarily because the former can achieve immeasurably low OFF-state leakage current (I_{OFF}) and abrupt switching behavior across a wide range of temperatures [7]. In principle, NEM relays can be operated with much lower voltage than can any type of transistor. (Although they switch more slowly than do transistors, circuit design optimization to minimize the number of mechanical switching delays per function can compensate for this [8].) A body-biased MEM relay design was previously developed for digital IC applications [9] and shown to provide for improved energy efficiency [10].

In Chapter 2, an anti-stiction self-assembled monolayer (SAM) coating was demonstrated to reduce the relay switching hysteresis voltage ($V_H \equiv V_{PI} - V_{RL}$) so that the relay can be switched ON/OFF with sub-50 milli-volt gate voltage (V_G) swing; therefore, in principle, the operating voltage (V_{DD}) of a relay-based integrated circuit (IC) can be less than 50 mV. However, due to variations in turn-on/pull-in voltage (V_{PI}) and release voltage (V_{RL}) values from device to device, V_{DD} must include voltage margin for these variations. In this chapter, variability in relay switching voltages and the impact of SAM coating on variability are investigated.

3.2 RELAY SWITCHING VOLTAGE VARIABILITY

Switching voltage variations practically limit the extent to which V_{DD} can be reduced, because in practice a single negative value of V_B should be used for all of the “pull-down” relays within a circuit block, while another single positive value of V_B should be used for all of the “pull-up” relays within a circuit block. In order for a relay-based IC to operate properly, then, the magnitude of the applied body bias voltage ($|V_B|$) cannot be larger than the minimum value of release voltage ($V_{RL\ low}$), to guarantee that each relay turns OFF properly; also, V_{DD} must be at least equal to the maximum value of V_{PI} ($V_{PI\ high}$) minus $V_{RL\ low}$, to guarantee that each relay turns ON properly. Therefore, V_{DD} scaling is constrained by the maximum and minimum values of V_{PI} and V_{RL} , respectively:

$$V_{DD} \geq V_{PI\ high} + V_B \quad (3.1)$$

$$|V_B| \leq V_{RL\ low} \quad (3.2)$$

3.2.1. Body-biased switching voltage stability

Process-induced variations in relay dimensions, as well as random variations in F_A from device to device and over the device operating lifetime, result in switching voltage variations. **Fig. 3.1** shows measured switching voltages for 100 sequential DC measurements made on a single body-biased relay.

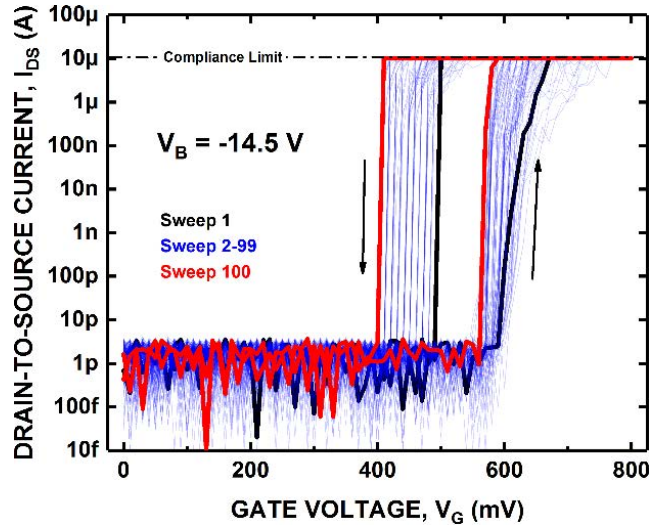


Fig. 3.1 Stable low voltage operation is enabled by body-biasing, with less than 100 mV variation in V_{PI} and V_{RL} over 100 gate voltage sweeps. The ON-state current was artificially limited to 10 μA , to prevent excessive Joule heating resulting in micro-welding. $L = 8\ \mu\text{m}$.

The plotted data in **Fig. 3.2** show that V_{PI} is very stable after the first ~ 20 sweeps, while V_H increases slightly (by ~ 20 mV) over time, possibly due to initial contact wear-in, stabilizing after ~ 50 sweeps. Weak dependence on the drain-to-source voltage (V_{DS}) is seen. The relays in this work were tested at room temperature under vacuum (~ 1.5 μ Torr).

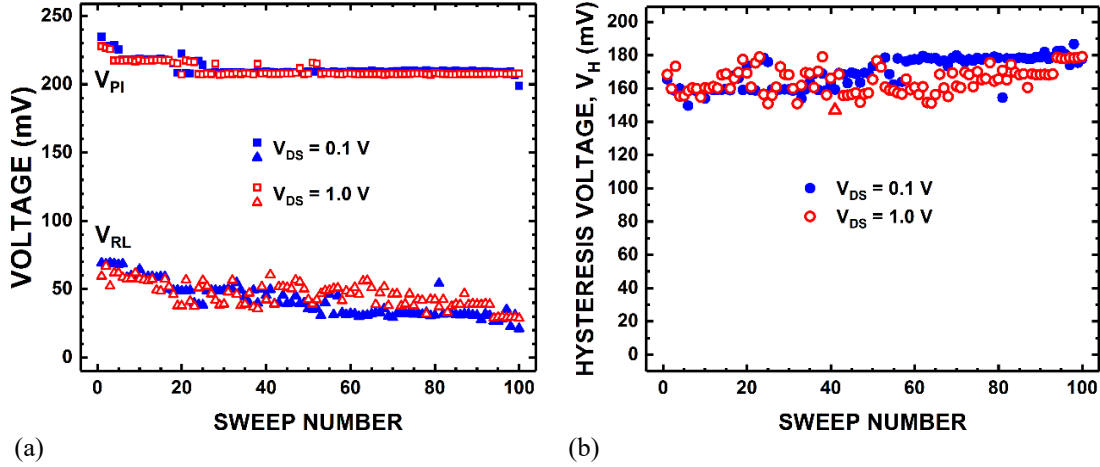


Fig. 3.2 Evolution of (a) relay switching voltages and (b) hysteresis voltage for a body-biased relay operated with various values of drain-to-source voltage V_{DS} . $L = 8$ μ m. The current compliance limit was set to 10 μ A.

Fig. 3.3 shows that body biasing is generally advantageous for improving switching voltage stability (i.e., reducing variability in V_{PI} and V_H). This is likely due to the reduction in impact velocity enabled by increased $|V_B|$ [10].

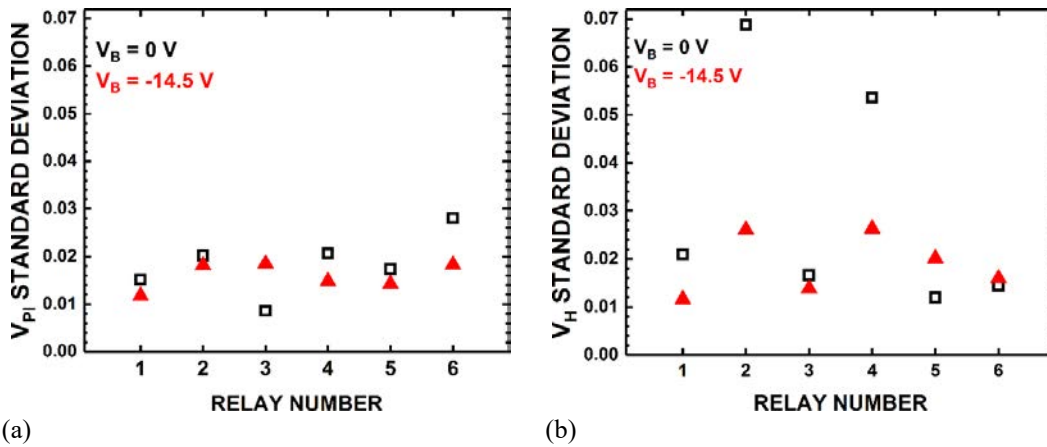


Fig. 3.3 Measured variability in (a) V_{PI} and (b) V_H for multiple relays operated at $V_{DS} = 1$ V with $V_B = 0$ V or $V_B = -14.5$ V. Body biasing generally decreases variability in V_{PI} and V_H . $L = 8$ μ m. The current compliance limit was set to 10 μ A.

3.2.2. Process-induced variations

The LPCVD processes used to deposit the sacrificial SiO_2 and structural poly- $\text{Si}_{0.4}\text{Ge}_{0.6}$ layers in this work resulted in significant systematic variations across a wafer (*i.e.*, die to die) and random variations from device to device, in the thicknesses of the actuation and contact gaps and the movable structure, as determined using an Olympus LEXT OLS4000 3D confocal laser microscope. Notably, the structural thickness of these relays was $1.6 \mu\text{m}$, as opposed to the nominal thickness listed in Table 1.1.

Fig. 3.4(a) shows how V_{PI} varies with poly- $\text{Si}_{0.4}\text{Ge}_{0.6}$ thickness. Utilizing Eqn. 1.4 and noting that $k_{eff} \propto t^3$, the theoretical change in V_{PI} relative to its nominal value due to a change in poly- $\text{Si}_{0.4}\text{Ge}_{0.6}$ thickness t and actuation gap g thickness is given by the following relationship:

$$V_{PI} = \left(\frac{g * t}{g_0 * t_0} \right)^{3/2} * V_{PI_0} \quad (3.3)$$

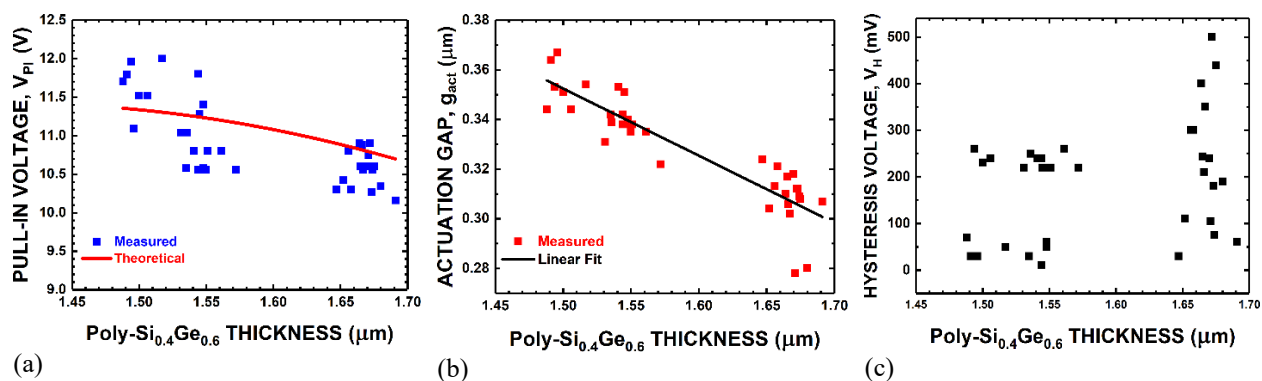


Fig. 3.4 Measured impact of process-induced variations in Poly- $\text{Si}_{0.4}\text{Ge}_{0.6}$ thickness on (a) pull in voltage V_{PI} (b) actuation gap g and (c) hysteresis voltage V_H . $L = 12 \mu\text{m}$. The negative correlation between structural layer thickness and actuation gap size is due to reduced out-of-plane deflection for a stiffer structure.

By comparing the measured V_{PI} values against the theoretically predicted trend based on Eqn. 3.3, indicated by the solid red line in **Fig. 3.4(a)**, taking into account the negative correlation between structural layer thickness and actuation gap size shown in **Fig. 3.4(b)**, it can be seen that random sources of variation are predominant. (Measured values $g_0 = 0.35 \mu\text{m}$, $t_0 = 1.5 \mu\text{m}$, and $V_{PI_0} = 11.9 \text{ V}$ were used to calibrate the theoretical curve.) The systematic variation is relatively small and can be further reduced in a relatively straightforward manner with improved LPCVD process control. **Fig. 3.4(c)** shows that there is significant random variation in V_H , which depends on local contact properties that vary from device to device.

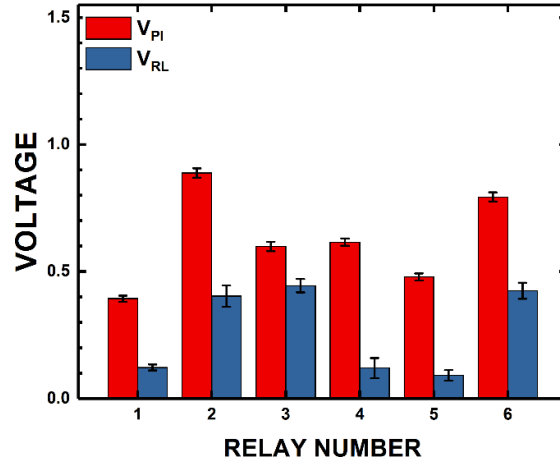


Fig. 3.5 Measured switching voltages for multiple relays operated at $V_{DS} = 1$ V and $V_B = -14.5$ V. The error bars correspond to switching variation measured for each relay over 100 gate voltage sweeps. $L = 8$ μm .

Fig. 3.5 shows the variation in switching voltages for relays located side-by-side on a single die, with the same value of V_B that was chosen to guarantee proper IC functionality. Although V_H can be less than 100 mV, random variability limits V_{DD} to be no less than ~ 0.9 V for this die. More uniform (device to device) switching voltages are necessary to overcome this issue, to fully realize the benefit of relay technology for ultra-low-voltage integrated circuits.

3.4 EFFECTS OF ANTI-STICTION COATING

In the previous chapter it was demonstrated that a hydrophobic coating of Perfluorodecyltriethoxysilane (PFDTES) is effective for reducing V_H , but at a tradeoff of increased sub-threshold swing, *i.e.* less abrupt switching behavior [11]. As seen in **Fig. 3.6**, a molecular coating with a shorter perfluoro chain, Perfluorooctyltriethoxysilane (PFOTES), was used in this work to mitigate the aforementioned tradeoff (cf. Sec. 2.5).

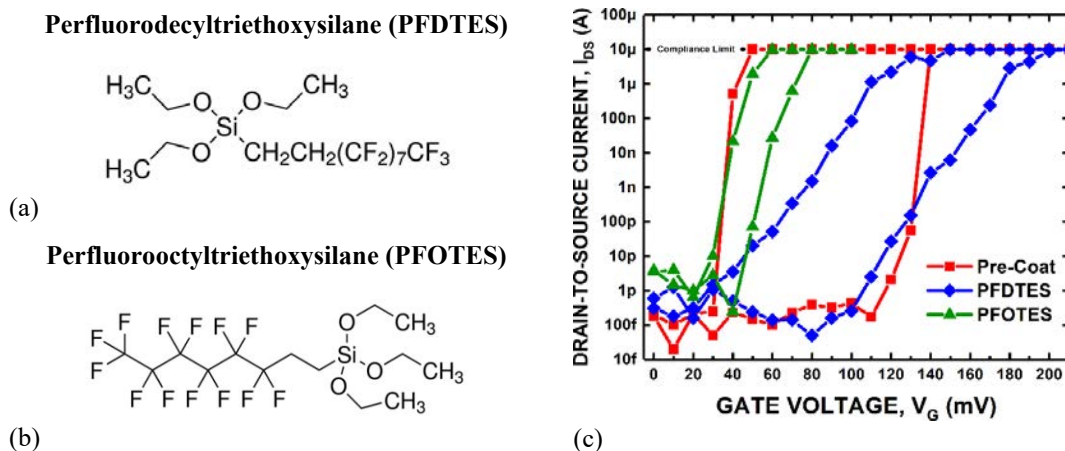


Fig. 3.6 Molecular structure of (a) PFDTES vs. (b) PFOTES, (c) measured I - V characteristics for body-biased relays, showing the effects of anti-stiction coatings. $L = 12$ μm .

As can be seen from **Fig. 3.6(c)**, a PFOTES-coated relay can be fully switched between ON and OFF states with sub-50 mill-volt V_G swing. **Fig. 3.7** shows that low V_H is stably maintained with PFOTES coating over many switching cycles.

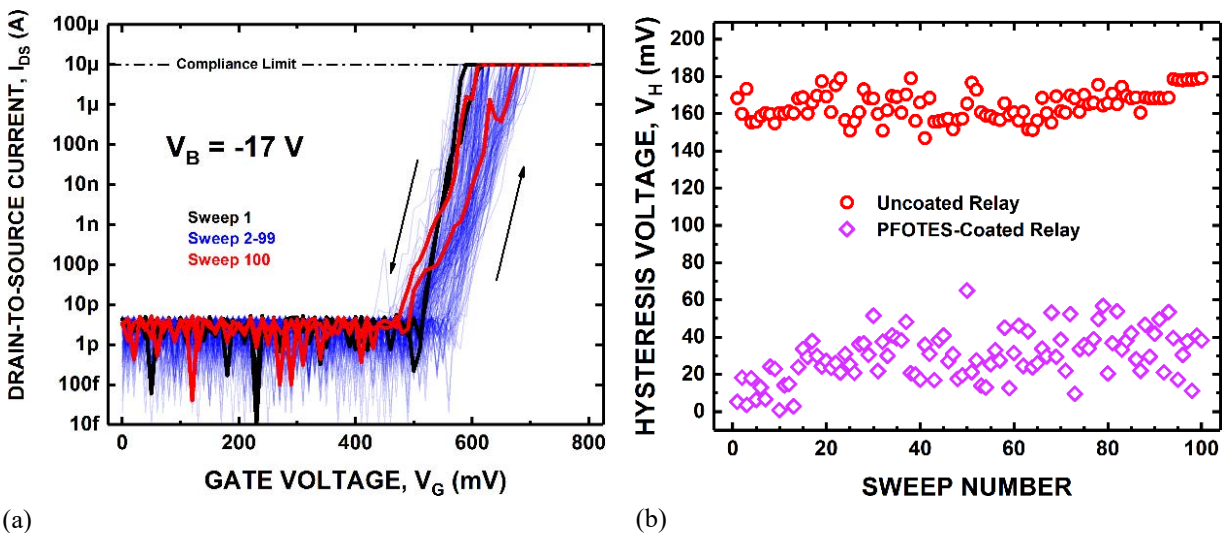


Fig. 3.7 (a) Measured I - V characteristics and (b) evolution of measured V_H for PFOTES-coated MEM relay operated over 100 gate voltage sweeps at $V_{DS} = 1$ V and body-biased conditions. These data indicate significantly decreased value and variability in V_H due to the PFOTES coating. $L = 8$ μm.

The data in **Fig. 3.8(a)** affirm that relay switching voltage stability is improved with the anti-stiction coating. **Fig. 3.8(b)** shows that device to device variation in V_H is also significantly improved, indicative of more uniform contact stiction for the coated relays.

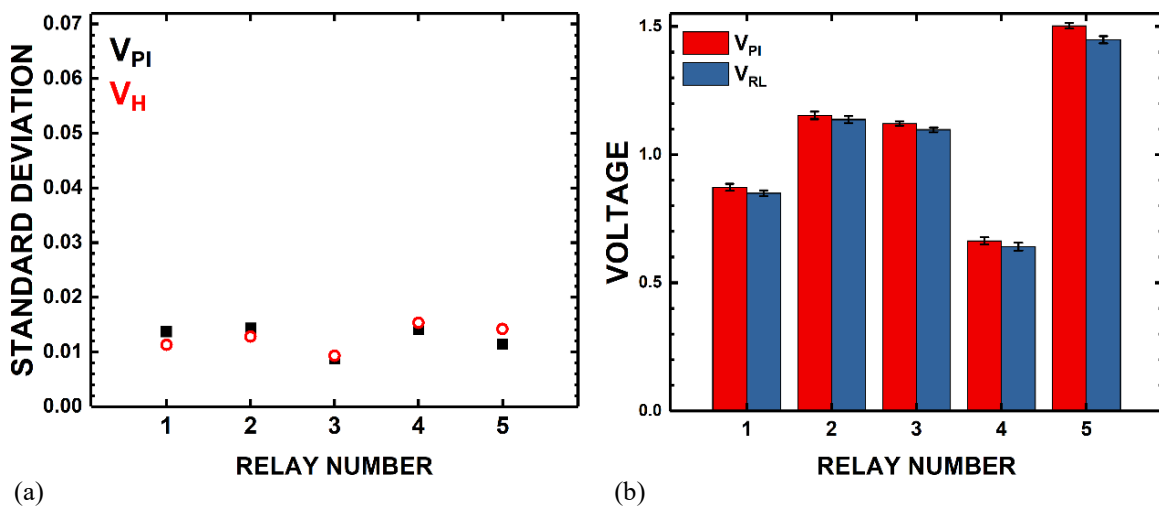


Fig. 3.8 Measured (a) variability in V_{PI} , V_H and (b) switching voltages for multiple PFOTES relays operated at $V_{DS} = 1$ V, $V_B = -16$ V. $L = 8$ μm.

3.5 DISCUSSION

The results of this study indicate that process-induced random variations in V_{PI} will practically limit V_{DD} reduction for relay-based ICs. Because the microstructure of the LPCVD poly-Si_{0.4}Ge_{0.6} structural film is highly non-uniform [13], out-of-plane deflection due to non-zero strain gradient is significant and varies from device to device, resulting in large random variation in V_{PI} as seen in **Fig. 3.4**. This issue can be mitigated by using a much thicker (stiffer) poly-Si_{0.4}Ge_{0.6} film, but at a trade-off of a much larger gate-to-body voltage required to turn on the relay, *i.e.*, larger $|V_B|$. Alternatively, a structural film with zero strain gradient could be developed. For instance, multi-target DC magnetron sputtering has been demonstrated to effectively and controllably grow amorphous metal thin films [14, 15].

3.6 SUMMARY

Variability and stability of relay switching voltages practically limits reductions in operating voltage for relay-based integrated circuits and hence was investigated in this work. Tight control ($\pm 1\%$) of the structural layer thickness and the actuation and contact gap thicknesses is necessary to reduce random variability and thereby enable sub-100 milli-volt relay IC operation. In this regard, a structural layer material with low residual stress and an amorphous microstructure may be necessary to minimize random out-of-plane deflection. An optimized anti-stiction coating is effective for reducing hysteresis and random variation thereof, and hence is expected to facilitate the practical implementation of sub-100 milli-volt relay-based circuits.

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CHAPTER 4:

Study of MEM relay contact design and body-bias effects on ON-state resistance stability

4.1 INTRODUCTION

In Chapter 3, an anti-stiction self-assembled monolayer coating was demonstrated to reduce variation in the hysteresis voltage (V_H), thereby facilitating implementation of millivolt integrated circuits with MEM relays. Another basic requirement for MEM relay technology to be practical for digital computing applications is adequate device reliability. Previous work has shown that the primary failure mode of a MEM relay is increased ON-state resistance (R_{ON}) due to contact oxidation [1][2]. Nevertheless, a MEM relay can operate with low and stable R_{ON} over many switching cycles [3]. This chapter discusses the effects of contact design and operating parameters – including supply voltage and body-bias voltage – on MEM relay R_{ON} stability.

4.2 RELAY DESIGN AND OPERATION

The original body-biased logic relay design comprised a single bridge-contact design [4]. To reduce the device count and hence the area required to implement a relay-based digital IC, a more functional design comprises two pairs of S/D electrodes, as shown in **Fig. 4.1(a)** [5]. Y.-H. Yoon *et al.* pointed out that the bridge contact design is not optimal, however, because an imbalance in contact force between the source and drain electrodes can result in significantly increased ON-state resistance [6]. This issue can be circumvented by adding an extra patterning step in the relay fabrication process to form vias for the patterned conductive “channel” electrode layer underneath the gate electrode to contact (and thereby serve to extend) the source electrodes, to allow direct physical contact between a pair of source and drain electrodes, as shown in **Fig. 4.1(b)** [7].

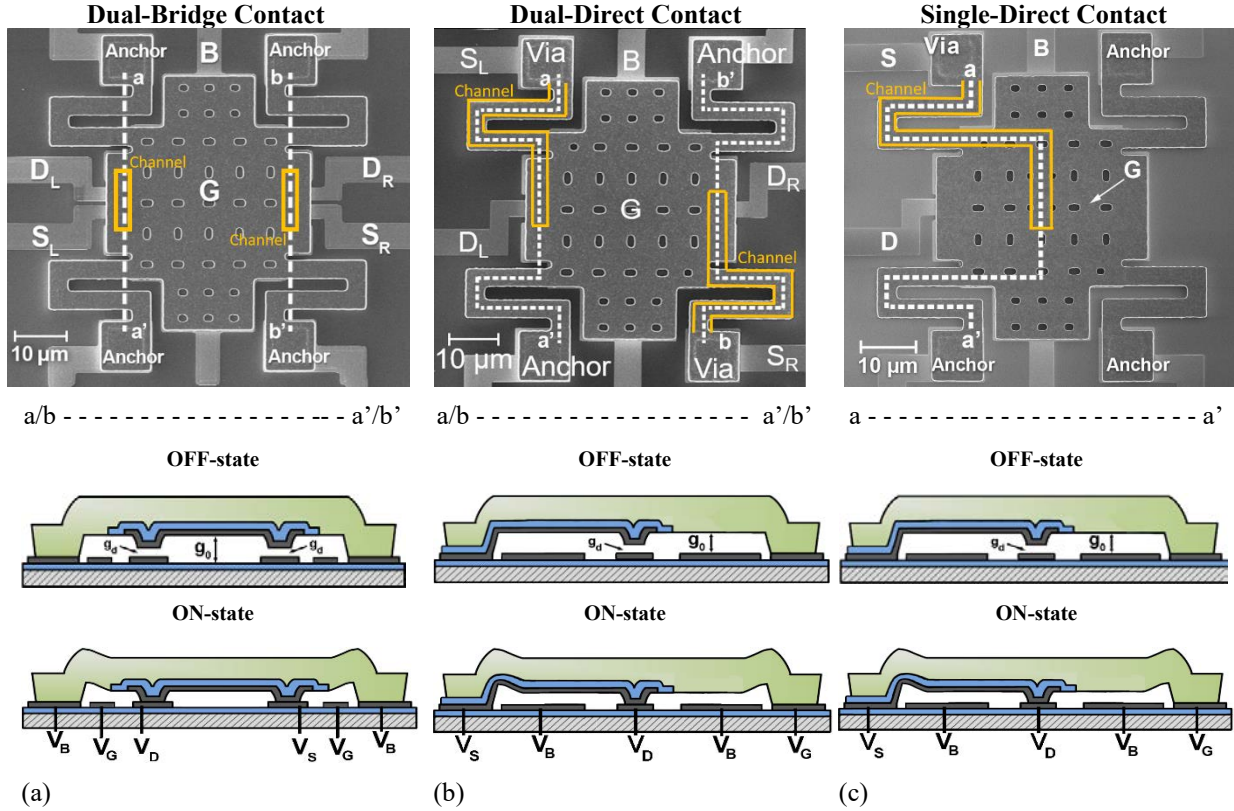


Fig. 4.1 SEM micrograph images (top) and schematic cross-sections (bottom) of relays with different contacting electrode designs in the OFF state and in the ON state: (a) dual bridge source/drain contact [8], (b) dual direct source/drain contact [7], and (c) single direct source/drain contact.

Typical measured body-biased relay current vs. gate voltage (I - V) characteristics are plotted for the different relay designs in **Fig. 4.2**. The greater the number of contacting regions, the greater the apparent contact area and F_A , resulting in larger hysteresis voltage ($V_H \equiv V_{PI} - V_{RL}$), which sets a lower limit for V_{DD} . In this work, a single direct S/D contact relay design (**Fig. 4.1(c)**) was included because it provides for smaller contact adhesive force and hence less hysteresis, as can be seen from Fig. 4.2.

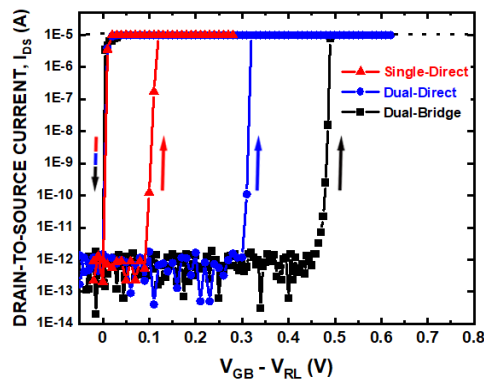


Fig. 4.2 Measured I - V characteristics for body-biased ($V_B \approx -11.4$ V) relays of various contact designs. The current I_{DS} is artificially limited to $10 \mu\text{A}$ in order to avoid micro-welding caused by Joule heating in the ON state.

4.3 RELAY FABRICATION PROCESS

The relay fabrication process is described in detail in [5] for the bridge-contact relay design and in [7] for the direct-contact relay design, and hence is only briefly summarized herein. The Al_2O_3 insulating layers for the substrate and gate were deposited by atomic layer deposition (ALD) at 300°C and plasma enhanced ALD at 250°C , respectively; the fixed electrode material (used to form the body, source and drain electrodes) is tungsten (W) deposited by sputtering; the structural material (used for the gate electrode and suspension beams) is polycrystalline silicon-germanium (poly- $\text{Si}_{0.4}\text{Ge}_{0.6}$) deposited by low-pressure chemical vapor deposition (LPCVD) at 410°C . The air gaps in the actuation region and contacting regions were formed by selectively removing sacrificial layers of SiO_2 (deposited by LPCVD at 400°C), to “release” the structure for movement. Nominal film and air gap thicknesses are listed in Table 4.1. The release process was performed using the uEtch Primaxx anhydrous HF vapor tool available in the Marvell Nanofabrication Laboratory, in order to prevent stiction due to capillary forces (c.f. Sec. 1.5). It should be noted that, due to non-zero strain gradient in the poly- $\text{Si}_{0.4}\text{Ge}_{0.6}$ film [9], out-of-plane deflection upon release caused the as-fabricated air-gap thicknesses to increase by ~ 100 nm [8], so that g_d is greater than $g_0/3$; hence the relays operate in pull-in mode [10].

TABLE 4.1
Process parameter values for relays used in this study

Design Parameter	Symbol	Value		
Poly- $\text{Si}_{0.4}\text{Ge}_{0.6}$ Thickness	t	1.9 μm		
Suspension Beam Width	W	2 μm		
Suspension Beam Length	L	12 μm		
Actuation Gap Thickness (nominal)	g_0	220 nm		
Contact Gap Thickness (nominal)	g_d	60 nm		
		<i>Single-Direct</i>	<i>Dual-Direct</i>	<i>Dual-Bridge</i>
Actuation Area	A	1000 μm^2	1062 μm^2	1032 μm^2
Total Contact Dimple Area	A_{CONT}	1 μm^2	2 μm^2	4 μm^2

4.4 COMPARISON OF RELAY CONTACT DESIGN

The relays in this work were measured in a Lakeshore TTPX cryogenic vacuum probe station at ~ 1.5 μTorr and room temperature. The hysteresis voltage was measured from static I - V curves obtained using a Keithley 4200 parameter analyzer, at a current level of 10 μA . The statistical data in **Fig. 4.3(a)** indicate that the hysteresis voltage roughly scales with total apparent contact area; this is because the contact adhesive force is predominantly due to van der Waals forces [10].

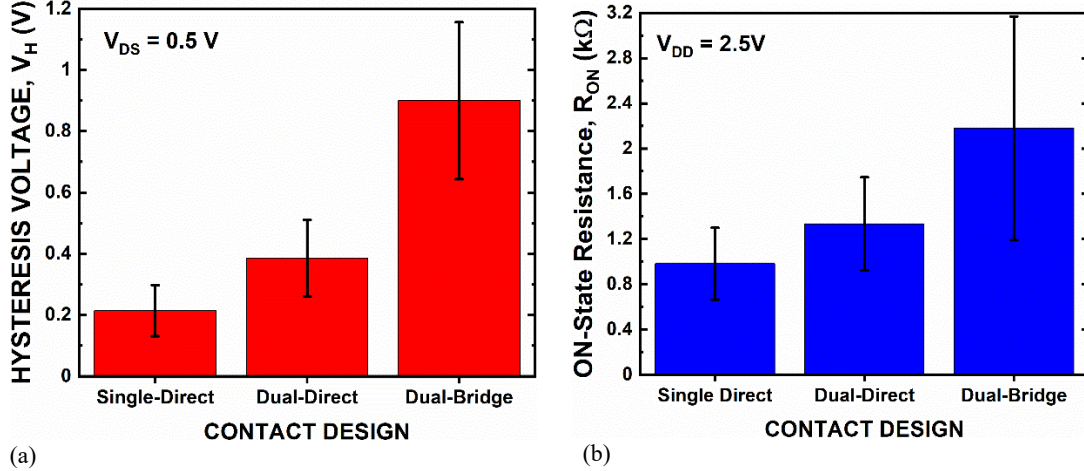


Fig. 4.3 Average measured values of (a) V_H and (b) R_{ON} for 10 relays of each contact design with $V_B = 0$ V. The bars indicate the ranges of standard deviation.

R_{ON} was determined from dynamic measurements of the output voltage (V_{OUT}) of a relay-based inverter circuit illustrated in **Fig. 4.4**, using Eq. 4.1 derived from the voltage-divider equation for the relay in the ON state (c.f. Sec 2.2).

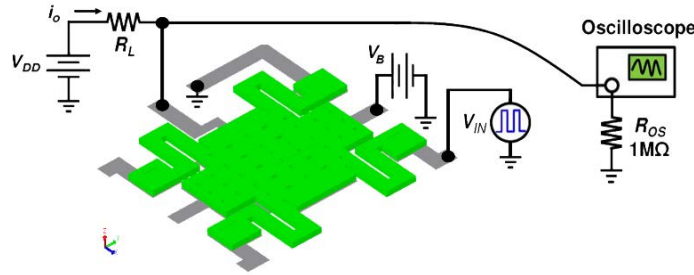


Fig. 4.4 Relay-based inverter circuit utilized for R_{ON} characterization.

$$R_{ON} \cong \left(\frac{V_{OUT}}{V_{DD} - V_{OUT}} \right) R_L \quad (4.1)$$

The statistical data in **Fig. 4.3(b)** indicate that R_{ON} improves with decreasing number of contact regions. This can be explained by the higher average contact force with decreasing number of contacting regions [2]. The greater R_{ON} variability for the bridge-contact design is related to the aforementioned issue of imbalance in contact force between the source and drain electrodes, which varies from device to device [8][9]. To enable the lowest possible operating voltage (*i.e.*, gate voltage swing), and for lowest R_{ON} , the single-direct contact design is optimal.

Fig. 4.5 shows how R_{ON} varies over many ON/OFF switching cycles, for single-direct, dual-direct and dual-bridge relay contact designs. Each design shows stable operation for at least 10^4 cycles, with the single-direct contact design exhibiting the best long-term R_{ON} stability.

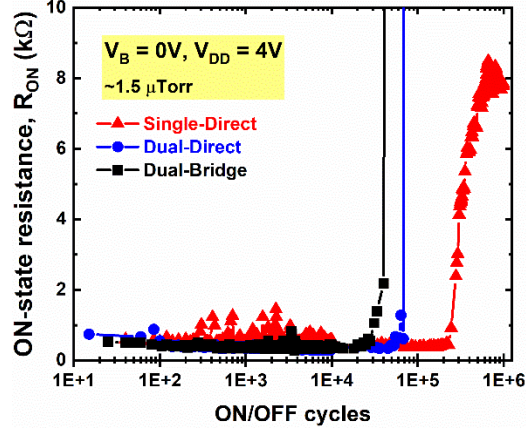


Fig. 4.5 Measured R_{ON} as a function of the number of ON/OFF switching cycles, for MEM relays switched at a frequency $f = 10$ kHz with peak $V_{IN} = 13$ V.

4.5 EFFECTS OF SUPPLY VOLTAGE SCALING AND BODY BIASING

As the gate voltage swing required to switch a relay ON/OFF is reduced, the operating voltage (V_{DD}) of a relay-based digital logic IC also can be reduced, since the maximum voltage that needs to be “passed” from the source to the drain to drive the gate(s) of the relays in the next logic stage can be reduced. **Fig. 4.6(a)** plots R_{ON} stability for a single-direct-contact relay operated with different values of V_{DD} . The data indicate that R_{ON} is significantly larger (although still well within the desired range below 10 k Ω [1]) for a smaller value of V_{DD} . This trend is likely due to the need for *in-situ* breakdown of native oxide on the W contacting electrode surfaces to maintain low contact resistance, a process which slows down exponentially with decreasing voltage [11].

Fig. 4.6(b) compares R_{ON} stability for a single-direct-contact relay operated with large gate voltage swing (with zero body bias) vs. a small gate voltage swing (with large negative body bias), for the same value of V_{DD} . The data show that smaller gate voltage swing makes the device more susceptible to the effect of contact electrode surface oxidation. This is because mechanical strain makes it easier to break down a thin oxide [13].

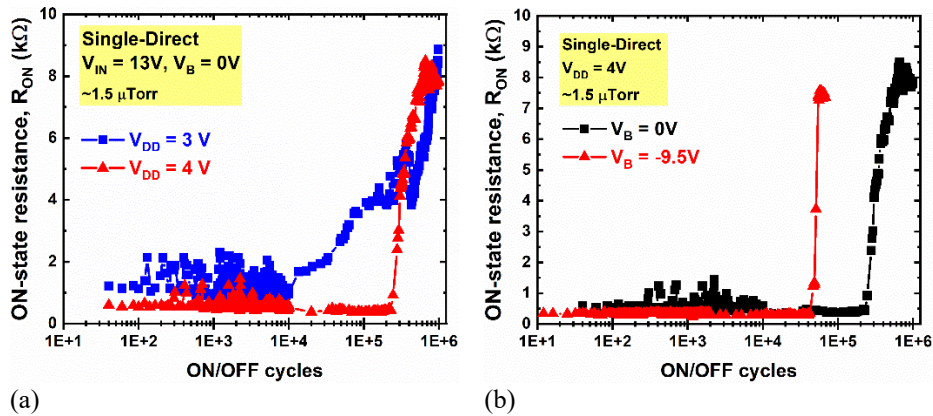


Fig. 4.6 Measured R_{ON} as a function of the number of ON/OFF switching cycles, for a single-direct contact relay switched at a frequency $f = 10$ kHz: (a) with $V_B = 0$ V and different values of V_{DD} , (b) with $V_{DD} = 4$ V and different values of V_B . The body-biased data in (b) are plotted for 6.75×10^4 hot switching cycles, after which the relay failed due to micro-welding.

The dynamic behavior of the MEM relay is governed by the following force-balance equation:

$$mg'' + bg' + k_{eff}g = \frac{\epsilon AV_{GB}^2}{2(g_0 - g)} \quad (4.2)$$

where m is the mass of the movable poly-Si_{0.4}Ge_{0.6} structure, b is the damping coefficient, and g is the displacement.

Fig. 4.7(a) plots simulated values of contact velocity as a function of body bias voltage, for a fixed value of overdrive voltage ($V_{OD} \equiv V_{GB} - V_{PI}$). It can be seen that the contact velocity decreases rapidly with increasing magnitude of V_B . Since oxide breakdown is facilitated by mechanical strain [13] this can explain the experimental results in Fig. 4.6(b). Qualitatively, a body bias actuates the gate electrode downward, *i.e.*, it reduces the air-gap thicknesses in the OFF state; therefore, the structure has a shorter distance to travel between OFF and ON states, so it does not reach as high a velocity before physical contact is made. **Fig. 4.7(b)** shows how the contact velocity can be increased by increasing the overdrive voltage, to (partially) compensate for the decrease in contact velocity with body biasing; this would come at the cost of increased relay switching energy, however.

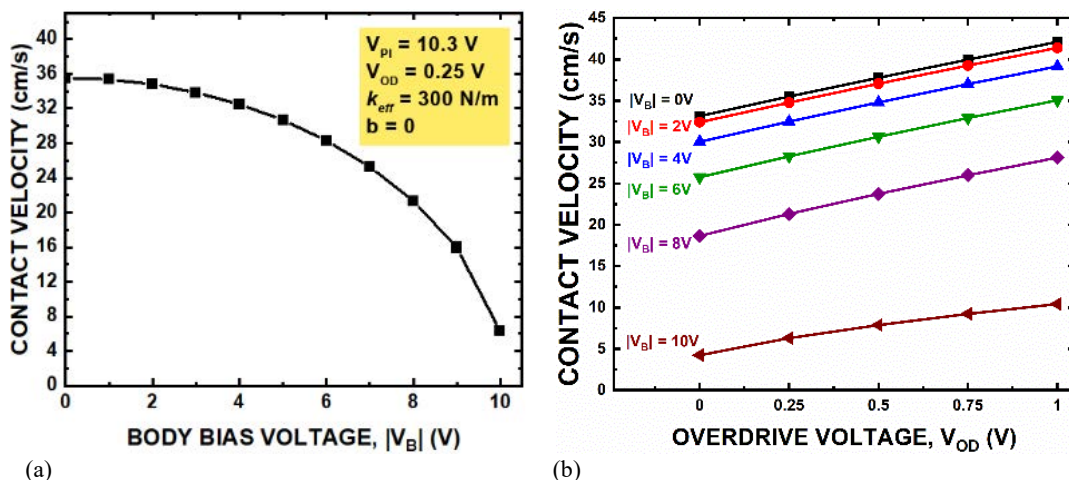


Fig. 4.7 Numerically (MATLAB) simulated relay contact velocity under varying (a) V_B and (b) V_{OD} operating conditions for a single-direct-contact relay design (cf. Table I). The damping coefficient b is assumed to be 0, *i.e.* operation in vacuum. MATLAB script for this analysis is available in the Appendix section.

4.6 DISCUSSION

The experimental findings in this work show that contact design significantly affects the ON-state resistance stability of MEM relays. For optimal results, the number of contact regions should be minimized to provide for not only the smallest hysteresis voltage but also the smallest R_{ON} . Body biasing to lower the gate voltage swing results in lower contact velocity so that the relay is less resilient to contact electrode surface oxidation; as a result, a rapid increase in R_{ON} occurs sooner.

The issue of contact oxidation resulting in increased R_{ON} is a challenge for implementing ultra-low-voltage relay-based digital logic ICs that operate reliably over many clock cycles, because it will not be possible to electrically breakdown native oxide formed on the contacting electrode surfaces *in situ* with ultra-low values of drain-to-source voltage. Approaches to address this issue include packaging to ensure inert ambient operating conditions (*e.g.*, N_2 or high vacuum), and the use of an alternative contacting electrode material that either has an electrically conductive oxide or that does not oxidize.

4.7 SUMMARY

The direct-contact source-drain electrode design is shown to be advantageous for achieving MEMS relays with low hysteresis voltage and low ON-state resistance. While body biasing allows for smaller gate voltage swing, it also increases susceptibility to the effects of contact surface oxidation. A reduction in relay operating voltage necessitates a non-oxidizing ambient or an alternative contacting electrode material such as Gold or Ruthenium [14] to overcome the issue of contact oxidation resulting in unacceptably high R_{ON} .

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CHAPTER 5:

Conclusions and Future Work

5.1 SUMMARY OF RESEARCH CONTRIBUTIONS

This dissertation has examined approaches and challenges for realizing reliable millivolt MEM relay operation for energy-efficient computing. Since the minimum gate voltage swing required to switch a relay ON/OFF is limited by the switching hysteresis voltage V_H [1] that arises from contact adhesive force, anti-stiction coating was first investigated. Perfluorodecyltriethoxysilane (PFDTES), a fluorinated molecule that can be easily coated onto exposed relay surfaces as a self-assembled monolayer (SAM), was found to be effective for reducing surface adhesive force and hence V_H , thereby enabling sub-50 milli-volt switching operation [2]. This improvement in V_H comes at the expense of degraded subthreshold swing since the SAM coating is electrically insulating and has non-zero mechanical stiffness, resulting in lower ON-state current for ultra-low-voltage operation. Alternative anti-stiction molecules can be chosen, with different quantities n of difluoromethane (CF_2) [3] or other organic configurations [4], to optimize this tradeoff.

A digital integrated circuit (IC) comprises multiple switching devices that should have stable and uniform performance characteristics to ensure that the circuit functions reliably. Therefore, the issue of stability (over time) and variability in relay switching voltages (from device to device) was investigated next. V_H was measured for relays over many DC gate voltage sweeps (hot switching cycles, with the value of V_{DS} fixed), for various values of V_{DS} and body-bias voltage V_B . The value of V_{DS} was found to have negligible impact, while body biasing (to reduce the gate voltage swing for switching operation) was found to reduce variation in relay switching voltages over many ON/OFF cycles. Anti-stiction SAM coating with perfluorooctyltriethoxysilane (PFOTES, $n = 5$) was found to be beneficial for reducing temporal variation as well device-to-device variation in V_H [3]. The primary source of device-to-device variation in relay switching

voltages – which ultimately will limit voltage scaling for relay-based ICs – is the non-zero strain gradient in the polycrystalline $\text{Si}_{0.4}\text{Ge}_{0.6}$ structural material [5].

ON-state resistance (R_{ON}) is another relay performance characteristic that must be stable and uniform to ensure proper IC operation. Therefore the effects of source/drain contact design and body biasing on R_{ON} were investigated. Contact structure design was found to significantly affect not only the value of R_{ON} but also its stability and variability. The number of contact dimple regions should be minimized to provide the lowest values and variability not only for V_{H} but also for R_{ON} , as this minimizes the contact dimple area and maximizes contact pressure [6][7]. A single direct-contact relay design is shown to achieve the most stable R_{ON} over 10^6 inverter circuit operating cycles. Body biasing provides for desirably lower R_{ON} but makes a relay more susceptible to contact electrode oxidation due to reduced contact velocity.

5.2 SUGGESTIONS FOR FUTURE WORK

Further work is needed to identify alternative SAM coatings that can mitigate the trade-off between smaller V_{H} for lower power consumption and higher I_{ON} for faster circuit operation. For instance, the length of the anti-stiction molecule chain can be tuned [4]. Additionally, the endurance of SAM coatings can be studied in more detail, to determine whether they are practical for long-term reliability of relay-based ICs.

Since non-zero strain gradient in the poly- $\text{Si}_{0.4}\text{Ge}_{0.6}$ structural film alters the actuation and contact gap thicknesses in a non-uniform manner, resulting in device-to-device variation in relay switching voltages, it ultimately limits V_{DD} scaling for a relay-based IC. Therefore, alternative structural materials should be investigated. For instance, an amorphous metal would eliminate the strain gradient caused by grain boundaries [8]. Laterally actuated relay designs could be investigated for better control of gap thicknesses as fabricated [9][10].

Ultra-low-voltage operation of a relay results in lower contact velocity [11]. Therefore, it would be worthwhile to reconsider softer and less reactive metals – *e.g.*, Gold (Au) or Platinum (Pt) [12] – as possible contact materials.

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APPENDIX

The following MATLAB script numerically computes MEM relay motion consistent with Eq. 4.2. The nominal design parameters are used to estimate the pull-in voltage in accordance with H. Kam *et al.* Given this pull-in voltage, the dynamic behavior of a MEM relay is analyzed with respect to varying body-bias voltage (VB) and overdrive voltage (V_{OD}) values. Each of the latter parameters affect initial system conditions, thereby affecting the values of mechanical turn-ON delay (tdelay) and contact velocity (cont_v).

```
%Solving for impact velocity for a given VB and V_OD initial input.
%Developed in collaboration with U. Sikder

clear all; close all; clc;
tic

%Material properties
rho=2300;          %Poly-SiGe density (kg/m^3)
E=160e9;          %Poly-SiGe Young's Modulus (kg/m/s^2)
G=79.6e9;         %Poly-SiGe Shear Modulus (kg/m/s^2)
eps0=8.854e-12;   %permittivity of free space (F/m)

%Design properties
h=1.9e-6;         %Poly-SiGe structural thickness (m)
W=2e-6;          %width of beams (m)
Lb=24e-6;        %length of the beams (m)
g0=220e-9;       %initial actuation gap (m)
gd=60e-9;        %contact dimple gap (m), also the max displacement

A = 1.112e-9;     %Area of poly-SiGe structure (m^2)
A_SD = 1.000e-9; %G-B overlap, single-direct actuation area (m^2)
A_DD = 1.062e-9; %G-B overlap, dual-direct actuation area (m^2)
A_DB = 1.032e-9; %G-B overlap, dual-bridge actuation area (m^2)

%k_eff estimation via H. Kam (TED 2011)
gammaf=3.66;      % (m^-2)
gammata=1.341e10; % (m^-2)
kflex=gammaf*E*W*(h^3)/(Lb^3); %flexural component
kctor=gammata*G*W*(h^3)/(Lb); %torsional component
keff=1/(1/kflex+1/kctor); %effective spring constant k_eff (N/m)

%Assume mass of beams and truss negligible compared to that of structure
m = A*h*rho; %mass = A * h * density, for the structure.

b = 0; %effective damping constant under vacuum, approx. 0 (kg/s)

V_OD = [0:0.25:1]; %Set relative values of V_OD to be simulated

% Set up time steps
v0=0;
delt=1e-9;
time=0:delt:1000e-9; %time column matrix, 1 to 1000e-9, delt increment
```



```

%w.r.t. Single Direct contact --> A_SD
%(Can alternate b/w design using appropriate area)

VPI=sqrt((8*keff*((g0)^3))/(27*eps0*A_SD)); %PI-mode V_PI equation

g=zeros(1, length(time)); %initialize array, g: real time gap wrt time
v=zeros(1, length(time)); %initialize array v: real time v wrt time

% Solve the ODE's with Euler's Method, w.r.t. different VB and/or V_OD
VB = [0:2:10]+eps;
for i=1:length(VB)

    %Uncomment this equation to analyze w.r.t. a single V_OD value:

        %V_OD0 = V_OD(1,5);

    %If using this method, comment out lines corresponding to "n" for loop,
    %so that the "n" for loop does not iterate value of V_OD.
    %

    for n = 1:length(V_OD) %Begin "n" For loop
        V_OD0 = V_OD(n);      %iterate value of V_OD

        VGB(i)=VPI+V_OD0;

        temp=roots([1,-g0, 0, eps0*A_SD*VB(i)*VB(i)/(2*keff)]);
        g0new(i)=temp(1);
        g(1)=g0new(i);
        v(1)=v0;

        for j=2:length(time)
            g(j)=g(j-1)+v(j-1)*delt;
            v(j)=v(j-1)+delt*(1/m)*(-b*v(j-1)+keff*(g0-g(j-1))-
            eps0*A_SD*VGB(i)*VGB(i)/(2*g(j-1)*g(j-1)));
        end
        tdelay(i)=interp1(g(10:end),time(10:end),g0-gd);
        cont_v(i)=interp1(g(10:end),v(10:end),g0-gd);

        figure, subplot(211), plot(time(1:300)/1e-6, g(1:300)/1e-9), xlabel('time
        (\mus)', 'FontSize', 12),ylabel('Gap (nm)', 'FontSize', 12),...
        subplot(212),plot(time(1:300)/1e-6, v(1:300)), xlabel('time (\mus)',
        'FontSize', 12),ylabel('Velocity (m/s)', 'FontSize', 12);

        %The cont_v and tdelay can be extracted manually from the graphs, which
        %iterate the "n" values of V_OD before iterating "i" value of VB.

        %For instance,Graph 2 is for the first VB value and the second V_OD value
        %Graph 30 is for the last VB value and last V_OD value.

        end %end of "n" For loop, which loops V_OD
    end

%Note: Manual extraction not necessary if analyzing w.r.t. single V_OD,
%since the loop will output values w.r.t. "i" value of VB.

```